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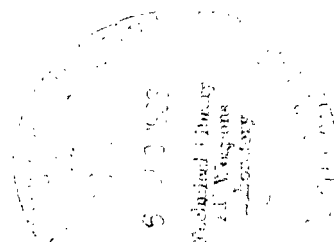
EARTH ORBITAL LIFETIME PREDICTION MODEL AND PROGRAM

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ABSTRACT

An earth orbital satellite lifetime deck has been developed and programmed in Fortran IV language for the IBM 7094. The deck represents the development of a sophisticated and accurate lifetime prediction technique, which includes the effect of aerodynamic drag and the nonspherical gravitational potential of the earth. The computer program can be used to predict lifetime based on only a gross description of the initial orbit and drag parameters, or based on a very exact definition of the initial orbit and detailed description of the drag parameters and their variations depending on the amount of information available. The primary factor contributing to uncertainty in lifetime predictions using this model is the atmospheric density. A very flexible model based on data from Discoverer, Gemini, and Saturn flights has been established. The primary uncertainty remaining in this model is prediction for future years of solar activity behavior and its influence on density as a function of altitude. As additional flight data and solar activity observations become available, they may readily be incorporated into the model, thus providing a rapidly changing density model which insures the best representation possible. Efforts to refine the models as presently defined and to perform pertinent studies in the lifetime area are continuing. This report represents only the present status of model definitions and defines the computer program now in use.

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RESEARCH AND DEVELOPMENT OPERATIONS

TABLE OF CONTENTS

	Page
SUMMARY	1
I. INTRODUCTION.	1
II. DENSITY MODEL.	3
A. Defining a Time-Dependent and Position-Dependent Density Model	4
B. Verification and Accuracy of Present Density Model from Flight Experience	10
C. Prediction of Future Behavior of Parametric Input to the Model	11
III. LIFETIME PROGRAM.	22
A. Notation	22
B. Program Description and Flow of Computations.	26
1. Control Phase	26
2. Transformation Phase.	32
3. Lifetime Phase	35
a. Orbital Parameter Computations.	36
b. Ballistic Parameter Computations.	38
c. Atmospheric Density Options	41
d. Apogee and Perigee Decay Rates at the i^{th} Apogee Integration Step	44
e. Integration of Time and Perigee with Respect to Apogee	46
f. Altitude Interpolations.	48
4. Computer Program Flow Charts	50
a. Block Flow of "Control" Phase	50
b. Block Flow of "LIFE" Routine	51
c. Block Flow of "PDAD" Routine	52
C. Computer Program Input.	54
D. Computer Program Output Options	70
1. Short Output	70
2. Detail Output.	76
3. Normal Output.	83

TABLE OF CONTENTS (Concluded)

	Page
IV. GRAPHIC METHOD FOR LIFETIME PREDICTION.	91
APPENDIX A. DERIVATION OF THE DECAY EQUATIONS	108
APPENDIX B. COMPUTER PROGRAM SOURCE LISTING	145

LIST OF ILLUSTRATIONS

Figure	Title	Page
1.	Ratio of Density for Various Values of S to the 59 ARDC Density.	15
2.	Ratio of Density for Various Values of S to the 62 U. S. Standard Density	16
3.	Exponential Atmospheric Weighting Factor (K) for Effect of Heating.	17
4.	Correction Factor for Density	18
5.	Currently Defined $\overline{F}_{10.7}$ and \overline{K}_p vs Time	19
6.	Currently Defined S vs Time	20
7.	Semiannual Effect on Atmospheric Heating	21
8.	Earth Orbital Lifetime Perigee: 100-650 km Apogee: 450-600 km	94
9.	Earth Orbital Lifetime Perigee: 100-200 km Apogee: 450-1750 km	95
10.	Earth Orbital Lifetime Perigee: 100-600 km Apogee: 200-600 km	96
11.	Earth Orbital Lifetime Perigee: 100-650 km Apogee: 450-6000 km	97
12.	Earth Orbital Lifetime Perigee: 100-200 km Apogee: 450-1750 km	98

LIST OF ILLUSTRATIONS (Concluded)

Figure	Title	Page
13.	Earth Orbital Lifetime Perigee: 100-600 km Apogee: 250-600 km	99
14.	Orbital Drag Coefficient	100
15.	$f_{i,\omega}$ Correction Factor	101
16.	f_d Correction Factor for Nominal Lifetime: 1959 ARDC Reference	102
17.	f_d Correction Factor for Nominal Lifetime: 1962 U. S. Standard Reference	103
18.	f_d Correction Factor for -3σ Lifetime: 1959 ARDC Reference	104
19.	f_d Correction Factor for $+3\sigma$ Lifetime: 1959 ARDC Reference	105
20.	f_d Correction Factor for -3σ Lifetime: 1962 U. S. Standard Reference	106
21.	f_d Correction Factor for $+3\sigma$ Lifetime: 1962 U. S. Standard Reference	107

LIST OF TABLES

Table	Title	Page
I.	Decayed Satellite Analysis	13
II.	Earth Radius as a Function of Inclination (i) and Argument of Perigee (ω)	93

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EARTH ORBITAL LIFETIME PREDICTION MODEL AND PROGRAM

SUMMARY

An earth orbital satellite lifetime deck has been developed and programmed in Fortran IV language for the IBM 7094. The deck represents the development of a sophisticated and accurate lifetime prediction technique, which includes the effect of aerodynamic drag and the nonspherical gravitational potential of the earth. The computer program can be used to predict lifetime based on only a gross description of the initial orbit and drag parameters, or based on a very exact definition of the initial orbit and detailed description of the drag parameters and their variations depending on the amount of information available. The primary factor contributing to uncertainty in lifetime predictions using this model is the atmospheric density. A very flexible model based on data from Discoverer, Gemini, and Saturn flights has been established. The primary uncertainty remaining in this model is prediction for future years of solar activity behavior and its influence on density as a function of altitude. As additional flight data and solar activity observations become available, they may readily be incorporated into the model, thus providing a rapidly changing density model which insures the best representation possible. Efforts to refine the models as presently defined and to perform pertinent studies in the lifetime area are continuing. This report represents only the present status of model definitions and defines the computer program in use.

SECTION I. INTRODUCTION

An extensive effort has been underway to develop a flexible and accurate orbital lifetime prediction model and a density model accurately describing the history of decayed satellites and providing the best available prediction for future satellites. This has been performed jointly by the authors and the Dynamics and Guidance Department of the Lockheed Missiles and Space Company, Huntsville Research and Engineering Center. Lockheed's work has been performed under Contracts NAS8-11148, NAS8-11121 and Task B of NASA Schedule Order No. 1, Contract NAS8-20082. Principal contributors from Lockheed are Mr. T. J.

Richards and Mr. H. F. Kilgo. This report was prepared jointly by MSFC and LMSC, Section V being prepared by Mr. W. B. Hawkins, of Lockheed. The computer program is documented in Reference 1.

The orbital lifetime of a satellite, in the final analysis, depends solely upon two things: the initial total energy of the satellite and the time history of its rate of energy loss. Initial total energy is determined immediately either by position and velocity or by orbit elements. However, the determination of rate of energy loss is not immediately evident. Consider the external influences which act on a satellite to change its orbit: those produced by atmospheric resistance, the earth's nonspherical gravitational potential, lunar-solar gravitation, solar radiation pressure, and geomagnetic potential. Each of these act to change the shape and orientation of the orbital ellipse. Only atmospheric resistance causes a net decrease in total energy. Nevertheless, these other forces are important in determining orbital lifetime because they influence the parameters which define aerodynamic forces.

The development of sophisticated and accurate lifetime prediction and density models has been prompted by the need in the Saturn program for better estimates of lifetime and decay characteristics for earth orbital flight. These data are essential to realistic mission planning.

The basic models have been developed and a computer program written in Fortran language for the IBM 7094. The program simulates the rates of change in the orbit of a satellite and ultimately calculates the total time it remains in orbit. As presently coded, it includes the effects of aerodynamic drag and the earth's nonspherical gravitational potential. The computer program can be used to predict lifetime based on only a gross description of the initial orbit and drag parameters, or on a very exact definition of the initial orbit and detailed description of the drag parameters and their variations, depending upon the amount of information available.

Since the elements in the drag function can be input as constants or variables in a number of ways, their accuracy is limited mainly by the amount of information available to the user. These elements are atmospheric density, drag coefficient, cross-sectional area, and mass of the satellite.

Of principal significance is the atmospheric density model. It was desired to construct a model best predicting density for future years and optimally utilizing data obtained from decayed satellites and actual measurements of solar and geomagnetic activity. Consequently, any "best" density model must remain in a constant state of flux as new data and input become available.

The development of this extensive capability for earth orbital lifetime predictions is by no means completely refined. The basic model and best known inputs to date are formulated for use. A continuing effort is being made to further develop and refine the model. The following list singles out some of the more significant areas either presently being investigated or planned to be investigated. Information concerning these items may be obtained from the authors.

1. The equation used to compute the radius to the satellite as a function of a set of "mean" orbital elements was derived using a definition of "mean" elements which differs from the definition used in the transformation phase of the deck. The deck will be revised to either redefine the function or to redefine the elements to establish a consistent set.

2. The transformation between osculating and "mean" elements required before lifetime computations is indeterminate for small eccentricities. This transformation is being derived.

3. Expressions accounting for the effects of solar radiation pressure have been derived and are being programmed into the deck.

4. Expressions for solar and lunar gravity effects are being derived and will be incorporated into the deck.

5. Uncertainties in extrapolating mean solar activity predictions have been determined. The uncertainties caused by short period fluctuations in solar activity are being established to arrive at an overall uncertainty in predictions for short and long lifetimes.

6. A technique for inclusion of new solar activity data into the density model and automatic updating of the solar activity future predictions based on past and current behavior will be established.

7. Updating of the density model incorporating the latest Saturn flight data is in progress. This will result in a more accurate model in the higher altitude region near 500 km.

SECTION II. DENSITY MODEL

The carefully formulated decay equations presented in following sections for the lifetime model are of little value for application unless an accurate

density model is also used. Any density model which defines density as a function of altitude alone may be in error by an order of magnitude in the 200-700 kilometer altitude range. This section is specifically devoted to discussion of the time-variant density model used in the orbital lifetime program since the model is of such primary significance.

A. Defining a Time-Dependent and Position-Dependent Density Model

For future planning, it is necessary to have the capability of accurately determining the instantaneous acceleration due to drag (for propellant seating considerations, etc.) and the amount the orbit decays during a short period of time. This presents the requirement for an accurate time-dependent and position-dependent model, whereas a less sophisticated model is usually sufficient for an accurate total lifetime prediction.

The density of the upper atmosphere (120-700 km altitude) has been shown to vary with certain indices of solar and geomagnetic activity, with local time, with season and latitude, in addition to its primary variation with altitude. Many of the relationships used in the following model were developed by H. Small in Reference 2.

To describe the variation in density due to solar and geomagnetic activity fluctuations and seasonal effect, Small defines a single parameter, S , and refers to it as a "heating parameter" or the "total heating." The heating parameter S is defined as

$$S = \bar{S} e^{g(t)}, \quad (1)$$

where

$$\bar{S} = 25 + 0.8 \bar{F}_{10.7} + 0.4 (F_{10.7} - \bar{F}_{10.7}) + 10 Kp$$

$$g(t) = .025 \cos \left[2\pi \left(\frac{t - 38047.0}{365.25} \right) \right] - .06 \cos \left[4\pi \left(\frac{t - 38047.0}{365.25} \right) \right]$$

$e^{g(t)}$ = correction for seasonal effects

t = time in modified Julian days

Kp = 3-hour planetary index of geomagnetic activity

$F_{10.7}$ = daily values of the 10.7 cm solar flux

$\overline{F}_{10.7}$ = smoothed values of the 10.7 cm solar flux.

This is formed by taking the running yearly mean of $F_{10.7}$, i.e.,

$$\overline{F}_{10.7} = \frac{1}{365} \sum_{i=-182}^{182} F_{10.7} (t + i) .$$

The daily values of $F_{10.7}$ and K_p , which are available in Reference 3, are incorporated into the model for use in post-flight prediction (section II B deals with extrapolating these values for future predictions).

Small also points out in Reference 2 that the following relationship holds (although he apparently did not use it in formulating his model):

$$\frac{d(\ln \rho)}{d(\ln S)} = \left[3 + 2.5 \left(\frac{h - 360}{240} \right) - .5 \left(\frac{h - 360}{240} \right)^2 \right] \left[\frac{5.6 - \cos \psi'}{6.6} \right] , \quad (2)$$

where

$\ln \rho$ = natural log of density

$\ln S$ = natural log of S

h = altitude in km

ψ' = geocentric angle between the field point and the center of the diurnal bulge. ψ' of 75 deg represents a mean diurnal effect.

By interpreting the above as

$$\frac{\ln \rho - \ln \rho_o}{\ln S - \ln S_o} ,$$

it follows directly that

$$\rho = \rho_o \left(\frac{S}{S_o} \right) \left[3 + 2.5 \left(\frac{h - 360}{240} \right) - .5 \left(\frac{h - 360}{240} \right)^2 \right] \left[\frac{5.6 - \cos \psi'}{6.6} \right] . \quad (3)$$

To apply the above equation, all that remained was the selection of a realistic density profile (density as a function of altitude) to define ρ_o and the associated value of S_o .

Values from the above equation using various combinations of S_o and ρ_o (reference profiles) were compared to empirical density data. The results of this comparison indicated that two such combinations provide realistic density models. These are the 1959 ARDC density model with an S_o of 220 and the 1962 U. S. Standard density model with an S_o of 200.

Figures 1 and 2 show $\frac{\rho}{\rho_o}$ when $\psi' = 75^\circ$ (mean diurnal effect)

$$\frac{\rho}{\rho_o} = \left(\frac{S}{S_o} \right)^{.81} \left[3 + 2.5 \left(\frac{h - 360}{240} \right) - .5 \left(\frac{h - 360}{240} \right)^2 \right] ,$$

for various values of S and $S_o = 220$ and $S_o = 200$, respectively.

These two reference atmospheres, the 1959 ARDC and U. S. Standard 1962, are used in the program. Lifetimes may be predicted solely on these models or using these models as a base with corrections for the time frame being considered as discussed above and adjusted with data obtained from flights. The selection of a model for the base is completely arbitrary. Essentially the same density model will result for either base reference. The base model is corrected in the program for solar activity behavior and diurnal effect in the following manner:

$$\rho = \rho_o (R'_1) D_c \left(\frac{S}{S_o} \right)^K \left\{ \frac{1 + .19 (e^{.0055 R'_1} - 1.9) \left(\frac{1 + \cos \psi'}{2} \right)^3}{1 + .19 (e^{.0055 R'_1} - 1.9) \left(\frac{1 + \cos 75^\circ}{2} \right)^3} \right\} , \quad (4)$$

where

$\rho_o(R_i')$ = Density of base reference atmosphere as a function of altitude R_i' . This is assumed to be a diurnal mean atmosphere.

D_c = Altitude dependent correction factor derived from satellite observations (discussed later in some detail).

S_o = Reference index of heating parameter, i. e. , the value of S to which the D_c factor is referenced.

R_i' = Field point altitude above an oblate earth

ψ' = Angle between the field point and the center of the diurnal bulge.

The heating effect on atmospheric density is altitude dependent and the density is greater on the side of the earth toward the sun. The latter effect, the diurnal bulge, is represented by the brackets

$$\left\{ \frac{1 + .19 (e^{.0055R_i'} - 1.9) \left(\frac{1 + \cos \psi'}{2} \right)^3}{1 + .19 (e^{.0055R_i'} - 1.9) \left(\frac{1 + \cos 75^\circ}{2} \right)^3} \right\}$$

and is derived in Reference 4. The formulation given above assumes that the base atmosphere represents a mean diurnal effect so that, when ψ' equals the mean value of 75 degrees the ratio becomes one (1) for any altitude (ψ' is derived below). The variation in the effect of the heating parameter with altitude and position on ρ is represented in the equation (Reference 2) by K, where

$$K = \left[3 + \frac{5}{2} \left(\frac{R_i' - 360}{240} \right) - \frac{1}{2} \left(\frac{R_i' - 360}{240} \right)^2 \right] \left[\frac{5.6 - \cos \psi'}{6.6} \right]. \quad (5)$$

This exponent K is shown in Figure 3 as a function of altitude. The angle ψ' is calculated as follows:

$$\cos \psi' = ll_B + mm_B + nn_B, \quad (6)$$

(l, m, n) = direction cosines of the field point

$$l = \frac{X_s}{R_i}$$

$$m = \frac{Y_s}{R_i}$$

$$n = \frac{Z_s}{R_i} \quad .$$

R_i = Radius vector from earth center to field point. X_s , Y_s , Z_s are the space-fixed components of the position of the vehicle computed as

$$X_s = X' \cos \Omega - Y' \sin \Omega$$

$$Y_s = X' \sin \Omega + Y' \cos \Omega$$

$$Z_s = Z'$$

$$X' = X$$

$$Z' = Y \sin i$$

and

$$X = R_i \cos (\omega + v)$$

$$Y = R_i \sin (\omega + v)$$

i = orbital inclination - angle between the earth equatorial plane and the plane of the orbit

Ω = Right ascension of the ascending node-angle between the intersection of the orbital plane with the earth equatorial plane and the vernal equinox

ω = Argument of perigee-angle between the ascending node and perigee

v = True anomaly-angle between perigee and the field point

(l_B, m_B, n_B) = Direction cosines of the diurnal bulge

$$l_B = \sqrt{n_s^2 + l_s^2} \cos RA_B \quad (7)$$

$$m_B = \sqrt{n_s^2 + l_s^2} \sin RA_B \quad (8)$$

$$n_B = n_s \quad (9)$$

$$\begin{pmatrix} l_s \\ m_s \\ n_s \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \epsilon & -\sin \epsilon \\ 0 & \sin \epsilon & \cos \epsilon \end{pmatrix} \begin{pmatrix} \cos \lambda_s \\ \sin \lambda_s \\ 0 \end{pmatrix} \quad (10)$$

ϵ = inclination of the ecliptic = 0.4092 rad

λ_s = celestial longitude of the sun

$\lambda_s = [0.017203 \text{ d} + .0335 \sin (0.017203 \text{ d}) - 1.41] \text{ rad}$

d = number of days elapsed since Dec. 31, 1957

$$RA_s = \tan^{-1} \left(\frac{m_s}{l_s} \right)$$

$$RA_B = RA_s - \theta$$

$$\theta_{\text{Radians}} = \frac{\pi}{180} [18.5 + 30e^{K_1} + K_2\sigma + (1 - \sigma^2)]$$

if $\theta > 5$ set $\theta = 5$

$$\sigma = \frac{s - 160}{90}$$

$$K_1 = -.00567 (R_i - 200) + e^{-.01455(R_i' - 200)}$$

$$K_2 = 18.5 + 21.5e^{-.0315(R_i' - 200)} .$$

B. Verification and Accuracy of Present Density Model From Flight Experience

The effective drag on the Saturn vehicle has been derived at MSFC primarily by the inclusion of drag as an additional unknown which is solved for in a conventional least square differential correction orbit determination program as discussed in Reference 5. The orbit correction program used included an atmospheric drag model which used the 1959 ARDC atmospheric density profile and assumed a constant ballistic factor for the satellite. The drag acceleration A_D on the satellite was calculated as

$$A_D = \frac{1}{2} D_c (C_D A/M) \rho_o v_e^2 , \quad (11)$$

where C_D is the drag coefficient, A is the effective cross-sectional area, M is the satellite mass, v_e is the velocity relative to the earth, ρ_o is the reference atmospheric density at the satellite, and D_c is a constant used nominally to compensate for variation of the actual current atmospheric density from the 1959 ARDC density profile. Solutions for D_c were made for SA-5, SA-6 and SA-7 using radar tracking data in the orbit correction process described in Reference 5. Using these data in addition to Gemini and Discoverer data, a correction factor from the 1959 ARDC atmosphere was established as shown in Figure 4. These factors are referenced to an index of heating S of 100 which was applicable during the Saturn I flight time frame. Using these empirically derived solutions in the new jointly developed MSFC/LMSC lifetime program, a comparison of actual to predicted lifetime was made for 39 decayed satellites. The results of this comparison are presented in Table I.

As an indication of the accuracy of the prediction, the ratio of actual lifetime to predicted lifetime is shown in Table I for each case. This ratio

(A/P) appears to be normally distributed, having a mean value of 1.000 and a standard deviation of .082. These results indicate that the representation of solar activity as presented and the corresponding density as a function of time for the altitude region of 350 km and below is indeed valid for the time frame up to 1965. The validity for future years is only as good as the prediction of solar activity.

Similar density models are currently being investigated: one using the 59 ARDC as the reference density model, $S_0 = 220$ and $DC = 1.0$ for all altitudes, and another using the 62 U. S. Standard as the reference density, $S_0 = 200$, and $DC = 1.0$ for all altitudes. These yield essentially the same density as the one previously mentioned ($S_0 = 100$, DC shown in Figure 4) in the 100-300 km altitude range and are currently being compared to data obtained in the 490-550 km altitude range from SA-8, SA-9, and SA-10 flights.

C. Prediction of Future Behavior of Parametric Input to the Model

Examination of the history of solar activity indicates that the present cycle need not necessarily follow a course similar to the last cycle. The $\overline{F}_{10.7}$ and \overline{K}_p for the period 1958-1975, which are currently being used in the MSFC computer program, are shown in Figure 5. Figure 6 shows the heating parameter \overline{S} based on the nominal values of $\overline{F}_{10.7}$ and \overline{K}_p given in Figure 5. The seasonal effect $eg^{(t)}$ on S is shown in Figure 7 as a function of the time of the year. The product of these two factors yields the heating parameter S . The $\overline{F}_{10.7}$ and \overline{K}_p values which occurred earlier than mid-1965 are averages of the actual recorded values, while those from mid-1965 to 1975 are based upon certain predictions and assumptions.

The extrapolation of $\overline{F}_{10.7}$ was based on the following assumptions:

1. $\overline{F}_{10.7}$ and Zurich smoothed sunspot number, R , are well correlated and the regression line is given by Reference 6 as

$$\overline{F}_{10.7} = 50 + .967 R \quad (\overline{F}_{10.7} > 100)$$

and

$$\overline{F}_{10} = 68 + .607 R \quad (F_{10.7} < 100) .$$

2. The beginning of the new cycle (minimum $\overline{F}_{10.7}$) was in mid-1964.
3. The new sunspot cycle was assumed to have the shape and duration of the mean of sunspot cycles 8 through 18.
4. The magnitude of the sunspot maximum, R_M , was assigned the value 150, based on the following:
 - (a) All predictions of R_M thus far found in the literature agree that R_M will be less than 150 (except one which indicates that $R_M < 160$).
 - (b) In predicting lifetimes for mission planning, it is generally better to underpredict lifetime than to overpredict lifetime.
 - (c) While most authors predict a value of R_M considerably lower than 150, the likelihood of this is questionable in view of the fact that the preceding cycle had the highest R_M ever recorded and natural phenomena tend not to change drastically from one occurrence to the next.
5. The time lapse of four years from minimum to maximum sunspot number for the new cycle is the same as that for the mean of cycles 8 through 18. The relationships of consideration 1 above were used to compute $\overline{F}_{10.7}$ from the R values obtained by adjusting the mean of cycles 8 through 18 by a proportionality factor which forced R_M to be 150.

The 3σ upper bound curve of $\overline{F}_{10.7}$, $\overline{F}_{10.7}(\text{max})$, was drawn by fairing straight line segments through points computed by the following formula:

$$\overline{F}_{10.7}(\text{max}) = \overline{F}_{10.7} + .2(\overline{F}_{10.7} - 60) + 4(\text{year} - 1964.5) \quad (12)$$

This formula was chosen to represent the increasing uncertainty in $\overline{F}_{10.7}$ as $\overline{F}_{10.7}$ increases and as time increases. The weighting factors were chosen so as to yield

$$\overline{F}_{10.7}(\text{max}) = 244 \text{ at } 1968.5.$$

The 244 maximum of the previous cycle was chosen as an absolute maximum for the new cycle. The 3σ lower bound was derived similarly from the lowest recorded cycle.

TABLE I. DECAYED SATELLITE ANALYSIS

	Name	t_s (year)	h_p (km)	A (days)	P (days)	R (A/P)
1	58 DELTA 2	1959.158	207	404.0	364.0	1.11
2	58 DELTA 2	1959.725	199	197.7	179.5	1.10
3	58 ZETA	1958.966	175	33.6	33.2	1.01
4	59 GAMMA	1959.287	257	11.2	10.7	1.05
5	59 EPSILON	1959.621	215	43.4	39.9	1.09
6	59 ZETA	1959.637	218	60.7	51.6	1.18
7	59 LAMBDA	1959.889	187	108.3	110.0	0.98
8	59 EPSILON 2	1960.125	219	362.0	355.5	1.02
9	60 DELTA	1960.294	173	9.83	10.6	0.93
10	60 THETA	1960.615	256	95.0	106.6	0.89
11	60 OMICRON	1960.880	183	42.9	42.7	1.01
12	60 SIGMA	1960.960	251	107.4	113.0	0.95
13	60 TAU	1960.973	195	32.9	33.8	0.97
14	61 EPSILON	1961.135	298	525.5	575.3	0.91
15	61 ZETA	1961.146	252	422.6	460.7	0.92
16	61 LAMBDA 1	1961.272	297	372.9	384.8	0.97
17	61 LAMBDA 2	1961.321	220	391.2	429.6	0.91
18	61 XI	1961.466	224	23.2	27.8	0.83
19	61 PI	1961.537	233	133.9	143.4	0.93
20	61 ALPHA BETA	1961.745	243	27.3	27.3	1.00
21	61 ALPHA GAMMA	1961.803	234	24.9	25.0	1.00
22	61 ALPHA EPSILON	1961.855	246	394.3	413.0	0.95
23	61 ALPHA KAPPA	1961.973	248	76.8	74.6	1.03
24	62 RHO	1962.356	203	15.6	13.1	1.19
25	62 CHI	1962.435	213	20.6	19.5	1.06
26	62 ALPHA GAMMA	1962.496	209	76.2	79.6	0.96
27	62 SIGMA	1962.556	323	492.0	484.2	1.02
28	62 ALPHA ETA	1962.575	204	16.5	15.8	1.04
29	62 ALPHA THETA	1962.594	206	18.6	18.2	1.02
30	62 ALPHA KAPPA	1962.602	208	18.3	20.0	0.92
31	62 ALPHA SIGMA	1962.673	176	6.9	7.1	0.97

t_s = initial time, h_p = initial perigee altitude, A = actual lifetime, P = predicted lifetime.

TABLE I. (Concluded)

Name		t_s (year)	h_p (km)	A (days)	P (days)	R (A/P)
32	62 ALPHA CHI	1962.728	211	56.9	56.8	1.00
33	62 BETA EPSILON	1962.797	220	29.5	26.8	1.10
34	62 BETA OMICRON	1962.865	210	20.1	20.4	0.99
35	62 BETA SIGMA	1962.928	134	3.6	3.85	0.94
36	62 BETA PHI	1962.980	200	16.1	15.15	1.06
37	64 (GEMINI)	1964.274	164	4.2	5.09	0.86
38	64 (SA-6)	1964.408	182	3.2	3.21	1.00
39	64 (SA-7)	1964.716	185	3.8	3.3	1.15

t_s = initial time, h_p = initial perigee altitude, A = actual lifetime, P = predicted lifetime.

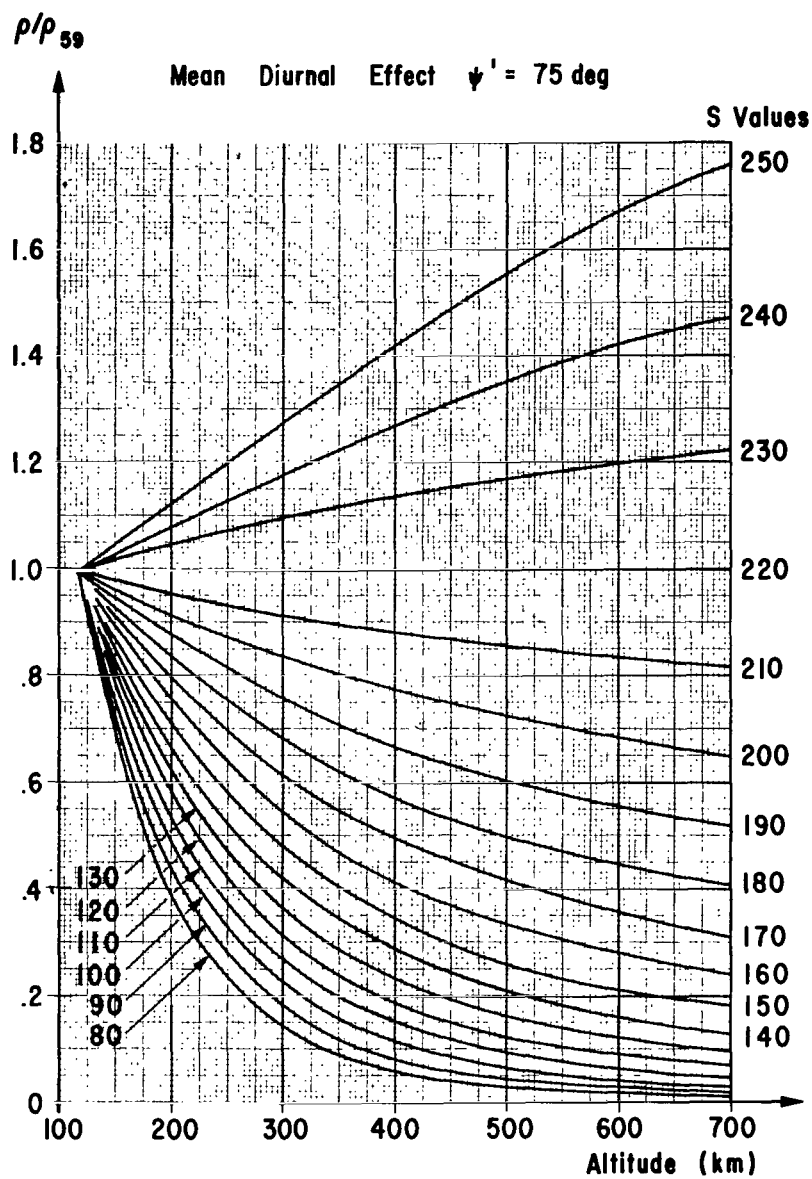


FIGURE 1. RATIO OF DENSITY FOR VARIOUS VALUES OF S TO THE 59 ARDC DENSITY

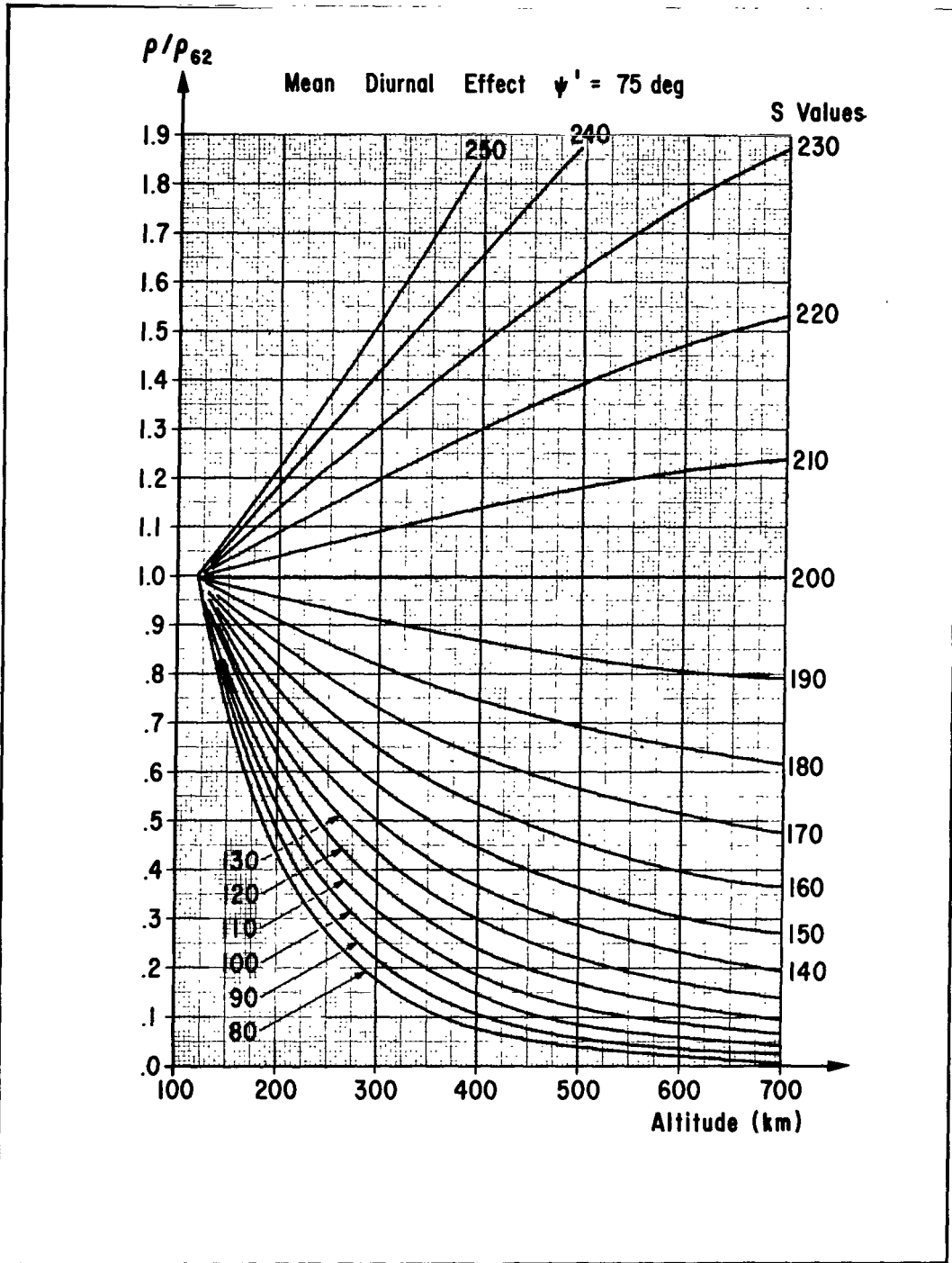


FIGURE 2. RATIO OF DENSITY FOR VARIOUS VALUES OF S TO THE 62 U.S. STANDARD DENSITY

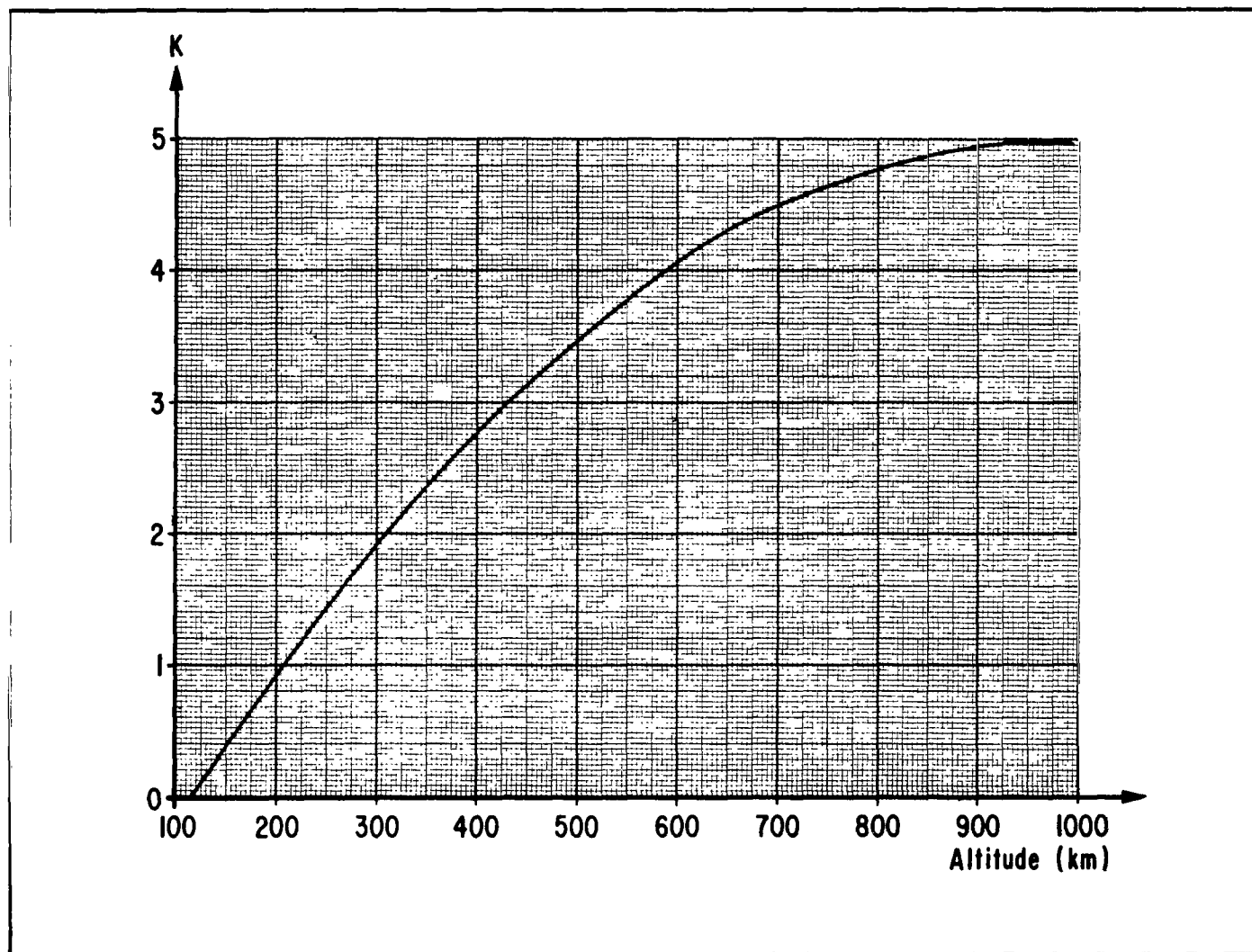


FIGURE 3. EXPONENTIAL ATMOSPHERIC WEIGHTING FACTOR (K) FOR EFFECT OF HEATING

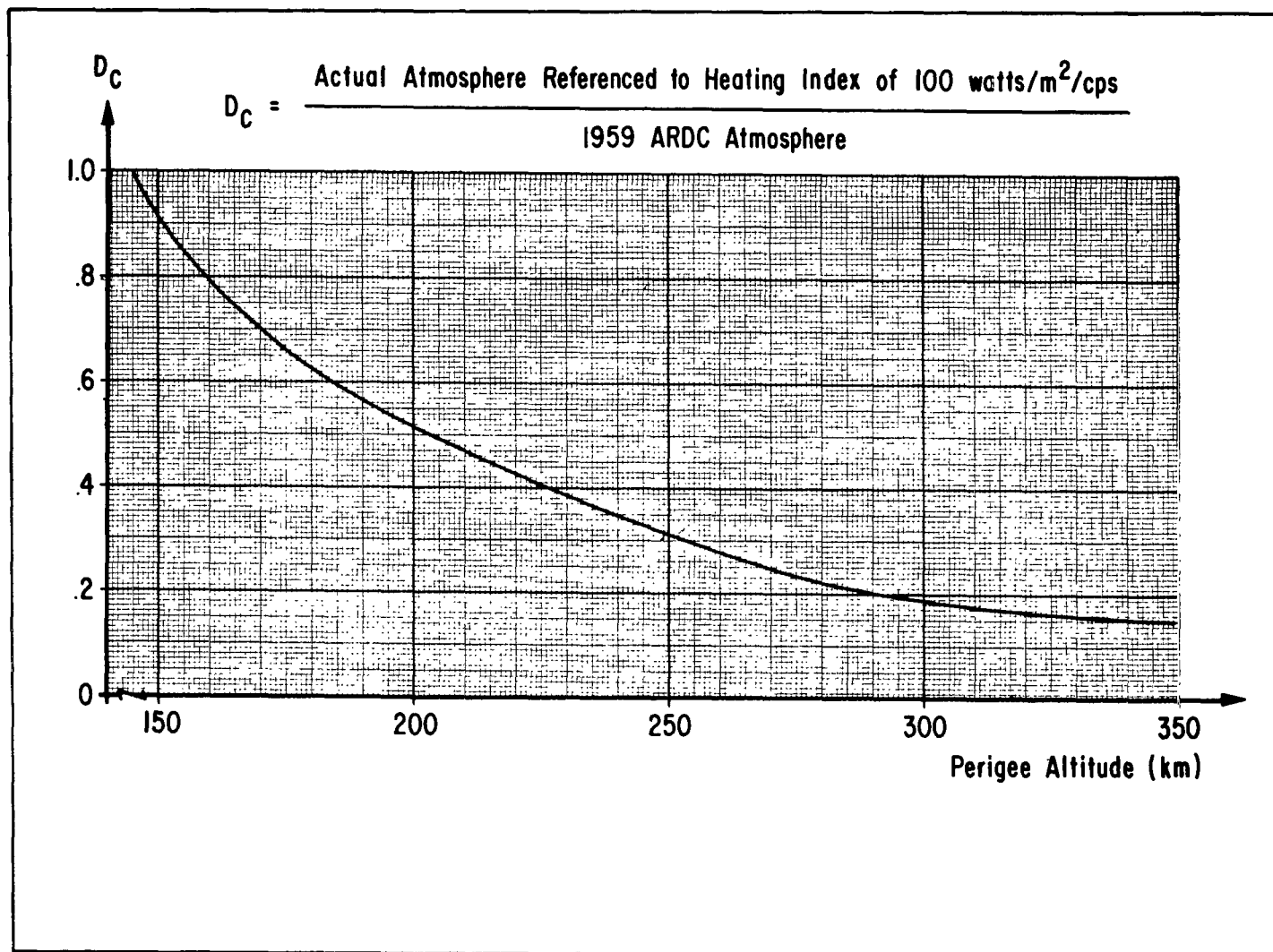


FIGURE 4. CORRECTION FACTOR FOR DENSITY

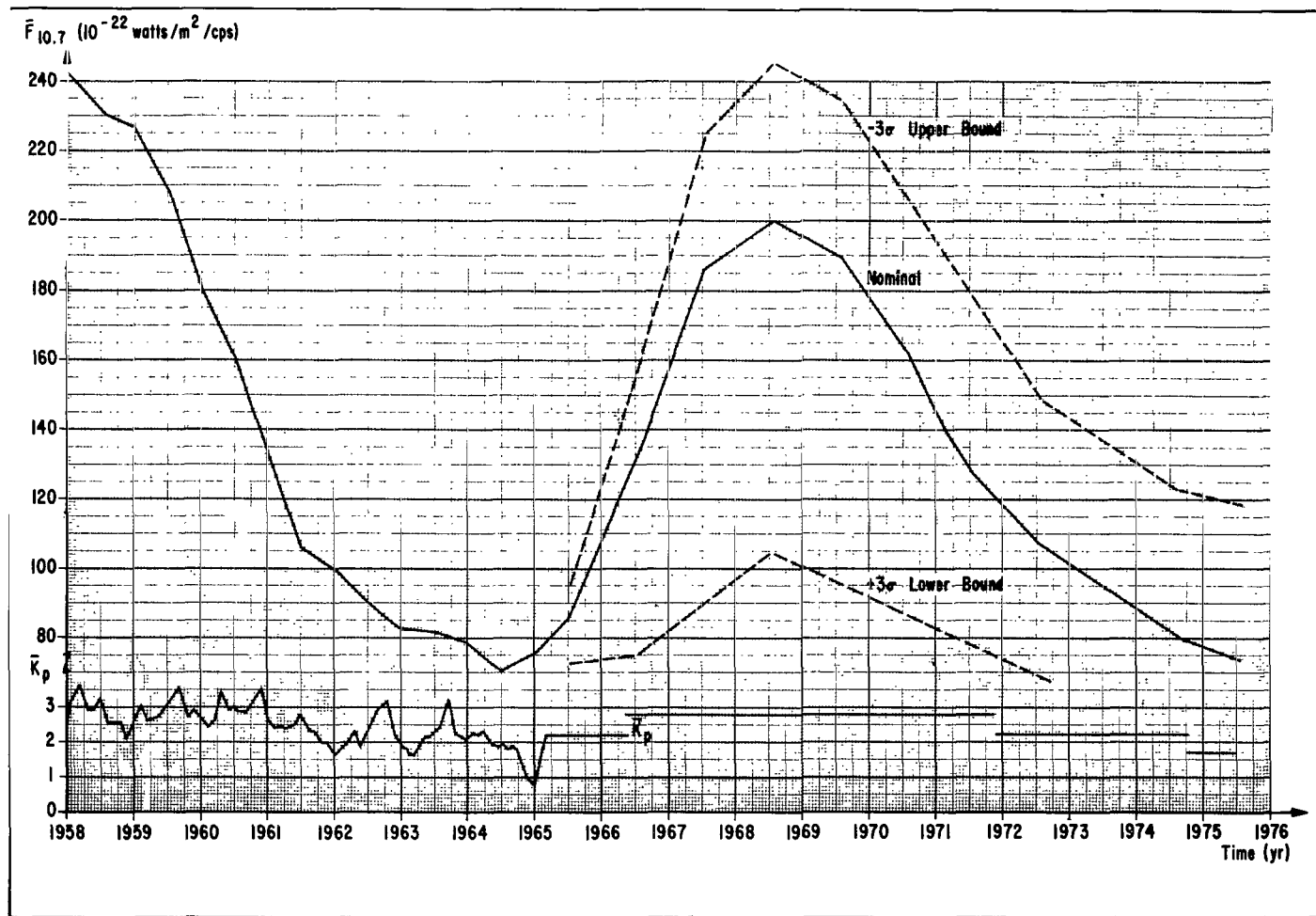


FIGURE 5. CURRENTLY DEFINED $\bar{F}_{10.7}$ AND \bar{K}_p VERSUS TIME

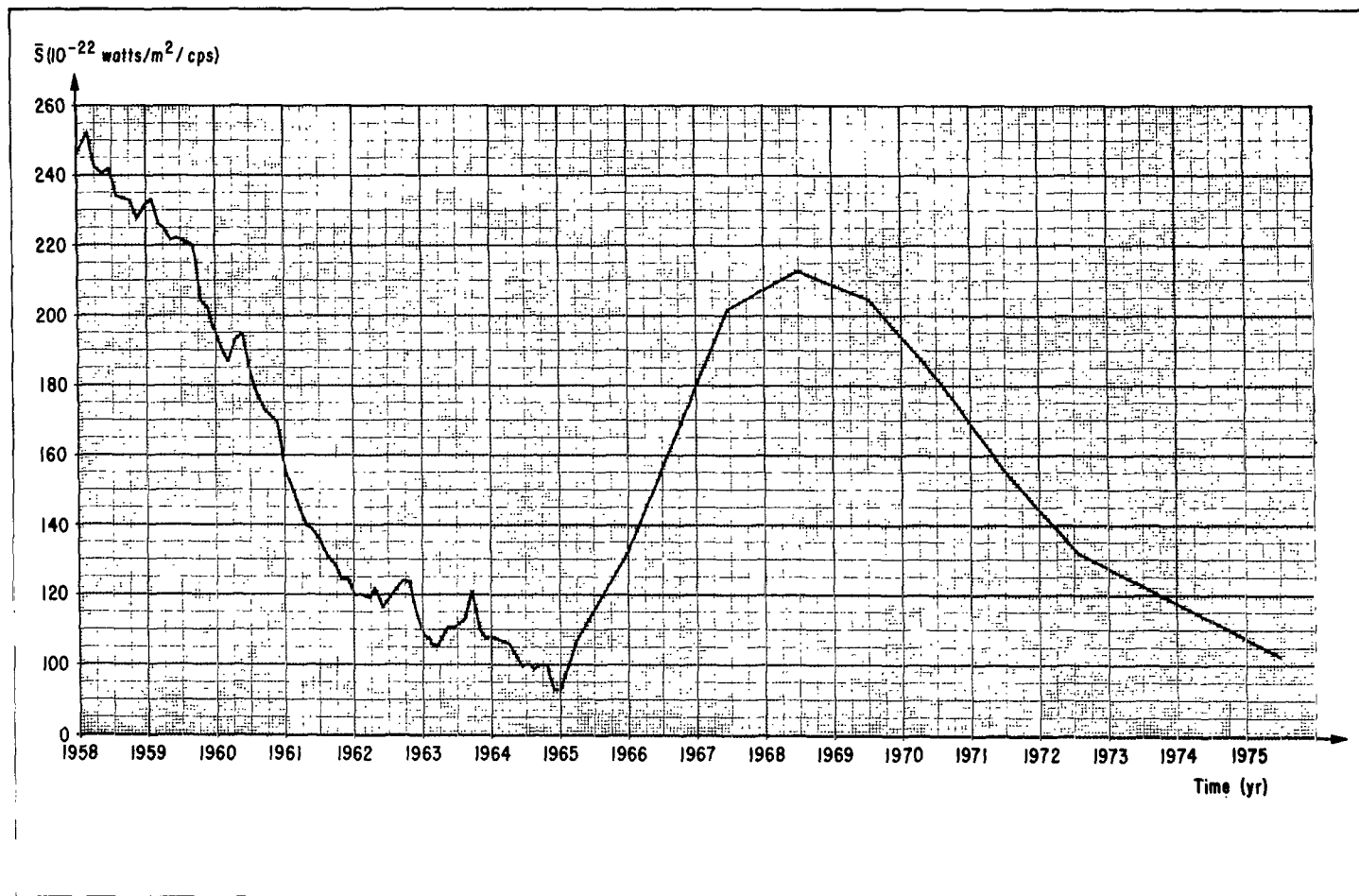


FIGURE 6. CURRENTLY DEFINED \bar{S} VERSUS TIME

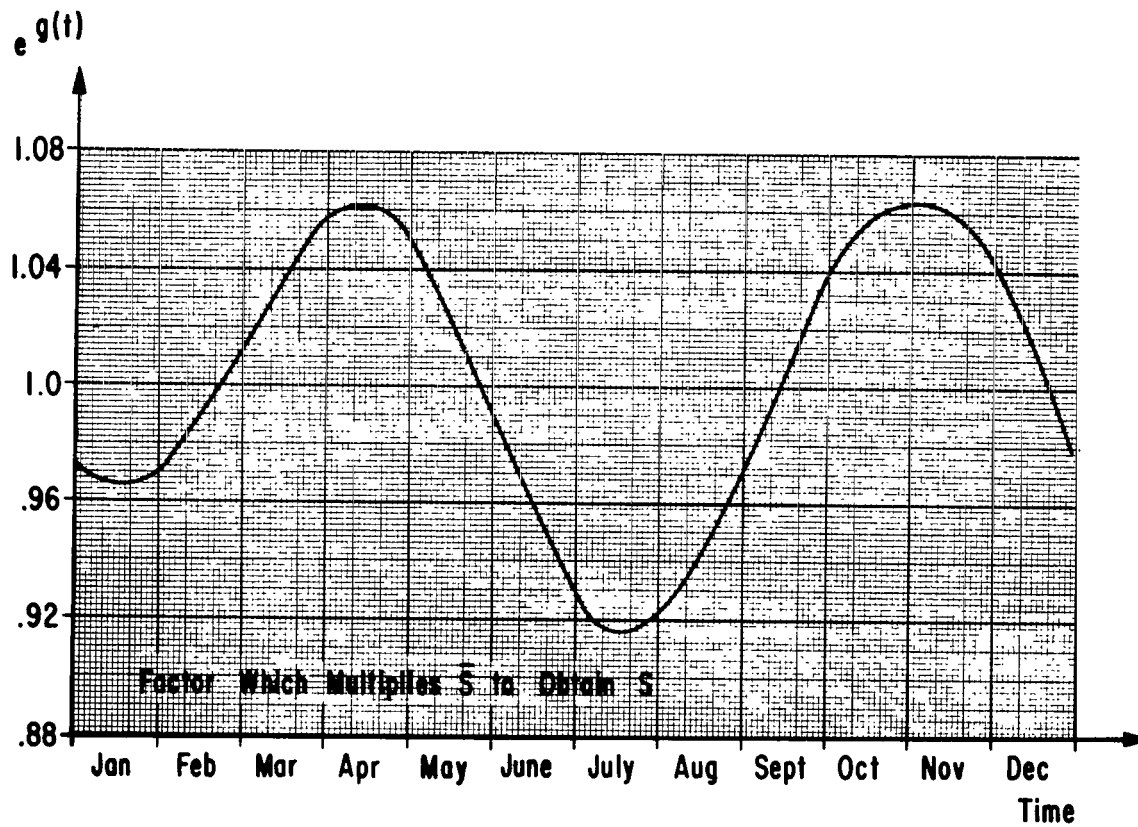


FIGURE 7. SEMIANNUAL EFFECT ON ATMOSPHERIC HEATING

III. LIFETIME PROGRAM

A. NOTATION

This list defines the equation symbols in terms of the computer input language used.

Equation Symbol	Program Symbol	Definition	Units
A_i, A_0	APO	apogee radius	km
\dot{A}_i	ADOT	time rate of change of apogee radius	km/day
\dot{A}'_i	ADOTP	$M(t)\dot{A}_i$	kg-km/day
A_{N_j}	AN	interpolated value of apogee at time T_{A_j} ($j = 1...5$)	km
A_{0_i}	ARAA	effective drag area of the orbiting vehicle	m^2
CD'_i	CDP	coefficient of drag as an altitude function	non-dimensional
CN_i	CNN	coefficient of drag as an attitude function	"
D	DD	coefficient of the 4th zonal harmonic of the earth's gravitational potential	"
F	F	reciprocal of the flattening of the earth (298.3)	"
$F_{10.7}$	FTEN	daily 10.7 cm solar flux	10^{-22} watts/ m^2 /cycle/sec
$\bar{F}_{10.7}$	FTENB	yearly mean values of $F_{10.7}$	"
H	HH	coefficient of the 3rd zonal harmonic of the earth's gravitational potential	non-dimensional
J	JJ	coefficient of the 2nd zonal harmonic of the earth's gravitational potential	"
K	KERTH	earth's gravitational constant	km^3/sec^2

(Continued)

Equation Symbol	Program Symbol	Definition	Units
K_P	AP	daily mean values of geomagnetic index	non-dimensional
$K\rho$	XK	$\partial \log_e \rho / \partial \log_e S$	"
$M(t)$	MT	mass of orbiting vehicle at time t	kg
PD_i	PDI	anomalistic period (time between two successive perigee passages)	min
P_i, P_0	PERI	perigee radius	km
\dot{P}_i	PDOT	time rate of change of perigee radius	km/day
\dot{P}_i'	PDOTP	$M(t)\dot{P}_i$	kg-km/day
P_{N_k}	PN	interpolated value of perigee at time T_{P_k} ($k = 1...5$)	km
R_{AB}	RAB	right ascension of the center of the diurnal bulge	deg
R_{AS}	RAS	right ascension of the sun	deg
R_E	AE	earth's equatorial radius	km
R_i	RI	radius to probe	km
R_i'	RIP	altitude to probe	km
RPA_i	RPAI	sub-perigee apogee earth radius	km
S	SS	current index of total heating of the atmosphere	non-dimensional
S_0	SO	reference index of total heating of the atmosphere	"

(Continued)

(Continued)

Equation Symbol	Program Symbol	Definition	Units
$T_{A_j} = 1...5$	INTERA	times at which apogee interpolations are performed	days
$T_{P_k} = 1...5$	INTERP	times at which perigee interpolations are performed	days
VP_i	VPI	earth-fixed velocity at perigee	km/sec
X_s, Y_s, Z_s	XS, YS, ZS	space-fixed ephemeris components of the position of the satellite (see Section II-B-2)	km
a_i, a_0	AI	semi-major axis of the ellipse	km
\dot{a}_i	SADOTI	time rate of change of semi-major axis	km/day
d	XDATE	number of days elapsed since 31 December 1957	days
e_i, e_0	EI	eccentricity	non-dimensional
i	INC	inclination	deg
l, m, n	XL, XM, XN	direction cosines of the satellite	non-dimensional
l_B, m_B, n_B	XLB, XMB, XNB	direction cosines of the center of the diurnal bulge	"
l_s, m_s, n_s	XLS, XMS, XNS	direction cosines of the vector to the sun	"
n_i, n_0	NI	mean motion	deg/day
t	TTT	universal time	hrs
t_i	TIME	time in orbit	days
t_{n_i}	REVOL	number of revolutions made by the satellite	non-dimensional

(Continued)

Equation Symbol	Program Symbol	Definition	Units
Δt_i	DTI	change in time for one apogee step	days
θ	THETA	sidereal time	deg
θ_ρ	XLAG	lag angle between earth-sun line and the diurnal bulge	deg
Ω_i, Ω_0	CAPW	right ascension of the ascending node	deg
$\dot{\Omega}_i, \dot{\Omega}_0$	CAPID	time rate of change of ascending node	deg/day
α_i	ALPHA	angle of attack of the satellite	deg
ΔA	DA	apogee integration step size	km
ϵ	ECLIPT	obliquity of the ecliptic	deg
λ_s	XLAMS	celestial longitude of the sun	deg
v_i, v_0	E	true anomaly	deg
ρ	RHO	atmospheric density	kg/m ²
ψ	COSPP	angle between the center of the diurnal bulge and the satellite	deg
ω_e	OMEGA	rotational velocity of the earth	deg/hr
ω_i, ω_0	SMAW	argument of perigee	deg
$\dot{\omega}_i, \dot{\omega}_0$	SMAID	time rate of change of argument of perigee	deg/day

Subscripted symbols such as ω_i, Ω_i, A_i denote values at the i^{th} apogee step, whereas ω_0, Ω_0, A_0 denote initial values.

B. Program Description and Flow of Computations

The Satellite Orbit Decay and Orbital Lifetime Program has three phases: (1) a control phase that controls the sequence of events in the entire program; (2) a transformation phase that accepts input in any of eight coordinate systems and transforms to the remaining seven; and (3) a lifetime phase that computes the decay history and lifetime of the orbiting body. The deck is programmed in Fortran IV language for the IBM 7094 computer.

1. Control Phase. This phase determines the route to be taken and the values to be used in computing both the decay history and lifetime. The Control Phase first calls the input routine "MAVRIK" which reads one or more data cards for the initial case. The only card that is always required for execution of the program is the one that defines either the satellite's initial position and velocity or orbit elements in one of eight optional coordinate systems. However, the actual breakdown of these options leads to more ways of inputting these initial orbit parameters than eight. The following outline elaborates on this.

The user can input in any one of eight coordinate systems, two of which contain three coordinate "subsystems"* each:

1. Earth-fixed plumbline (position and velocity)
2. Earth-fixed ephemeris (position and velocity)
3. Space-fixed ephemeris (position and velocity)
4. Space-fixed geographic (position and velocity)
5. Earth-fixed geographic (position and velocity)
6. Platform (position and velocity)
7. Osculating orbital elements:
 - (a) Semi-major axis, eccentricity, inclination, right ascension of ascending node, argument of perigee, and true anomaly (alphanumeric code OET).

*In effect, there are 12 coordinate systems.

- (b) Semi-major axis, eccentricity, inclination, right ascension of ascending node, argument of perigee, and eccentric anomaly (OEE).
- (c) Semi-major axis, eccentricity, inclination, right ascension of ascending node, argument of perigee, and mean anomaly (OEM).

8. Mean orbital elements:

- (a) Same as (7) except mean elements replace osculating elements. Corresponding alphanumeric codes are MOT, MOE, and MOM.

The coordinate systems described previously are explained in detail in Section III. B. 2.

Each of the six coordinate "subsystems" in (7) and (8) above can be input in one of four optional ways:

- A Apogee and perigee radius.
- B Apogee and perigee radius, inclination, right ascension of ascending node, (true, eccentric, or mean) anomaly, argument of perigee, universal time, sidereal time.
- C Semi-major axis and eccentricity.
- D Semi-major axis, eccentricity, inclination, right ascension of ascending node, (true, eccentric, or mean) anomaly, argument of perigee, universal time, and sidereal time.

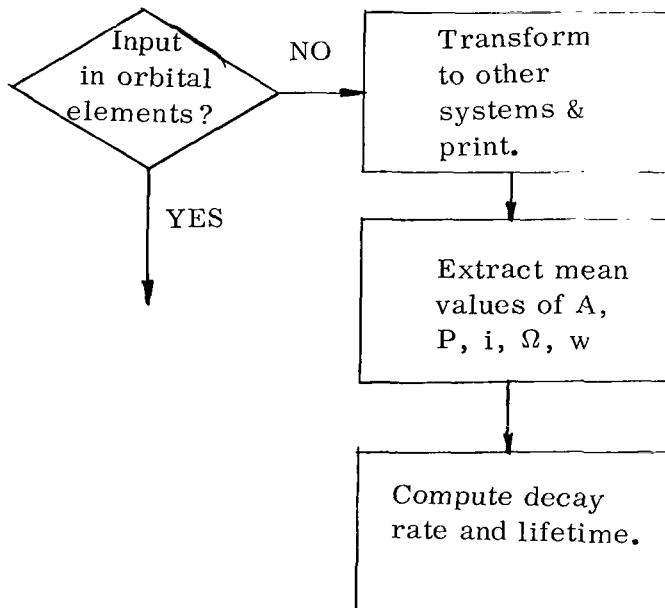
In option A and C the apogee radius, perigee radius, semi-major axis, and eccentricity are treated as mean elements whether they are mean or osculating. This is the case since the other elements required for the transformation between osculating and mean elements are not given. Nominal values of inclination, right ascension of ascending node, (true, eccentric, and mean) anomaly, argument of perigee, universal time, and sidereal time are built into the program. For orbits having elements grossly different from these, use options B or D. Options A and C should be used only if a bare minimum of information is available.

After calling "MAVRIK," the control phase logically decides whether input is position and velocity or orbit elements. If it decides that an orbital element system was not used, then the program proceeds immediately to the transformation phase; if an orbital element was used, further decision-making is required by the control phase. In all cases except options A and C of the orbital element system the program uses the transformation phase. However, when either options A or C are chosen the transformation phase is not used since it is unlikely that one would desire transformation based on "nominal" values of i , Ω , w , etc.

a. Orbital Element System Not Used. If the coordinate system input is other than orbital elements, such as earth-fixed geographic (EFG), then the following events occur:

1. Transform EFG to the remaining seven systems.
2. Print transformations.
3. Extract from mean orbital elements the following: apogee radius, perigee radius, inclination, right ascension of ascending node, and argument of perigee. These elements are then ready for use in the lifetime phase.

Logical Flow:



Option B

If any of positions 3 through 8 are non-zero, then the input is assumed to be in the form:

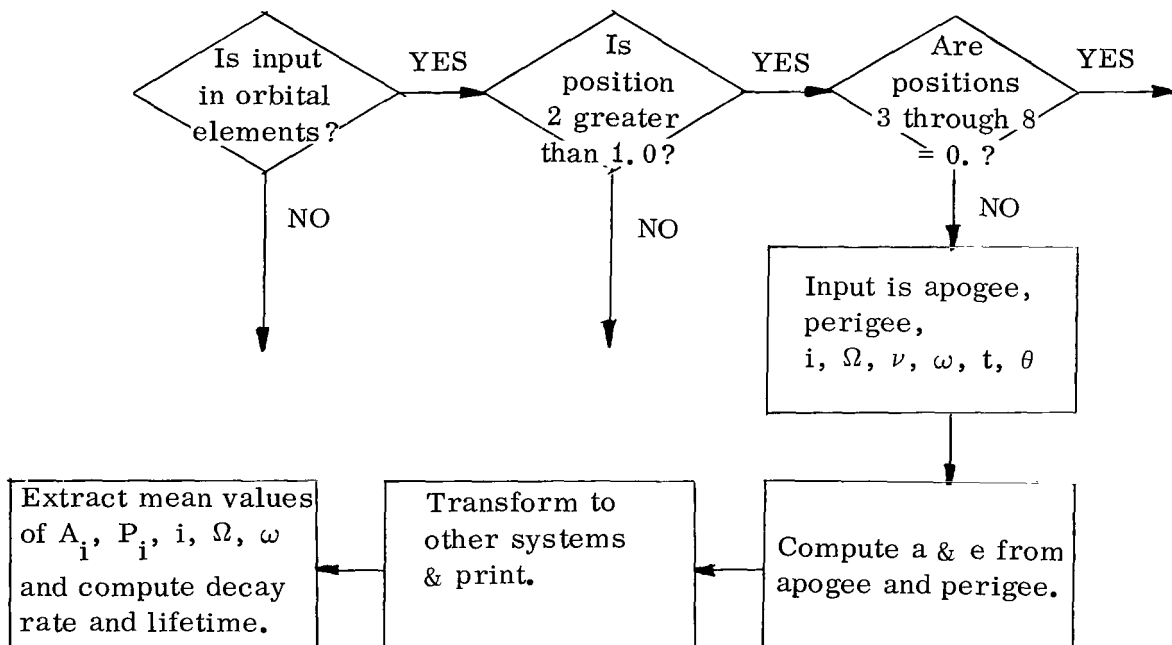
OET = apogee radius) perigee radius) inclination) right ascension of node)
true anomaly) argument of perigee) universal time) sidereal time).

Semi-major axis and eccentricity are computed from the input values of apogee and perigee radius:

$$a_o = \frac{A_o + P_o}{2}, \quad e_o = \frac{A_o - P_o}{A_o + P_o}.$$

These elements are now in the format required for transformation not only to mean elements for use in the lifetime phase, but also to the elements in the remaining coordinate systems for display in the printout.

Logical Flow:



Option C

If position 2 is less than 1.0, then positions 3 through 8 are tested. If these positions are all zero then the input is in the form:

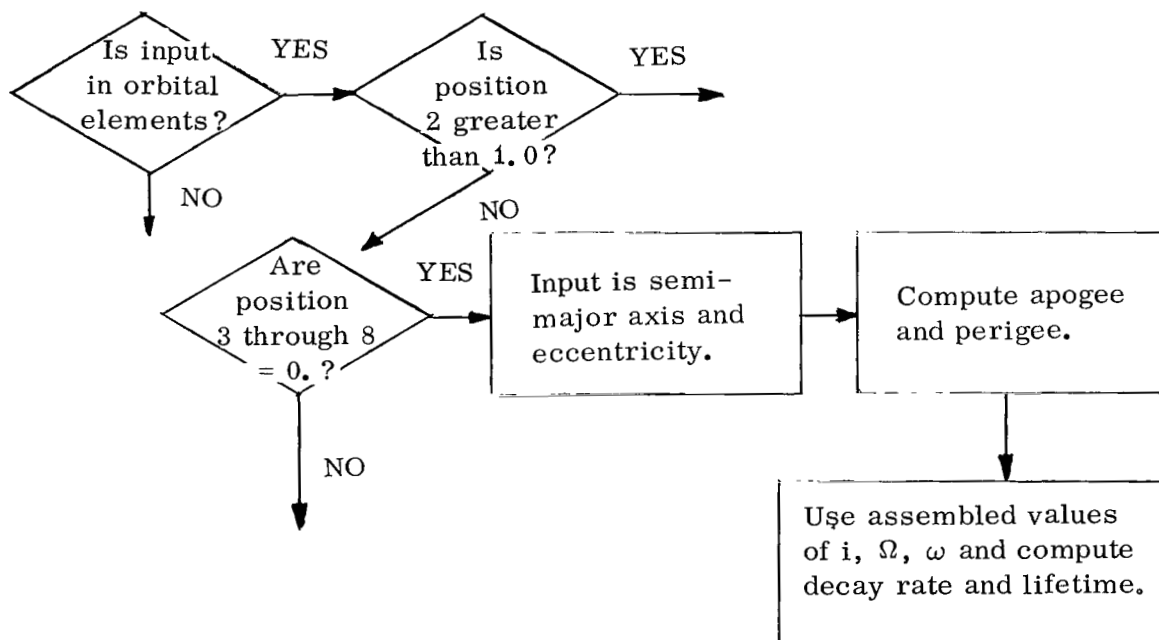
$$\text{OET} = \text{semi-major axis) eccentricity}.$$

From these two values, apogee and perigee radius are calculated:

$$A_o = a_o (1. + e_o) \qquad P_o = a_o (1. - e_o)$$

These values are used along with the assembled "nominal" values of inclination, right ascension of ascending node, and argument of perigee in the lifetime phase.

Logical Flow:



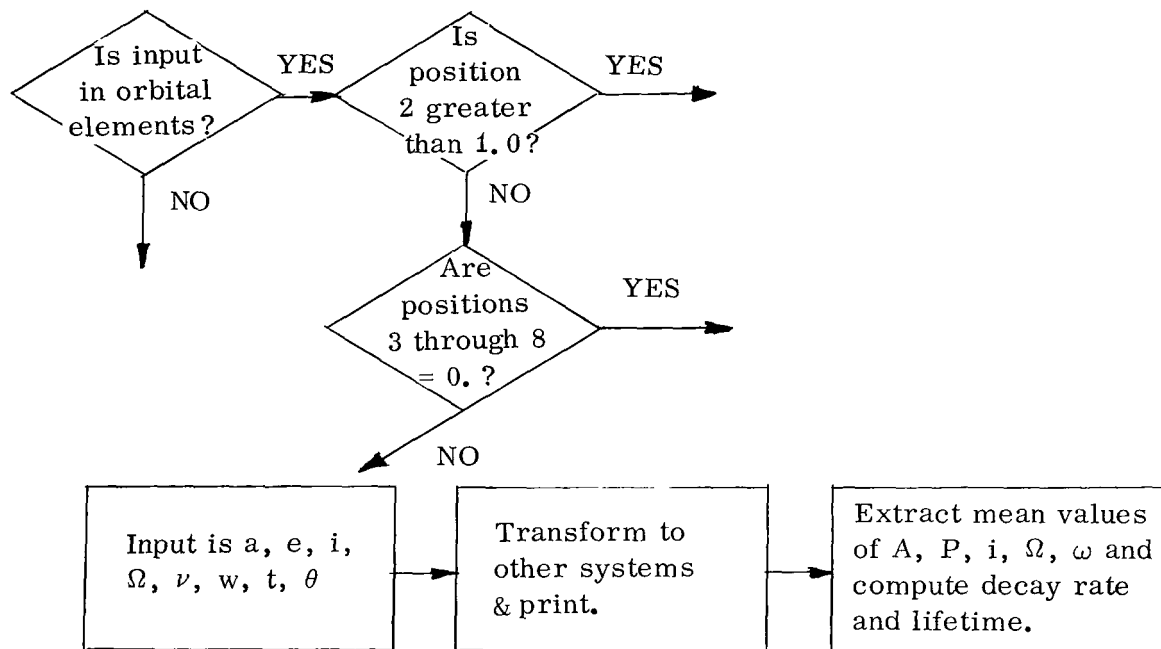
Option D

If position 2 is less than 1.0 and if any of positions 3 through 8 are non-zero then the input is in the form:

OET = semi-major axis) eccentricity) inclination) right ascension of ascending node) true anomaly) argument of perigee) universal time) sidereal time).

These elements are in the format required for transformation not only to mean elements for use in the lifetime phase, but also to the elements in the remaining coordinate systems for display in the printout.

Logical Flow:



2. Transformation Phase. The transformation phase accepts input in any one of the eight aforementioned coordinate systems, performs the required transformations, and outputs in the remaining seven. All programming is done in double precision. The transformation subroutine is a general purpose one used in other computer programs. A detailed description of this phase of the program is not included in this writeup, but may be obtained from the author. A brief description of each coordinate system follows:

a. Earth-Fixed Plumblin (EFP)

XEP, YEP, ZEP, DXEP, DYEP, DZEP

A right-handed Cartesian coordinate system with its origin at a point on the surface of the earth, specified by geodetic coordinates ϕ_0 , and λ_0 . The Z-axis points in the direction of the local geodetic vertical (plumbline). The X-Y plane is tangent to the geodetic ellipsoid with the X-axis pointing along a specified azimuth defined as (KAPPA) (normally the firing direction). This system is completely earth-fixed.

b. Earth-Fixed Ephemeris (EFE)

XE, YE, ZE, DXE, DYE, DZE

A right-handed geocentric Cartesian coordinate system. The Z-axis points north along the axis of rotation of the earth (through the north pole). The X-Y plane is the earth equatorial plane, and the X-axis points through the Greenwich meridian of longitude. The system is completely earth-fixed.

c. Space-Fixed Ephemeris (SFE)

XS, YS, ZS, DXS, DYS, DZS

A right-handed geocentric Cartesian coordinate system. The Z-axis points north along the axis of rotation of the earth (through the north pole). The X-Y plane is the earth equatorial plane, and the X-axis is collinear with and directed toward the vernal equinox of date (i.e., at time t). At time $t = 0$, the Greenwich Hour Angle equals zero.

d. Space-Fixed Geographic (SFG)

$R_s, \psi_s, \lambda_s, V_s, \alpha_s, \epsilon_s$

A right-handed system containing an earth-fixed position vector and a space-fixed velocity vector. The position vector is specified by geocentric earth-fixed spherical coordinates: radius, R_s , geocentric latitude, ψ_s , with respect to the earth

equatorial plane; and geographic longitude, λ_s , measured positive eastward from the Greenwich meridian in the earth equatorial plane. The velocity vector is referenced to a fundamental plane tangent to the sphere of radius R_s , perpendicular to R_s , and with origin at the point of tangency. The velocity vector is specified by space-fixed velocity magnitude, V_s ; elevation angle, ϵ_s , with respect to the fundamental plane; and azimuth α_s , the angle between the projection of the velocity vector in the fundamental plane and the north vector in that plane.

e. Earth-Fixed Geographic (EFG)

$$R_e, \psi_e, \lambda_e, V_e, \alpha_e, \epsilon_e$$

The right-handed (nonrectangular) system with its origin at the center of the earth. The position vector is defined by R_e , ψ_e , and λ_e which are the same as R_s , ψ_s , and λ_s in the space-fixed geographic system. The earth-fixed velocity vector is defined by V_e , the earth-fixed velocity magnitude, α_e the earth-fixed azimuth of the velocity vector, and ϵ_e the earth-fixed elevation of the velocity vector. This system is completely earth-fixed. V_e , α_e , and ϵ_e are defined the same as V_s , α_s , and ϵ_s except they are earth-fixed and not space-fixed.

f. Platform System (PLT)

$$XPL, YPL, ZPL, XDPL, YDPL, ZDPL$$

The platform coordinate system is defined such that it coincides with the earth-fixed plumbline system until the time of first motion of the vehicle. At the instant of first motion, the system becomes space-fixed and is a space-fixed plumbline system with its origin centered at the launch pad at the time of first motion. Gravitational effects on the position and velocity component at the transformation time are accounted for. The system is a right-handed rectangular coordinate system. The Y-axis points in the direction of the local geodetic vertical (plumbline). The X-Y plane is tangent to the geodetic ellipsoid and at the time of first motion, the X-axis

points along a specified azimuth defined as KAPPA (normally the firing direction). The system is then completely space-fixed.

g. Osculating Orbital Elements (\overline{OET}), (\overline{OEM}), (\overline{OEE})

$a, e, i, \Omega, \omega, (\nu, E \text{ or } M)$

The orbital element system is defined by six elements of the two-body ellipse with the reference body being determined by the body constants used, normally those of the earth. The elements are the semi-major axis (a) of the ellipse; the eccentricity (e); the inclination of the orbital plane to the equatorial plane (i); the right ascension of the ascending node (Ω); measured eastward in the equatorial plane from the vernal equinox to the ascending node of the orbit; the argument of perigee or the angle between the ascending node and the perigee (ω); and the angular position of the satellite defined by either true (ν), eccentric (E) or mean (M) anomaly.

h. Mean Orbital Elements (\overline{MOT}), (\overline{MOM}), (\overline{MOE})

$\overline{a}, \overline{e}, \overline{i}, \overline{\Omega}, \overline{\omega} (\overline{\nu}, \overline{M} \text{ or } \overline{E})$

The mean orbital elements are defined as the osculating orbital elements with either or both the long and short periodic variation due to the earth oblateness removed.

Equation defining the short-period variations in orbital elements contain trigonometric functions in argument of latitude or in one of the anomalies; hence, they have periods equal to or less than one orbital period. Expressions for the long-period variations, on the other hand, contain trigonometric functions in argument of perigee and hence have periods much larger than one orbital period. These long-period terms may contain some short-period terms also.

Note that universal time and sidereal time are common to all eight coordinate systems.

3. Lifetime Phase. The initial mean orbital elements $A_0, P_0, i_0, \Omega_0, \omega_0$, are input to the orbit lifetime-decay computation phase from the control phase. At the initial point the instantaneous apogee and perigee rates of change (A_0, P_0)

are evaluated using Simpson's numerical integration technique. Integration steps in true anomaly are taken from 0 to 360° , completing one orbital revolution, and the mean rates of change over the revolution evaluated. The effective drag coefficient, area, and atmospheric density are required input at each integration step. The orbital decay is thus evaluated at successive apogee steps in the following manner. For successive apogee (A) values taken in increments of \dot{A} , the corresponding perigee (P) values are determined, the rates of change \dot{A} and \dot{P} are evaluated and the resulting lifetime calculated using Runge-Kutta integration of \dot{A} and the orbital mass function. More detailed explanations are given in the following subsections.

a. Orbital Parameter Computations

(1) Parameters that are constant at the i^{th} apogee integration step for all ν values.

	<u>Units</u>
$a_i = \frac{1}{2} (A_i + P_i)$	km
$e_i = (A_i - P_i) / (A_i + P_i)$	
$R_{PA_i} = R_E \left[1 - (\sin^2 i_o \sin^2 \omega_i) / F \right]$	km

where i_o is initial inclination.

$n_i = (K/a_i^3)^{\frac{1}{2}} \left[1 + J (R_E/a_i)^2 b_1 (1 - e_i^2)^{-\frac{3}{2}} \right] \left[C \right]$	deg/day
--	---------

where

$$b_1 = 1 - \frac{3}{2} \sin^2 i_o$$

$$C = (24) (3600) (57.2957795)$$

$\dot{\Omega}_i = -J n_i \cos i_o \left\{ R_E / \left[a_i (1 - e_i)^2 \right] \right\}^2$	<u>Units</u> deg/day
$\dot{\omega}_i = \frac{1}{2} J n_i (4 - 5 \sin^2 i_o) \left\{ R_E / \left[a_i (1 - e_i)^2 \right] \right\}^2$	deg/day.

Compute

$$\Delta t_i = (A_i - A_{i-1}) / \dot{A}_{i-1} ; \quad \text{days}$$

then

$$\Omega_i = \Omega_{i-1} + \dot{\Omega}_{i-1} \Delta t_i \quad \text{deg}$$

$$\omega_i = \omega_{i-1} + \dot{\omega}_{i-1} \Delta t_i \quad \text{deg}$$

At initial time,

$$\omega_i = \omega_o ; \quad \Omega_i = \Omega_o .$$

Finally, period and velocity at perigee are computed from

$$PD_i = (2\pi/60) (a_i^3/K)^{\frac{1}{2}} \quad \text{min}$$

$$VP_i = K^{\frac{1}{2}} \left\{ (2/P_i) \left[1 + \frac{1}{3} J (R_E/P_i)^2 (1 - 3 \sin^2 i_o \sin^2 \omega_i) \right] - 1/a_i \right\}^{\frac{1}{2}} \quad \text{km/sec}$$

(2) Parameters that are variable with ν at each apogee integration step. Geocentric radius to the satellite is

$$R_i = \frac{a_i (1 - e_i^2)}{1 + e_i \cos \nu} + \frac{2JR_E^2}{3a_i (1 - e_i^2)} \left\{ \sin^2 i_o \left[1 - \frac{1}{2} \sin^2 (\omega_i + \nu) \right] - \frac{1}{2} \right\} \frac{\text{Units}}{\text{km}} \\ - (0.3R_E H/J) \sin i_o \left[\sin (\omega_i + \nu) - \sin (\omega_o + \nu) \right] . \quad \text{km}$$

Altitude of the satellite is

$$R_i' = R_i - R_E \left[1 - (1/F) \sin^2 i_o \sin^2 (\omega_i + \nu) \right] . \quad \text{km}$$

This value of R' is used in the density $\rho_o(R_i')$ and drag coefficient (C_D') calculations.

b. Ballistic Parameters Computation

(1) Drag Coefficient. The effective drag coefficient is input in two parts. (Note that the nomenclature was arbitrarily selected and may not be consistent with standard aerodynamic terminology.)

- (a) The first part, C_D' , is input as a function of altitude (R_i'). The input is given in table form with up to 20 values of C_D' and the associated altitude. This allows for the variation in C_D with altitude. The table is input with the highest altitude first followed by succeeding altitudes in decreasing order.

A linear interpolation is performed to determine C_D' for a specific value of P . If only one C_D' is input no interpolation is performed and the one value of C_D' is used for all values of P . If P exceeds the first value in the table, the first value of C_D' in the table is used; if it is smaller than the last value in the table, the last value is used.

- (b) The second part, C_N , is input as a function of angle of attack or time. The input is given in table form with up to 20 values of C_N and the associated angles of attack or time. Angle α

varies from 0 to 360° while time starts at smallest value. This allows for variable attitudes of the vehicle during an orbit.

1 If α is input a linear interpolation should be performed to determine C_N for a specific value of α . If only one C_N is input, this value is used for all values of α .

2 If time is input check lifetime t_{i-1} , then:

If $t_{i-1} \geq t_{N-1}$, use C_N at t_N value.

If $t_{i-1} < t_{N-1}$, use C_N at t_{N-1} value.

The times associated with the C_N 's mean that discrete changes in C_N are made at these times.

The value of the coefficient of drag to be used at each integration point around the orbit is then

$$C_D = C_D' C_N .$$

(2) Drag Area

$$A_{oi} = f(\alpha, \text{ or time})$$

The effective drag area is input as a function of angle of attack or time. This then allows for variable attitude during an orbit or at some time in flight but not both. The input is given in table form with up to 20 values of area and the associated angles of attack or time.

If α is input, a linear interpolation is performed to determine A_{oi} at a specific α . If only one A_{oi} is input, this value is used for all values of α .

If time is input, check lifetime t_{i-1} at the previous integration step. Then,

if $t_{i-1} \geq t_{N-1}$, use A at t_N value;

if $t_{i-1} < t_{N-1}$, use A at t_{N-1} value.

The times associated with the A's mean that discrete changes are made in A at these time points.

(3) Special $C_D A_{oi}$ Provision

A special provision is made to compute $C_D A_{oi}$ for use in the \dot{A} ' and \dot{P} ' equations if called for by the flag. This allows for a variation in attitude during an orbit with only a specification of the number of revolutions made.

$$CDA = (\text{Sine}(N_1, t_1, \dots, N_N, t_N) \text{ End($$

where N is the number of cycles/orbit made by the orbiting vehicle input as a function of time t. A check is made of the lifetime t_{i-1} :

If $t_{i-1} \geq t_{N-1}$, use N at t_N value.

If $t_{i-1} < t_{N-1}$, use N at t_{N-1} value.

The following equation is then used to compute CDA:

$$CDA = CD_1 A_{01} + (CD_2 A_{02} - CD_1 A_{01}) |\sin(N\nu + \alpha_o)|,$$

where

$$CD_1 = C_D' CN_1, CD_2 = C_D' CN_2 \dots$$

CN_1 , A_{01} , CN_2 , A_{02} and C_D' values are determined from the table functions, and α_o is taken from the angle of attack table (described below) for a true anomaly, ν , equal to zero.

(4) Angle of Attack, α

The angle of attack is input as a function of true anomaly. The input is given in table form with up to 20 values of α and the associated values of ν . If only one value of α is given, then this value should be used for all ν 's.

(5) Mass Functions

$$M(t) = f(\dot{M}, t) \text{ or } f(t) \text{ or a constant}$$

The mass function $M(t)$ will be handled in three ways:

- (a) Input M_0 and up to 20 values each of M_N and M_{fN} in table form. Then the following calculations are made:

$$M(t_i) = M_0 - \dot{M}_{N-1} t_{i-1}.$$

A check on mass at the previous time point is made:

If $M(t) > M_{fN-1}$, continue use of \dot{M}_{N-1} .

If $M(t) < M_{fN-1}$, change to use of \dot{M}_N .

This should be continued in table until $M(t) < M_{fN}$; then use $M(t) = M_{fN}$.

- (b) Input up to 20 values of mass as a function of time in table form. Then, the following check is made on lifetime at the previous integration step:

If $t_{i-1} \geq t_{N-1}$, use M at t_N value.

If $t_{i-1} < t_{N-1}$, use M at t_{N-1} value.

This table allows for discrete changes to be made in M at specified time point.

- (c) If mass is desired as a constant throughout the total lifetime, just the initial mass M_0 is loaded.

C. Atmospheric Density Options. The provision is made to call for the use of any one of six atmospheric density models by flag. These models are 1959 ARDC, 1962 U. S. Standard, Poe, Small, Special 1959 ARDC, and Special 1962 U. S. Standard. For altitudes greater than 700 km, density is set equal to 0.

(1) 1959 ARDC and 1962 U. S. Standard Atmospheric Models. These two atmospheric density models are in subroutine form and are on the system library tape at the Computation Laboratory at Marshall Space Flight Center.

These two models differ from the standard 1959 ARDC and 1962 U. S. Standard in that they are referenced to the Patrick Air Force Base altitude rather than a mean sea level altitude.

To use this lifetime program at an installation that does not have a system library tape that originated at MSFC, either the subroutine cards must be obtained or one of the models described in the following section must be used.

(2) Poe and Small Atmospheric Models. The Poe and Small atmospheric density models (References 2 and 7) are time and position dependent since the effects of atmospheric heating are included. A subroutine for each of these models is included as a part of the Lifetime program and can be used directly.

(3) Special 1959 ARDC and Special 1962 U. S. Standard Atmospheric Models. These two models were previously discussed in detail in Section II. The models as programmed are respecified in this section. These two models are the same as (1) with the exception that atmospheric heating and diurnal bulge can be included on option. There are two options for specifying the effect of the diurnal bulge. One method is to compute the angle (ψ') between the satellite and the center of bulge as follows:

$$\cos \psi' = \ell \ell_B + m m_B + n n_B .$$

To evaluate the two sets of direction cosines, the following formulas are required:

$$\ell = \cos \Omega \cos (\omega + \nu) - \sin \Omega \cos i \sin (\omega + \nu)$$

$$m = \sin \Omega \cos (\omega + \nu) + \cos \Omega \cos i \sin (\omega + \nu)$$

$$n = \sin i \sin (\omega + \nu)$$

$$\ell_B = \sqrt{n_s^2 + \ell_s^2} \cos (RA_B)$$

$$m_B = \sqrt{n_s^2 + \ell_s^2} \sin (RA_B)$$

$$n_B = n_s ,$$

where

$$\ell_s = \cos \lambda_s ; m_s = \sin \lambda_s \cos \epsilon ; n_s = \sin \lambda_s \sin \epsilon$$

$$RA_B = [\tan^{-1} (m_s / \ell_s)] - \theta_\rho$$

$$\lambda_s = .017203 d + .0335 \sin (.017203 d) - 1.41$$

$$\theta_\rho = (\pi/180) [18.5 + 30 \exp (K_1) + K_2 \sigma + 4(1 - \sigma^2)] ; \quad \theta_\rho < 5$$

$$\theta_\rho = 5 ; \quad \theta_\rho \geq 5$$

and

$$K_1 = -.00567 (R_i' - 200) + \exp [-.01455 (R_i' - 200)]$$

$$K_2 = 18.5 + 21.5 \exp [-.0315 (R_i' - 200)]$$

$$\sigma = (S - 160)/90 .$$

The second method for specifying the effect of the diurnal bulge is to set $\psi' = 75^\circ$ which is simply a mean diurnal bulge.

The angle ψ' is then used in the equation

$$K_\rho = \left[3 + 2.5 \left(\frac{R_i' - 360}{240} \right) - 0.5 \left(\frac{R_i' - 360}{240} \right)^2 \right] \left[\frac{5.6 - \cos \psi'}{6.6} \right] .$$

Finally, density is computed from

$$\rho = \rho_o (R_i') D_c \left(\frac{s}{s_o} \right)^{K_p} \left\{ \frac{1 + .19 [\exp (.0055 R_i' - 1.9)] [\cos \frac{\psi'}{2}]^6}{1 + .19 [\exp (.0055 R_i' - 1.9)] [\cos 37.5^\circ]^6} \right\},$$

in which $\rho_o (R_i')$ is either the 1959 ARDC or the 1962 U. S. Standard reference density called for, and D_c is an altitude-dependent density correction factor. If $R_i' \leq 120$ km,

$$\rho = \rho_o (R_i') D_c .$$

However, when $120 \text{ km} < R_i' < 700 \text{ km}$, compute

$$S = \bar{S} \exp [g(t)]$$

$$\bar{S} = 25 + 0.8 \overline{F_{10.7}} + 0.4 (F_{10.7} - \overline{F_{10.7}}) + 10K_p$$

$$g(t) = .025 \cos \left[2\pi \left(\frac{d - 1843}{365.25} \right) \right] - .06 \cos \left[4\pi \left(\frac{d - 1843}{365.25} \right) \right] .$$

The yearly mean solar flux, $\overline{F_{10.7}}$, may be input in table form as a function of date (decimal year) and a linear interpolation for the current value of $\overline{F_{10.7}}$ performed. If no values of $\overline{F_{10.7}}$ are input, then $\overline{F_{10.7}}$ is computed as follows:

$$\overline{F_{10.7}} = 135 + 75 \cos \left[2\pi \left(\frac{d - 136}{4090} \right) \right] + 15 \cos \left[4\pi \left(\frac{d + 174}{4090} \right) \right] .$$

$F_{10.7}$ may also be input in table form. If no value of $F_{10.7}$ is input then $F_{10.7}$ is set equal to $\overline{F_{10.7}}$. K_p is input in table form as a function of date (decimal year) and a linear interpolation performed to obtain the current value of K_p .

Many of the foregoing parameters and their definitions were adopted from Reference 2.

d. Apogee and Perigee Decay Rates at the i^{th} Apogee Integration Step. At each i^{th} integration step the time rates of change of apogee and perigee

radius (which are functions of ν) are averaged over 2π on ν . The resultant definite integrals are evaluated by Simpson's rule using fixed increments of ν . The procedure follows: *

$$\dot{A}_i' = \frac{-86.4 \times 10^6}{2\pi} \sqrt{\frac{a(1+e)}{K(1-e)^3}} \int_0^{2\pi} C1(1 + \cos \nu) d\nu \quad \text{kg-km/day}$$

$$\dot{P}_i' = \frac{-86.4 \times 10^6}{2\pi} \sqrt{\frac{a(1-e)}{K(1+e)^3}} \int_0^{2\pi} C1(1 - \cos \nu) d\nu \quad \text{kg-km/day}$$

$$C1 = (C_{D_i})(A_{oi})(\rho_i)(1 + 2e_i \cos \nu + e_i^2)^{\frac{1}{2}},$$

then

$$\dot{A}_i = \dot{A}_i' / M(t)$$

$$\dot{P}_i = \dot{P}_i' / M(t) ,$$

where $M(t)$ is taken from calculations in Section III. B. 3. b. (5).

For printout only, the time rate of change of semi-major axis is computed from

$$\dot{a}_i = \frac{1}{2} (\dot{A}_i + \dot{P}_i) .$$

Finally, for use by the Runge-Kutta integration routine, the rates of change of time and perigee with respect to apogee are computed.

* The derivations of \dot{A}_i' and \dot{P}_i' are given in Section V.

$$\frac{d t_i}{d A_i} = M(t) / \dot{A}_i,$$

$$\frac{d P_i}{d A_i} = P_i' / \dot{A}_i, \quad .$$

e. Integration of Time and Perigee with Respect to Apogee. The integration scheme used to numerically determine the change in time and perigee with respect to apogee is Runge-Kutte (Reference 4).

The Fortran source listing of the Runge-Kutta routine is given in Section VI, Statements 3 to 13. However, a brief explanation of the flow of the computations performed by Runge-Kutta follows.

At the starting point for any lifetime computation, initial values of A, P, i, Ω , ω are known. Using these initial values, the initial rates of change of time and perigee with respect to apogee are computed via the equations in Sections III-3-a through III-3-d. With the information now available (A, P, dt/dA, dP/dA), the Runge-Kutta scheme is used to take a step (δA) in apogee and to arrive eventually at a solution for perigee and time at the end of this step. For the next step initial values of A, P, i, Ω , ω are available from the previous step and the whole sequence of computation is repeated as in step one. One of the main points to understand is that the Runge-Kutta scheme, for any one apogee step, is keyed to obtaining a very good value of dt/dA and dP/dA at the midpoint of the particular apogee step. Once this is obtained, values of perigee radius and time at the end of the step are evaluated immediately. Remember that δA is an exact quantity input to the program while δP and δt must be calculated. The operations performed by Runge-Kutta are as follows.

For convenience of notation let:

(1) P_i = known perigee at beginning of step.

A_i = known apogee at beginning of step.

T_i = known time at beginning of step.

δA = known step size in apogee to be taken.

$$PD = dP/dA$$

$$TD = dt/dA \quad ,$$

then

$$CP_1 = \frac{\delta A}{2} PD$$

$$P_i = CP_1 + P_1$$

$$A_i = A_1 + \delta A/2$$

$$CT_1 = \frac{\delta A}{2} TD$$

$$t_i = T_1 + CT_1$$

Compute new PD & TD using aforementioned equations in Sections III-3-a through III-3-d.

$$CP_2 = \frac{\delta A}{2} PD$$

$$P_i = CP_2 + P_1$$

$$CT_2 = \frac{\delta A}{2} TD$$

$$t_i = T_1 + CT_2$$

Compute new PD & TD as above.

$$CP_3 = \frac{\delta A}{2} PD$$

$$P_i = 2 CP_3 + P_1$$

$$A_i = A_1 + \delta A$$

$$CT_3 = \frac{\delta A}{2} TD$$

$$t_i = T_1 + 2 CT_3$$

Compute new PD & TD as above.

$$\Delta = \frac{\delta A}{2} PD + 2 CP_3 + 2 CP_2 + CP_1 / 3$$

$$P_i = \Delta + P_1$$

$$\Delta_i = \frac{\delta A}{2} TD + 2 CT_3 + 2 CT_2 + CP_1 / 3$$

$$t_i = \Delta_i + T_1$$

(2) P_i and t_i are now good at $A_i + A$

Using the latest values of P_i , A_i , t_i , PD, and TD, the above process from (1) to (2) is repeated until some cutoff criterion is met, namely, apogee, perigee or earth impact.

The lifetime t_i is converted at each apogee step to revolutions, t_{Ni} , for printing only.

$$t_{Ni} = t_{Ni-1} + \frac{(t_i - t_{i-1}) 1440}{PD_i}$$

f. Altitude Interpolations. Although the values of apogee and perigee radius are computed and printed at the end of every apogee step, the user might like to know what these values are at intermediate points.

An option is available which allows the interpolation for the the printout of a maximum of five intermediate apogees and five intermediate perigees, or a total of ten extra points if the user so desires.

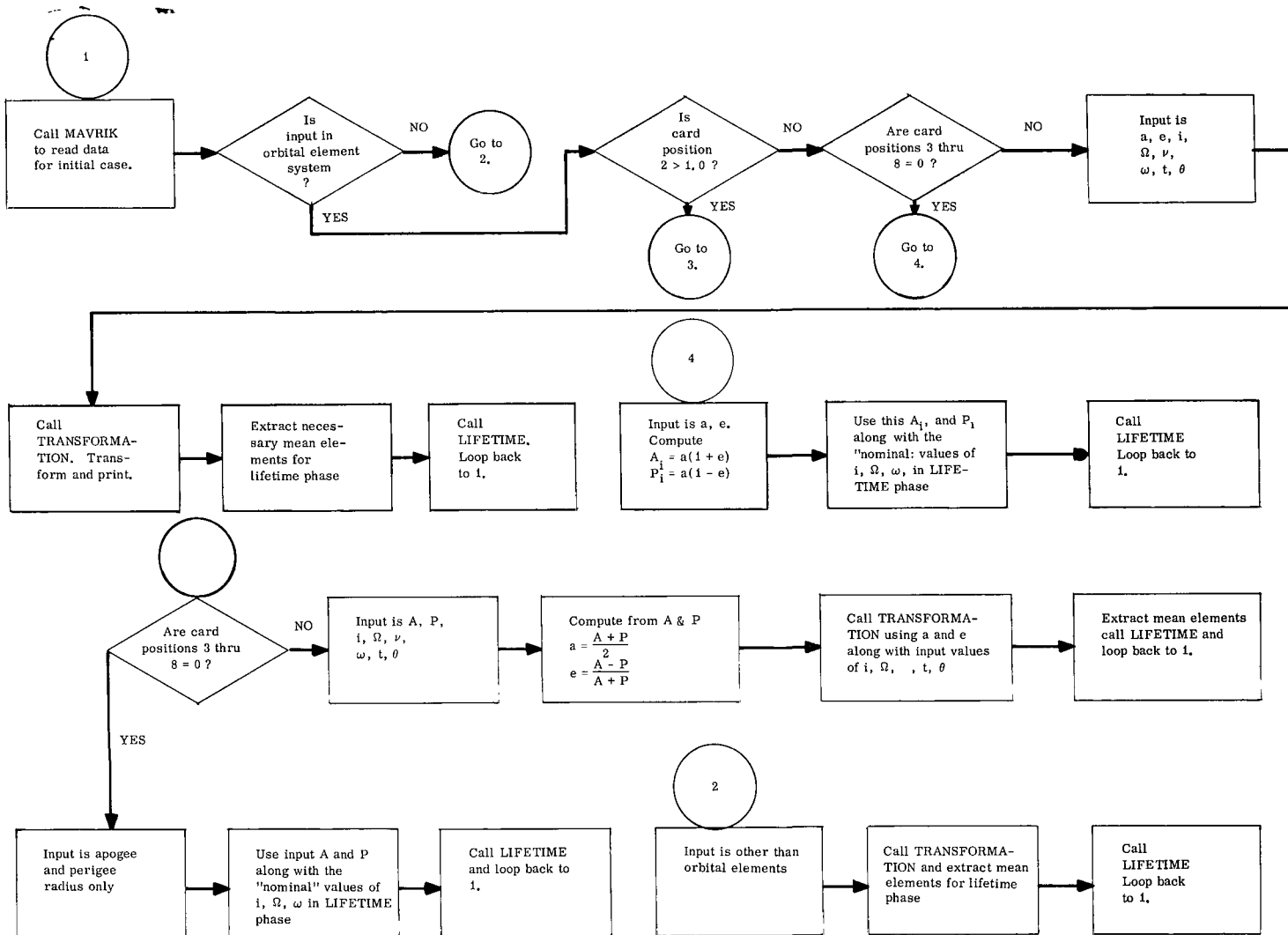
The equations used for interpolation are

$$A_{N_j} = A_{i-1} + \frac{(T_{A_j} - t_{i-1})(A_i - A_{i-1})}{(t_i - t_{i-1})}$$

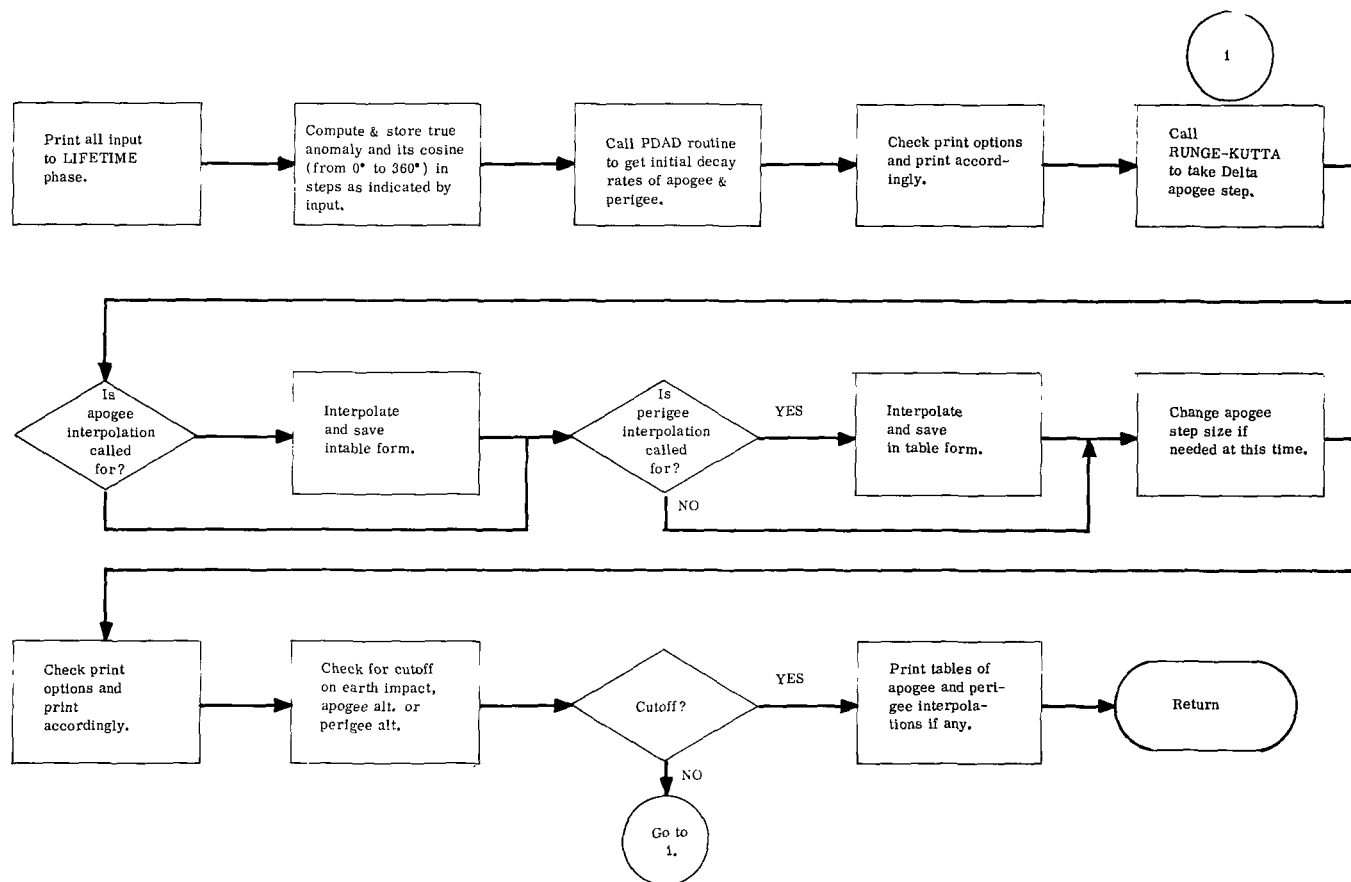
$$P_{N_k} = P_{i-1} + \frac{(T_{P_k} - t_{i-1})(P_i - P_{i-1})}{(t_i - t_{i-1})} ,$$

where A_{N_j} and P_{N_k} are the interpolated radii of the apogee and perigee and T_{A_j} and T_{P_k} are the times at which the interpolations are performed.

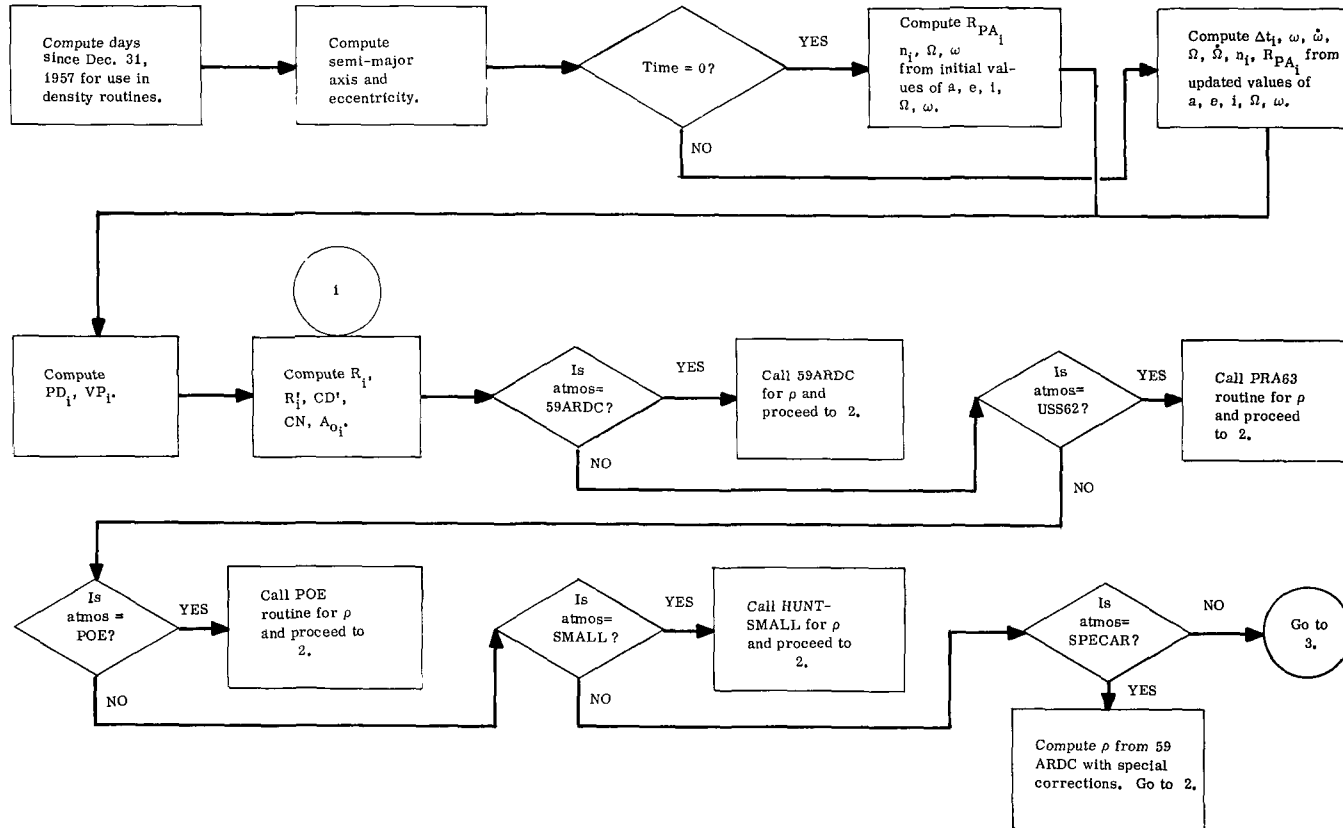
4. Computer Program Flow Charts



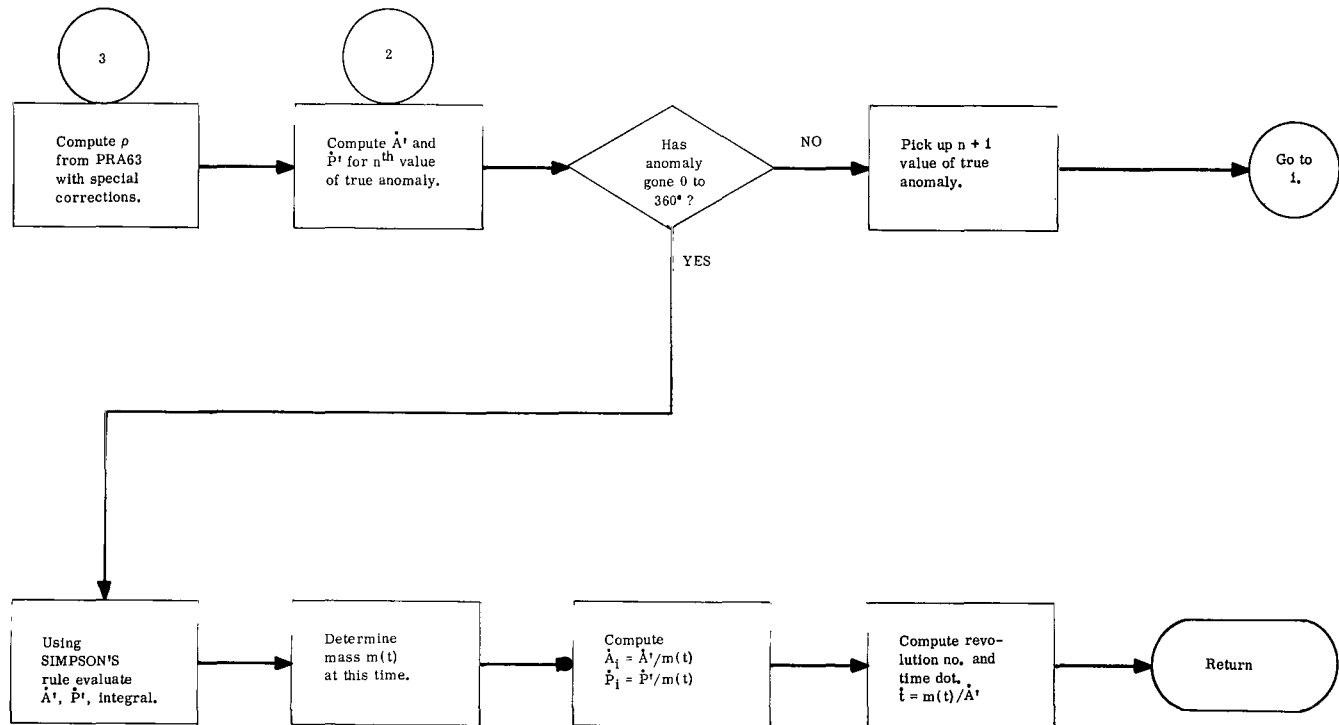
Block Flow of Control Phase



Block Flow of "Life" Routine



Block Flow of "PDAD" Routine



Block Flow of "PDAD" Routine (Cont'd)

1. Description of Input Routine (MAVRIK) Used By The Orbit Decay and Orbital Lifetime Program

The MAVRIK input routine is unique to the Computation Laboratory at MSFC. This routine allows flexibility of input and is therefore well suited for engineering work.

Single precision floating point numbers containing up to 10 digits (sign, decimal, and exponent excluded) may be input. Such numbers always contain a decimal point, are terminated by a comma, and may be input in one of several forms. For example, the number 6378.168 may be input as follows:

6378.165,	6.378165E+03,	6.378165+03,
6.378165+3,	6378165.E-3,	637816.5-2,

Integers may also contain up to 10 digits (sign excluded). Integers contain no decimal points and are terminated by commas as follows: 6378, 100, 71658,.

Double precision numbers may contain up to 16 digits (sign, decimal, and exponent excluded). These numbers always contain a decimal point, are terminated by a right hand parenthesis, and may be input in one of several forms. For example, the number 6378.165987654321 may be input as:

6378.165987654321)	.6378165987654321D+04)
637.8165987654321D+1)	637816.5987654321D-2)

Alphanumeric information, as used in this program, may contain up to 6 characters. Each piece of information is enclosed by left hand parenthesis and is left-adjusted in machine storage. Examples of alphanumeric input follows:

ON CARD	IN STORAGE
(ALPHA(ALPHAb
(MASS(MASSbb
(bMASS(bMASSb

All input is loaded by code name followed by an equality sign. For example: MASS = 74812., ATMOS = (ARDC(. A complete listing of all input codes is given in the following tables.

2. Description of Parameters That May Be Input to The Lifetime Phase

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
	***** BALLISTIC PARAMETERS *****			
AREA=***(++., ++, ++. ++, ... (END(A_o	m^2	(ALPHA (1., 360., (END(Table of effective drag area values as a function of either angle of attack or time. *** specifies whether area is a function of (ALPHA(or (TIME(. The first value after *** is the dependent variable, AREA, followed the independent variable; either ALPHA in degrees or TIME in hours. The table may contain up to 20 values of area (with the corresponding 20 values of independent variable).
ATTACK=++., ++, ++. ++, ... (END(α	deg	1., 360., (END(Table of angle of attack as a function of true anomaly. First table value is the dependent variable, α , followed by the independent variable, true anomaly, in degrees. Table may contain up to 20 values of α (with the corresponding 20 values of true anomaly).

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
CDPRIM=++. ++, ++. ++, ... (END(CD'	non-dimensional	1., 0., (END(Table of drag coefficients as a function of perigee altitude. First value is dependent variable, CD, followed by independent variable, perigee altitude, in kilometers. Table may contain up to 20 values of CD with corresponding values of perigee altitude.
CDA=***(++. ++, ++. ++, ... (END(N	cycles/orbit		When this table is input the quantity CDA is computed as some function of AREA, ATTACK, COPRIM, and N. ***indicates the sine function (SINE(. Other functions could be added at a later time. The first number in the table is N, the number of cycles/orbit made by the orbiting body. The second number in the table is time in hours at which the next value of N should be used. Table may contain up to 20 values of N with the corresponding times.

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
MASS=***(+++. ++, ++. ++, ... (END(m(t)	see definition	(CON(1.,	<p>Orbiting mass function. There are three methods for specifying mass.</p> <p><u>Method one.</u> ***specifies (RATE(, the first value in the table is an initial mass (M_0) in kilograms, the second value is a mass decay rate (\dot{m}) in kilograms/day, and the third value is a final mass (M_f) in kilograms. If the mass decays to (M_f) then the next decay rate in the table is used along with a new M_f. If an (END(is found in the table the last M_f is used as a constant mass until the run is completed. Table may contain up to 20 values of \dot{m} and corresponding M_f.</p> <p><u>Method two.</u> *** specifies (TIME(, the first value in the table is an initial mass (M) in kilograms, and the second value in the table is a time (t) in hours to change to a succeeding mass (m). If an (END(is found in the table the last M is used as a constant mass until the run is completed. Table may contain up to 20 values of M and corresponding times.</p>

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
MASS (cont.)				<p><u>Method three.</u> ***specifies (CON(, the first and only value in the table is the mass in kilograms to be used throughout the entire run. For this option no (END(is needed in the table.</p>
CN=***(++., ++, ++. ++, ..., (END(C_N	non-dimensional	(ALPHA(1., 360., (END(<p>Table of normal force coefficients as a function of either angle of attack or time. ***specifies whether cn is a function of (ALPHA(or (TIME(. The first value in the table is the dependent variable, C_N followed by the independent variable, either α in degrees or time in hours. The table may contain up to 20 values of C_N with the corresponding independent variable.</p>

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
***** DENSITY PARAMETERS *****				
DATE=++. ++, ++.++, ++. ++,		month, day year		Calendar date to be used in density calculation when special density is desired.
ATMOS=(***(ρ	kg/m ³	(ARDC(Flag indicating atmosphere to be used. Options available are: (ARDC(1959 ARDC Atmosphere. USSTD(1962 US Standard Atmosphere. (POE(L MSC Atmosphere Routine (SMALL(L MSC Atmosphere Routine (SPECAR(Modified 1959 ARDC Atmosphere (SPECUS(Modified 1962 US Standard Atmosphere
CORREC=++. ++, ++. ++,... (END(DC	non-dimensional	1., 0., (END(Table of density correction factors DC as a function of perigee altitude in km. First value in table is DC, second value is perigee altitude. Table may contain up to 50 values of DC and corresponding altitude.

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
DIURNL=***(..... (END(ψ'	deg	(MEAN(..... (END(Flag indicating diurnal (bulge) effect desired in special density calculations. ***=(MEAN(indicates a mean diurnal effect where lag angle, ψ' , is set equal to 75°. This effect corresponds to 9:00 a.m. local time for a lag angle of 30°. ***=(NORMAL(indicates computation of diurnal effect as given by special density equations.
ECLIPT=++. ++, (END(deg	23.4436 (END(Obliquity of the ecliptic. Used in computing ψ' .
KP=++. ++, ++. ++, (END(KP	k _p	2.5, 2000., (END(Table of monthly mean values of geomagnetic index. Table is input as a function of decimal year. Up to 50 KP's and corresponding years may be loaded.

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
KP (cont.)				Note: In the literature K_p is listed as O_0 , $O+$, $1-$, 1_0+ , ..., $9-$, 9_0 ; however loaded values are specified as a decimal number, e.g. 8.7.
FTEN=++. ++, ++. ++, ... (END($F_{10.7}$	10^{-22} watts/ m ² /cycle/ sec	0.	Table of monthly mean values of $F_{10.7}$. These values will be available only for post flight predictions. The values are loaded in the order $F_{10.7}$ decimal year, F_{10} decimal year etc. Up to 50 values of $F_{10.7}$ and corresponding years may be loaded.
FTENB=++. ++, ++. ++, (END($\overline{F}_{10.7}$	10^{-22} watts/ m ² /cycle/ sec	SEE BELOW	Table of yearly mean values of $F_{10.7}$. These values are loaded in the order $\overline{F}_{10.7}$ decimal year, $\overline{F}_{10.7}$ decimal year, etc. Up to 50 values of $\overline{F}_{10.7}$ and corresponding years may be loaded. The assembled, nominal table is given below.
<p>Nominal Value of $\overline{F}_{10.7}$</p> <p>243.6, 1958., 230.7, 1958.5, 226.5, 1959., 208.9, 1959.5, 180.5, 1960., 161., 1960.5, 130.8, 1961., 104.8, 1961.5, 99.3, 1962., 89.7, 1962.5, 382.7, 1963., 80.8, 1963.5, 77.9, 1964., 70., 1964.5, 75., 1965., 80., 1965.5, 131., 1966.5, 186., 1967.5, 200., 1968.5, 190., 1969.5, 163., 1970.5, 142., 1971., 128., 1971.5, 108., 1972.5, 94., 1973.5, 81., 1974.5, 75., 1975., 75., 1975.5, (END(</p>				

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
SO=++, ++,	S _o	non-dimensional	220.0	Reference value of total heating used in the computation of special 59 ARDC and 62STD densities. Normally the 100. value will be used but if a D _c curve derived for some other heating value is loaded then SO must be changed to that total heating value.
SA=++, ++,	ss	non-dimensional	0.	Reference value of total heating used in LMSC Hunt Small density computation. If no SA is loaded, program automatically computes this value.
***** SPECIAL INPUT *****				
PRINT=(***((NORMAL(Flag denoting type of output desired. (NORMAL(, (SHORT(, (DETAIL(are the options available. Complete description of each option is given in the output section of this report.

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
INTERA=++.++, ++.++,	A_{N_j}	days		Table of up to 5 times for which an interpolation for apogee will be performed. Apogee values stored in table form to be output at end of run.
INTERP=++.++, ++.++,	P_{N_K}	days		Table of up to 5 times for which an interpolation for perigee will be performed. Perigee values stored in table form to be output at end of run.
CUTOFF=***(++.,++)		km from earth center	(I(6378.166,	Flag denoting method of terminating run. *** indicates which parameter cutoff will be made on. Three options are available: (A) apogee radius, (P) perigee radius, (I) earth impact. ++.++ is the radius at which cutoff is desired.
DANOM=++.++,	δv	deg.	10.0	Integration step size in true anomaly to be used in Simpson's rule integration around orbit. Must be a multiple of 360.

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
DAPOGE=++, ++, ++, ++,	δA	km	See table at right.	Integration step size in apogee used in RUNGE-KUTTA integration. The step size is a function of apogee radius and is loaded in the form of δA , A (km), δA , A (km), etc. Up to 5 step sizes and the corresponding apogee radius may be loaded. The nominal, assembled table is: -5., 6778., -10., 6578., -20., 0.,
	***** CONSTANTS *****			
F=++, ++,	f	non-dimensional	298.3	Reciprocal of the flattening of the earth.

Description of Parameters That May Be Input to The Transformation Phase.

Input Code	Equation Symbol	Unit & Direction	Nominal Value	Definition
The following constants, KERTH through DD, are input to the Transformation phase in double precision and are carried to the Lifetime phase in single precision. These constants are common to both phases.				
KERTH=++. ++)	K	km ³ /sec ²	398603.2	Earth gravitation constant.
AE=++. ++)	R _e	km	6378.165	Mean equatorial radius of the earth.
AO=++. ++)	AO	km	6378.165	Semi-major axis of Fischer ellipsoid
BO=++. ++)	BO	km	6356.784	Semi-minor axis of Fischer ellipsoid
OMEGA=++. ++)	ω _e	deg/hr	15.04106705	Rotational velocity of the earth.
JJ=++. ++)	J	non-dimensional	.162345D-2	Coefficient of the 2nd zonal harmonic of the earth's gravitational potential.
HH=++. ++)	H	"	.575D-5	Coefficient of the 3rd zonal harmonic of the earth's gravitational potential.
DD=++. ++)	D	"	.7875D-5	Coefficient of the 4th zonal harmonic of the earth's gravitational potential.
PHIO=++. ++)	Φ	deg.n	28.5	Geodetic latitude of launch pad.
LAMDO=++. ++)	λ	deg.w	80.5	Longitude of launch pad.

Input Code	Equation Symbol	Unit & Direction	Nominal Values	Definition
KAPPA=++. ++)	α_F	deg. e of n	105.	Launch Azimuth
XG=++. ++)	XG	km	0.	X-component of position due to gravitational acceleration at transformation time.
YG=++. ++)	YG	km	0.	Y-component of position due to gravitational acceleration at transformation time.
ZG=++. ++)	ZG	km	0.	Z-component of position due to gravitational acceleration at transformation time.
XDG=++. ++)	XDG	km/sec	0.	X-component of velocity due to gravitational acceleration at transformation time.
YDG=++. ++)	YDG	km/sec	0.	Y-component of velocity due to gravitational acceleration at transformation time.
ZDG=++. ++)	ZDG	km/sec	0.	Z-component of velocity due to gravitational acceleration at transformation time.
TFM=++. ++)	t_{fm}	hrs	0.	Universal time of first motion.

Coordinate Systems That May Be Input to the Transformation Phase

Input Code	Order of Input	Unit & Direction	Definition
EFE=++ . ++) ++ . ++))	XE	km	Earth-fixed ephemeris system in order: position vector, velocity vector, universal time, sidereal time.
	YE	km	
	ZE	km	
	$\dot{X}E$	km/sec	
	$\dot{Y}E$	km/sec	
	$\dot{Z}E$	km/sec	
	t	hours	
EFP=++ . ++) ++ . ++))	θ	deg	
	XEP	km	Earth-fixed plumblane system in order: position vector, velocity vector, universal time, sidereal time.
	YEP	km	
	ZEP	km	
	$\dot{X}EP$	km/sec	
	$\dot{Y}EP$	km/sec	
	$\dot{Z}EP$	km/sec	
	t	hours	
SFE=++ . ++) ++ . ++))	θ	deg	
	XS	km	Space-fixed ephemeris system in order: position vector, velocity vector, universal time, sidereal time.
	YS	km	
	ZS	km	
	$\dot{X}S$	km/sec	
	$\dot{Y}S$	km/sec	
	$\dot{Z}S$	km/sec	
	t	hours	
SFG=++ . ++) ++ . ++))	θ	deg	
	Rs	km	Space-fixed geographic system in order: range, geocentric latitude, longitude, velocity, azimuth, geocentric elevation.
	ψ_s	deg	
	λ_s	deg	
	Vs	km/sec	
	α_s	deg	
	ϵ_s	deg	
	t	hours	
	θ	deg	

Input Code	Order of Input	Unit & Direction	Definition
EFG=++. ++)+++. ++). . . .)	Re ψ_e λ_e Ve α_e ϵ_e t θ	km deg deg km/sec deg deg hours deg	Earth-fixed geographic system in order: range, geocentric latitude, longitude, velocity, azimuth, geocentric elevation.
OET=++. ++)+++. ++). . . .)	A	km	Osculating orbital element system in order: semi-major axis, eccentricity, inclination, ascending node, anomaly, argument of perigee, universal time, sidereal time. Anomaly may be input in any of three ways: True (OET), Mean (OEM), Eccentric (OEE).
OEM=++. ++)+++. ++). . . .)	E	non-dimensional	
	I	deg	
	Ω	deg	
OEE=++. ++)+++. ++0. . . .)	V, M, E	deg	
	ω	deg	
	t	hours	Mean orbital element system in order: semi-major axis, eccentricity, inclination, ascending node, anomaly, argument of perigee, universal time, sidereal time. Anomaly may be input in any of three ways: True (MOT), Mean (MOM), Eccentric (MOE).
	θ	deg	
MOT=++. ++)+++. ++). . . .)	A	km	
	E	non-dimensional	
MOM=++. ++)+++. ++). . . .)	I	deg	
	Ω	deg	
MOE=++. ++)+++. ++). . . .)	V, M, E	deg	Platform coordinate system in order: position vector, velocity vector, universal time, sidereal time.
	ω	deg	
	t	hours	
	θ	deg	
PLT=++. ++)+++. ++). . . .)	Xpl	km	
	Ypl	km	
	Zpl	km	
	\dot{X}_{pl}	km/sec	
	\dot{Y}_{pl}	km/sec	
	\dot{Z}_{pl}	km/sec	
	t	hours	
	θ	deg	

Description of IOMET Flag Controlling Addition or Subtraction of Long and Short Periodic Terms in
Orbital Element Transformations

INPUT CODE	IOMET=(***(***(
NOMINAL VALUE	IOMET=(SHORT((NOLONG(

If input is given in any system other than mean orbital elements, then the following conditions apply.

IOMET = (SHORT((NOLONG(Short-period terms are subtracted.
IOMET = (NOSHRT((LONG(Long-period terms are subtracted.
IOMET = (NOSHRT((NOLONG(No terms are subtracted.
IOMET = (SHORT((LONG(Both short and long-period terms are subtracted.

If input is in mean elements the above conditions apply with the exception that the periodic terms are added instead of subtracted.

D. Computer Program Output Options

There are three formats for output available in the Lifetime program. They are: short, normal, and detail. The following input cards to "MAVRIK" produced a sample of each of the three types of output.

```
CN      = (ALPHA(2. , 360. , (END(
DATE    = 4. , 8. , 1964. ,
AREA    = (ALPHA(26.04, 360. , (END(
MASS    = (CON(6040. ,
MOT     = 6618.567) .01211) 32.68) 81.4) 101.809) 60.407)
ATMOS   = (ARDC(
PRINT   = (SHORT(/
PRINT   = (DETAIL(/
PRINT   = (NORMAL(/
```

1. Short Output. (See computer output on following page.)

EARTH ORBIT TRANSFORMATION

PHI0 =	0.2850000000000000 02	DEG	LAP00 =	0.8050000000000000 02	DEG	AZFIR =	0.1050000000000000 03	DEG
A =	0.6378165000000000 04	KM	B =	0.6356783999999999 04	KM	OMEGA =	0.1504106705000000 02	DEG/HR
RADIUS =	0.6378165000000000 04	KM	KERTH =	0.3986032000000000 06	KM3/SLC2	J =	0.1623450000000000 02	
H =	0.5750000000000000 05		D =	0.7875000000000000 05		XG =	0.	KM
YG =	0.	KM	ZG =	0.	KM	XOG =	0.	KM/SEC
YDG =	0.	KM/SEC	ZDG =	0.	KM/SEC	TFM =	0.	HOURS

INPUT IN M0T SYSTEM SH0RT N0LONG

POSITION (KM) VELOCITY (KM/SEC) ANGLES (DEG)

EF0

XE =	-0.3037077883473387D 04	YE =	-0.1046142628496821D 04	ZE =	0.2505989924336480D 04
XDE =	0.5957246065928864D 01	YDE =	0.1620505487157563D 01	ZDE =	0.3982714918979543D 01

PLT

XPL =	-0.3037077883473385D 04	YPL =	-0.1046142628496822D 04	ZPL =	0.2505989924336479D 04
XDPL =	0.5979686903636678D 01	YDPL =	0.1850067816184628D 01	ZDPL =	0.4105741525364290D 01

EFE

XEP =	-0.2630237597954840D 04	YEP =	-0.5986299572715291D 04	ZEP =	0.1089689476602931D 04
XDEP =	0.5318120342908635D 01	YDEP =	-0.3161077262043163D 01	ZDEP =	-0.3962580881258863D 01

SFE

XS =	-0.2630237597954840D 04	YS =	-0.5986299572715291D 04	ZS =	0.1089689476602931D 04
XDS =	0.5754648197067024D 01	YDS =	-0.3352877214687555D 01	ZDS =	-0.3962580881258863D 01
TIME =	-0.	THETA =	-0.		

SFG

R =	0.6628827615152297D 04	GCLAT =	0.9461594291796026D 01	L0NG =	0.2462804560176325D 03
VS =	0.7749826367686954D 01	AZVS =	0.1213593542378151D 03	ELVS =	0.6884420409938637D 00

EFG

R =	0.6628827615152297D 04	GCLAT =	0.9461594291796026D 01	L0NG =	0.2462804560176325D 03
VE =	0.7346894628261875D 01	AZVE =	0.1232949670245073D 03	ELVE =	0.7262007992049315D 00

00E

AXIS =	0.6620903169689641D 04	ECCEN =	0.1207474821557146D 01	INC =	0.3261583446622047D 02
ASN0D =	0.8137605735536910D 02	ARGP =	0.658662223696307D 02	TAN0M =	0.9637668968299269D 02
EAN0M =	0.9568865963933066D 02	MAN0M =	0.950002346568445D 02		

M0E

AXIS =	0.6618566999999999D 04	ECCEN =	0.1211000000000000 01	INC =	0.3259999999999999D 02
ASN0D =	0.8139999999999999D 02	ARGP =	0.6040699999999999D 02	TAN0M =	0.1018090000000000D 03
EAN0M =	0.1011289736909772D 03	MAN0M =	0.1004481695590716D 03		

AUXILIARY CALCULATIONS

AP0GEE =	0.3226839064233206D 03	KM	PLRIGEE =	0.1627924309559598D 03	KM	PERI0D =	0.8935813214091380D 02	MIN
RANGE =	0.4058034132300353D 04	KM	ALT =	0.2512432309216819D 03	KM	TPITCH =	0.8938692960398236D 02	DEG
ECV =	-0.4641984480867212D 02	KM/SEC	E0V =	-0.3216647944953037D 01	KM/SEC	MAP2GEE =	0.3205528463699984D 03	KM
MPERIGEE =	0.1602511536299994D 03	KM	MPERI0D =	0.8931084161151252D 02	MIN	DARGP =	0.1117929829829709D 02	DEG/DAY
DASN0D =	-0.7393552696386070D 01	DEG/DAY						

***** EARTH CONSTANTS *****

EARTH SECOND HARMONIC 0.16234499E-02 EARTH THIRD HARMONIC 0.57500000E-05 EARTH FOURTH HARMONIC 0.78749999E-05
 EARTH GRAVITATIONAL CONSTANT (KILOMETERS CUBED/SECONDS SQUARED) 0.39860319E 06
 EQUATORIAL RADIUS (KILOMETERS) 0.63781650E 04 ELLIPTICITY 0.29830000E 03

***** BALLISTIC PARAMETERS *****

ANGLE OF ATTACK FUNCTION

ALPHA(DEGREES) ANOMALY(DEGREES)
 0. 0.36000000E 03

COEFFICIENT OF DRAG FUNCTION

CN ALPHA(DEGREES)
 0.20000000E 01 0.36000000E 03

CDPRIME

1.00000000E 00 PERIGEE(KILOMETERS)
 0.

EFFECTIVE DRAG AREA FUNCTION

AREA(METERS SQUARED) ALPHA(DEGREES)
 0.26040000E 02 0.36000000E 03

MASS CONSTANTS

INITIAL MASS(KILOGRAMS) 0.60399999E 04

***** DENSITY PARAMETERS *****

MONTH= 0.40E 01 DAY= 0.80E 01 YEAR 0.1964E 04 DAYS ELAPSED SINCE DEC. 31 , 1957 0.22899999E 04
 1959 ARDC ATMOSPHERE

DENSITY CORRECTION

DC	PERIGEE(KILOMETERS)
0.12000000E-00	0.50000000E 03
0.13000000E-00	0.40000000E 03
0.14200000E-00	0.34999999E 03
0.18400000E-00	0.30000000E 03
0.22000000E-00	0.27999999E 03
0.27500000E-00	0.26000000E 03
0.30400000E-00	0.25000000E 03
0.34000000E-00	0.23999999E 03
0.38500000E-00	0.23000000E 03
0.42500000E-00	0.22000000E 03
0.47000000E-00	0.20999999E 03
0.52000000E 00	0.20000000E 03
0.56500000E 00	0.19000000E 03
0.62000000E 00	0.18000000E 03
0.70000000E 00	0.16999999E 03
0.80000000E 00	0.16000000E 03
0.84000000E 00	0.15499999E 03
0.86000000E 00	0.15000000E 03
1.00000000E 00	0.14500000E 03
1.00000000E 00	0.

KP YEAR

0.23400000E 01	0.19580000E 04
0.24800000E 01	0.19588000E 04
0.18900000E 01	0.19588999E 04
0.25099999E 01	0.19589999E 04
0.29700000E 01	0.19591000E 04
0.24199999E 01	0.19592000E 04
0.25600000E 01	0.19593000E 04
0.25900000E 01	0.19594000E 04

0.29200C00E	01	0.19594999E	04
0.31599999E	01	0.195960C0E	04
0.34999999E	01	0.195970C0E	04
0.24600C00E	01	0.19598000E	04
0.289C0C00E	01	0.195990C0E	04
0.25699999E	01	0.19599999E	04
0.23199999E	01	0.19601000E	04
0.24400C00E	01	0.196020C0E	04
0.34199999E	01	0.19603000E	04
0.27899999E	01	0.19604000E	04
0.29200C00E	01	0.19605000E	04
0.27100C00E	01	0.19605999E	04
0.27500C00E	01	0.19606999E	04
0.32299999E	01	0.19608000E	04
0.34400C00E	01	0.19609000E	04
0.24900C00E	01	0.19610000E	04
0.22700C00E	01	0.196110C0E	04
0.23199999E	01	0.19611999E	04
0.22899999E	01	0.19613000E	04
0.23999999E	01	0.19614000E	04
0.26899999E	01	0.19615000E	04
0.22600C00E	01	0.19616000E	04
0.21799999E	01	0.19616999E	04
0.18499999E	01	0.19617999E	04
0.19199999E	01	0.19619000E	04
0.14900C00E	01	0.19620000E	04
0.17299999E	01	0.196210C0E	04
0.18099999E	01	0.196220C0E	04
0.23100C00E	01	0.19622999E	04
0.16000C00E	01	0.19623999E	04
0.21799999E	01	0.19625000E	04
0.26199999E	01	0.19626000E	04
0.29399999E	01	0.196270C0E	04
0.30800C00E	01	0.19628000E	04
0.20100C00E	01	0.19628999E	04
0.17500C00E	01	0.196200C0E	04
0.17200C00E	01	0.196310C0E	04
0.15400C00E	01	0.1963120C0E	04
0.15099999E	01	0.19632100E	04
0.18600C00E	01	0.19632900E	04
0.20800C00E	01	0.196338C0E	04
0.20599999E	01	0.19634600E	04
0.22300C00E	01	0.19635399E	04
0.23499999E	01	0.196362C0E	04
0.32600C00E	01	0.19637100E	04
0.21999999E	01	0.196379C0E	04
0.20200C00E	01	0.19638800E	04
0.19800C00E	01	0.19639600E	04
0.20599999E	01	0.19640400E	04
0.22099999E	01	0.19641200E	04
0.21600C00E	01	0.196421C0E	04
0.22499999E	01	0.196429C0E	04
0.18099999E	01	0.196438C0E	04
0.17299999E	01	0.19644599E	04
0.18900C00E	01	0.19645400E	04
0.16900C00E	01	0.19646200E	04
0.17800C00E	01	0.19647100E	04
0.16700C00E	01	0.19647899E	04
0.90000C00E	00	0.196488C0E	04
0.77000C00E	00	0.19649599E	04
0.24999999E	01	0.19650000E	04
0.24999999E	01	0.200000C0E	04

FTEN
0.

YEAR
0.

FIENB	YEAR
0.2436000E 03	0.19580000E 04
0.23070000E 03	0.19585000E 04
0.22650000E 03	0.19589999E 04
0.20890000E 03	0.19594999E 04
0.18049999E 03	0.19599999E 04
0.16100000E 03	0.19605000E 04
0.13079999E 03	0.19610000E 04
0.10479999E 03	0.19615000E 04
0.99300000E 02	0.19620000E 04
0.89699999E 02	0.19625000E 04
0.82699999E 02	0.19630000E 04
0.80800000E 02	0.19634999E 04
0.77899999E 02	0.19639999E 04
0.70000000E 02	0.19645000E 04
0.75000000E 02	0.19650000E 04
0.87000000E 02	0.19655000E 04
0.13100000E 03	0.19660000E 04
0.18600000E 03	0.19675000E 04
0.20000000E 03	0.19684999E 04
0.19000000E 03	0.19695000E 04
0.16300000E 03	0.19705000E 04
0.14200000E 03	0.19710000E 04
0.12800000E 03	0.19715000E 04
0.10800000E 03	0.19724999E 04
0.94000000E 02	0.19735000E 04
0.80999999E 02	0.19745000E 04
0.75000000E 02	0.19750000E 04
0.75000000E 02	0.19755000E 04

DIURNAL MEAN

***** SPECIAL EVENTS *****

EARTH IMPACT CUTOFF

***** INITIAL CONDITIONS *****

SHORT PRINTOUT

ANOMALY STEP(DLGRS) 0.99999999E 01

APOGEE STEPS(KM)	PERIGEE RADIUS(KM)
-0.49999999E 01	0.67780000E 04
-0.99999999E 01	0.65780000E 04
-0.20000000E 02	0.
0.	0.
0.	0.

APGEE, PERIGEE, MAJOR AXIS, AND EARTH RADIUS (KM)
 APGEE, PERIGEE, MAJOR AXIS RATES (KM/DAY) MASS (KG)
 ASCENDING NODE, ARGUMENT OF PERIGEE (DEG)
 NODE, PERIGEE REGRESSION RATES (DEG/DAY)
 PERIGEE VELOCITY (KM/SEC)
 ORBITAL PERIOD (MIN)
 LIFETIME SPENT (ORBIT AND DAY)
 RHO (KG/M3), EI (UNITLESS), RPERG AND RIPAPG (KM)

A	0.66987178E 04	P	0.65384161E 04	AXIS	0.66185670E 04	RADIUS	0.63734720E 04
ADDT	-0.20172292E 02	PDJT	-0.40069964E 01	AXIDJT	-0.12089644E 02	MASS	0.60399999E 04
NODE	0.81400000E 02	ARSP	0.60406999E 02	DNODE	-0.73800376E 01	DARGP	0.11164444E 02
VPERIG	0.78563969E 01	PERIOD	0.89310846E 02	ORBIT	0.	TIME	0.
RHO	0.10019261E-08	EI	0.12110000E-01	RPERG	0.16281848E 03	RIPAPG	0.32312018E 03

A	0.63687178E 04	P	0.63691773E 04	AXIS	0.63689475E 04	RADIUS	0.63724373E 04
ADDT	-0.45995754E 11	PDJT	-0.46000738E 11	AXIDJT	-0.45996245E 11	MASS	0.60399999E 04
NODE	0.51174578E 02	ARSP	0.10612672E 03	DNODE	-0.84419879E 01	DARGP	0.12769567E 02
VPERIG	0.79116516E 01	PERIOD	0.64306248E 02	ORBIT	0.60625867E 02	TIME	0.37282697E 01
RHO	0.12254324E 01	EI	-0.36066525E-04	RPERG	-0.59685668E 01	RIPAPG	-0.57626952E 01

EARTH ORBIT TRANSFORMATION

PHID =	0.2850000000000000 02	DEG	LAMD8 =	0.8050000000000000 02	DEG	AZFIR =	0.1050000000000000 03	DEG
A =	0.6378165000000000 04	KM	B =	0.6356783999999999 04	KM	OMEGA =	0.1504106705000000 02	DEG/HR
RADIUS =	0.6378165000000000 04	KM	KERTH =	0.3986032000000000 06	KM3/SEC2	J =	0.1623450000000000 -02	
H =	0.5750000000000000 -05		D =	0.7875000000000000 -05		XG =	0.	KM
YG =	0.	KM	ZG =	0.		XDG =	0.	KM/SEC
YDG =	0.	KM/SEC	ZDG =	0.		TFM =	0.	HOURS
INPUT IN MOT SYSTEM SHORT NOLONG								
POSITION (KM) VELOCITY (KM/SEC) ANGLES (DEG)								
EFP								
XE =	-0.3037077883473387D 04		YE =	-0.1046142628496821D 04		ZE =	0.2505989924336480D 04	
XDE =	0.5957248065928864D 01		YDE =	0.1620505487157563D 01		ZDE =	0.3982714918979543D 01	
PLT								
XPL =	-0.3037077883473385D 04		YPL =	-0.1046142628496822D 04		ZPL =	0.2505989924336479D 04	
XDPL =	0.5979686903636678D 01		YDPL =	0.1850067816184628D 01		ZDPL =	0.4105741525364290D 01	
EFE								
XEP =	-0.2630237597954840D 04		YEP =	-0.5986299572715291D 04		ZEP =	0.1089689476602931D 04	
XDEP =	0.5318120342908635D 01		YDEP =	-0.3161077262043163D 01		ZDEP =	-0.3962580881258863D 01	
SFE								
XS =	-0.2630237597954840D 04		YS =	-0.5986299572715291D 04		ZS =	0.1089689476602931D 04	
XDS =	0.5754648197067024D 01		YDS =	-0.3352877214687555D 01		ZDS =	-0.3962580881258863D 01	
TIME =	-0.		THETA =	-0.				
SFG								
R =	0.6628827615152297D 04		GCLAT =	0.9461594291796026D 01		LJNG =	0.2462804560176325D 03	
VS =	0.7749826367686954D 01		AZVS =	0.1213593542378151D 03		ELVS =	0.6884420409938637D 00	
EFG								
R =	0.6628827615152297D 04		GCLAT =	0.9461594291796026D 01		LJNG =	0.2462804560176325D 03	
VE =	0.7346894628261875D 01		AZVE =	0.1232945670245073D 03		ELVE =	0.7262007992049315D 00	
E0E								
AXIS =	0.6620903169689641D 04		ECCEN =	0.1207474821557146D -01		INC =	0.3261583446622047D 02	
ASN0D =	0.8137605735536910D 02		ARGP =	0.658662223696307D 02		TAN2M =	0.9637668968299269D 02	
EAN0M =	0.9568865963933066D 02		PAN0M =	0.950002346568445D 02				
M0E								
AXIS =	0.6618566999999999D 04		ECCEN =	0.1211000000000000D -01		INC =	0.3259999999999999D 02	
ASN0D =	0.8139999999999999D 02		ARGP =	0.6040699999999999D 02		TAN2M =	0.1018090000000000D 03	
EAN0M =	0.1011209736909772D 03		PAN2M =	0.1004481695590716D 03				
AUXILIARY CALCULATIONS								
APUGEL =	0.3226039084233206D 03	KM	PERIGEE =	0.1627924309559598D 03	KM	PERIOD =	0.8935213214091380D 02	MIN
RANGE =	0.4058034132300353D 04	KM	ALT =	0.2512432309218819D 03	KM	TPITCH =	0.8938692960398236D 02	DEG
ECV =	-0.4641964488867212D -02	KM/SEC	EEV =	-0.3216647944953037D 01	KM/SEC	MAPDUE =	0.3205528453699904D 03	KM
MPERIGEE =	0.1602511536299994D 03	KM	MPERIOD =	0.8931084161151252D 02	MIN	DARGP =	0.1117429829829709D 02	DEG/DAY
CASN0D =	-0.7393552696386070D 01	DEG/DAY						

***** EARTH CONSTANTS *****

EARTH SECOND HARMONIC 0.16234499E-02 EARTH THIRD HARMONIC 0.57500000E-05 EARTH FOURTH HARMONIC 0.78749999E-05
EARTH GRAVITATIONAL CONSTANT (KILOMETERS CUBED/SECONDS SQUARED) 0.39860319E 06
EQUATORIAL RADIUS (KILOMETERS) 0.63781650E 04 ELLIPTICITY 0.29830000E 03

***** BALLISTIC PARAMETERS *****

ANGLE OF ATTACK FUNCTION

ALPHA(DEGREES) ANOMALY(DEGREES)
0. 0.36000000E 03

COEFFICIENT OF DRAG FUNCTION

CN ALPHA(DEGREES)
0.20000000E 01 0.36000000E 03

CDPRIME PERIGEE(KILOMETERS)
1.00000000E 00 0.

EFFECTIVE DRAG AREA FUNCTION

AREA(METERS SQUARED) ALPHA(DEGREES)
0.26040000E 02 0.36000000E 03

MASS CONSTANTS

INITIAL MASS(KILOGRAMS) 0.60399999E 04

***** DENSITY PARAMETERS *****

MONTH= 0.40E 01 DAY= 0.80E 01 YEAR 0.1964E 04 DAYS ELAPSED SINCE DEC. 31, 1957 0.22899999E 04
1959 ARDC ATMOSPHERE

DENSITY CORRECTION

DC	PERIGEE(KILOMETERS)
0.12000000E-00	0.50000000E 03
0.13000000E-00	0.40000000E 03
0.14200000E-00	0.34999999E 03
0.18400000E-00	0.30000000E 03
0.22000000E-00	0.27999999E 03
0.27500000E-00	0.26000000E 03
0.30400000E-00	0.25000000E 03
0.34000000E-00	0.23999999E 03
0.38500000E-00	0.23000000E 03
0.42500000E-00	0.22000000E 03
0.47000000E-00	0.20999999E 03
0.52000000E 00	0.20000000E 03
0.56500000E 00	0.19000000E 03
0.62000000E 00	0.18000000E 03
0.70000000E 00	0.16999999E 03
0.80000000E 00	0.16000000E 03
0.84000000E 00	0.15499999E 03
0.86000000E 00	0.15000000E 03
1.00000000E 00	0.14500000E 03
1.00000000E 00	0.

KP	YEAR
0.23400000E 01	0.19580000E 04
0.24800000E 01	0.19588000E 04
0.18900000E 01	0.19588999E 04
0.25099999E 01	0.19589999E 04
0.29700000E 01	0.19591000E 04
0.24199999E 01	0.19592000E 04
0.25600000E 01	0.19593000E 04
0.25900000E 01	0.19594000E 04

0.29200000E 01	0.19594999E 04
0.31599999E 01	0.19596000E 04
0.34999999E 01	0.19597000E 04
0.24600000E 01	0.19598000E 04
0.28900000E 01	0.19599000E 04
0.25699999E 01	0.19599999E 04
0.23199999E 01	0.19601000E 04
0.24400000E 01	0.19602000E 04
0.34199999E 01	0.19603000E 04
0.27899999E 01	0.19604000E 04
0.29200000E 01	0.19605000E 04
0.27100000E 01	0.19605999E 04
0.27500000E 01	0.19606999E 04
0.32299999E 01	0.19608000E 04
0.34400000E 01	0.19609000E 04
0.24900000E 01	0.19610000E 04
0.22700000E 01	0.19611000E 04
0.23199999E 01	0.19611999E 04
0.22899999E 01	0.19613000E 04
0.23999999E 01	0.19614000E 04
0.26899999E 01	0.19615000E 04
0.22600000E 01	0.19616000E 04
0.21799999E 01	0.19616999E 04
0.18499999E 01	0.19617999E 04
0.19199999E 01	0.19619000E 04
0.14900000E 01	0.19620000E 04
0.17299999E 01	0.19621000E 04
0.18099999E 01	0.19622000E 04
0.23100000E 01	0.19622999E 04
0.16000000E 01	0.19623999E 04
0.21799999E 01	0.19625000E 04
0.26199999E 01	0.19626000E 04
0.29399999E 01	0.19627000E 04
0.30800000E 01	0.19628000E 04
0.20100000E 01	0.19628999E 04
0.17500000E 01	0.19629000E 04
0.17200000E 01	0.19631000E 04
0.15400000E 01	0.19631200E 04
0.15099999E 01	0.19632100E 04
0.18600000E 01	0.19632900E 04
0.20800000E 01	0.19633800E 04
0.20599999E 01	0.19634600E 04
0.22300000E 01	0.19635399E 04
0.23499999E 01	0.19636200E 04
0.32600000E 01	0.19637100E 04
0.21999999E 01	0.19637900E 04
0.20200000E 01	0.19638800E 04
0.19800000E 01	0.19639600E 04
0.20599999E 01	0.19640400E 04
0.22099999E 01	0.19641200E 04
0.21600000E 01	0.19642100E 04
0.22499999E 01	0.19642900E 04
0.18099999E 01	0.19643800E 04
0.17299999E 01	0.19644599E 04
0.18900000E 01	0.19645400E 04
0.16800000E 01	0.19645200E 04
0.17800000E 01	0.19647100E 04
0.16700000E 01	0.19647899E 04
0.90000000E 00	0.19648800E 04
0.77000000E 00	0.19649599E 04
0.24999999E 01	0.19650000E 04
0.24999999E 01	0.20000000E 04

FTEN
0.

YEAR
0.

FTENB	YEAR
0.24360C00E 03	0.19580000E 04
0.23070C00E 03	0.19585000E 04
0.22650C00E 03	0.19589999E 04
0.20890000E 03	0.19594999E 04
0.18049999E 03	0.19599999E 04
0.16100C00E 03	0.19605000E 04
0.13079999E 03	0.19610000E 04
0.10479999E 03	0.19615000E 04
0.99300C00E 02	0.19620000E 04
0.89699999E 02	0.19625000E 04
0.82699999E 02	0.19630000E 04
0.80800C00E 02	0.19634999E 04
0.77899999E 02	0.19639999E 04
0.70000C00E 02	0.19645000E 04
0.75000C00E 02	0.19650000E 04
0.87000C00E 02	0.19655000E 04
0.13100C00E 03	0.19665000E 04
0.18600C00E 03	0.19675000E 04
0.20000C00E 03	0.19684999E 04
0.19000000E 03	0.19695000E 04
0.16300C00E 03	0.19705000E 04
0.14200C00E 03	0.19710000E 04
0.12800C00E 03	0.19715000E 04
0.10800C00E 03	0.19724999E 04
0.94000000E 02	0.19735000E 04
0.80999999E 02	0.19745000E 04
0.75000C00E 02	0.19750000E 04
0.75000C00E 02	0.19755000E 04

DIURNAL MEAN

***** SPECIAL EVENTS *****

EARTH IMPACT CUTOFF

***** INITIAL CONDITIONS *****

DETAIL PRINTOUT

ANOMALY STEP(DEGREES) 0.99999999E 01

APOGEE STEPS(KM)	PERIGEE RADIUS(KM)
-0.49999999E 01	0.67780000E 04
-0.99999999E 01	0.65780000E 04
-0.20000C00E 02	0.
0.	0.
0.	0.

APOGEE, PERIGEE, MAJOR AXIS, AND EARTH RADIUS (KM)
 APOGEE, PERIGEE, MAJOR AXIS RATES (KM/DAY) MASS (KG)
 ASCENDING NODE, ARGUMENT OF PERIGEE (DEG)
 NODE, PERIGEE REGRESSION RATES (DEG/DAY)
 PERIGEE VELOCITY (KM/SEC)
 ORBITAL PERIOD (MIN)
 LIFETIME SPENT (ORBIT AND DAY)
 RH0 (KG/H3), EI (UNITLESS), RIPEG AND RIPAPG (KM)

A	0.66987178E 04	P	0.65384161E 04	AXIS	0.66185670E 04	RADIUS	0.63734720E 04
ADOT	-0.20172292E 02	PDOT	-0.40069964E 01	AXIDOT	-0.12089644E 02	MASS	0.60399999E 04
NODE	0.81400006E 02	ARGP	0.60406999E 02	DNODE	-0.73808376E 01	DARGP	0.11164444E 02
VPERIG	0.78563969E 01	PERIOD	0.89310846E 02	ORBIT	0.	TIME	0.
RH0	0.16019261E-08	EI	0.12110000E-01	RIPEG	0.16281848E 03	RIPAPG	0.32312018E 03
A	0.66887178E 04	P	0.65363847E 04	AXIS	0.66125512E 04	RADIUS	0.63729899E 04
ADOT	-0.21854386E 02	PDOT	-0.45366886E 01	AXIDOT	-0.13195537E 02	MASS	0.60399999E 04
NODE	0.77741100E 02	ARGP	0.65941543E 02	DNODE	-0.74041695E 01	DARGP	0.11199737E 02
VPERIG	0.78550523E 01	PERIOD	0.89189111E 02	ORBIT	0.76963580E 01	TIME	0.47668843E-00
RH0	0.10763352E-08	EI	0.11518484E-01	RIPEG	0.16103314E 03	RIPAPG	0.31368445E 03
A	0.66787178E 04	P	0.65342648E 04	AXIS	0.66064913E 04	RADIUS	0.63726118E 04
ADOT	-0.23836359E 02	PDOT	-0.51580800E 01	AXIDOT	-0.14497220E 02	MASS	0.60399999E 04
NODE	0.74353144E 02	ARGP	0.71066251E 02	DNODE	-0.74277838E 01	DARGP	0.11235456E 02
VPERIG	0.78538398E 01	PERIOD	0.89066537E 02	ORBIT	0.14785457E 02	TIME	0.91516171E 00
RH0	0.11652293E-08	EI	0.10932652E-01	RIPEG	0.15911090E 03	RIPAPG	0.30412115E 03
A	0.66687178E 04	P	0.65320580E 04	AXIS	0.66003878E 04	RADIUS	0.63723129E 04
ADOT	-0.26187366E 02	PDOT	-0.58897937E 01	AXIDOT	-0.16038579E 02	MASS	0.60399999E 04
NODE	0.71236986E 02	ARGP	0.75779830E 02	DNODE	-0.74516790E 01	DARGP	0.11271600E 02
VPERIG	0.78527560E 01	PERIOD	0.88943137E 02	ORBIT	0.21272498E 02	TIME	0.13158407E 01
RH0	0.12720751E-08	EI	0.10352410E-01	RIPEG	0.15705157E 03	RIPAPG	0.29444018E 03
A	0.66587178E 04	P	0.65297680E 04	AXIS	0.65942429E 04	RADIUS	0.63721424E 04
ADOT	-0.29008224E 02	PDOT	-0.67591456E 01	AXIDOT	-0.17883664E 02	MASS	0.60399999E 04
NODE	0.68391461E 02	ARGP	0.80084042E 02	DNODE	-0.74758501E 01	DARGP	0.11308163E 02
VPERIG	0.78517914E 01	PERIOD	0.88818957E 02	ORBIT	0.27161858E 02	TIME	0.16770955E 01
RH0	0.14009906E-08	EI	0.97774551E-02	RIPEG	0.15486291E 03	RIPAPG	0.28465612E 03
A	0.66487178E 04	P	0.65273999E 04	AXIS	0.65880588E 04	RADIUS	0.63720265E 04
ADOT	-0.32431474E 02	PDOT	-0.78004355E 01	AXIDOT	-0.20115954E 02	MASS	0.60399999E 04
NODE	0.65814312E 02	ARGP	0.83982302E 02	DNODE	-0.75002896E 01	DARGP	0.11345130E 02
VPERIG	0.78509342E 01	PERIOD	0.88694043E 02	ORBIT	0.32462037E 02	TIME	0.20055498E 01
RH0	0.15571679E-08	EI	0.92074110E-02	RIPEG	0.15255591E 03	RIPAPG	0.27478613E 03
A	0.66387178E 04	P	0.65249590E 04	AXIS	0.65818384E 04	RADIUS	0.63719703E 04
ADOT	-0.36582107E 02	PDOT	-0.90565055E 01	AXIDOT	-0.22819306E 02	MASS	0.60399999E 04
NODE	0.63501654E 02	ARGP	0.87480488E 02	DNODE	-0.75249887E 01	DARGP	0.11382490E 02
VPERIG	0.78501709E 01	PERIOD	0.88568456E 02	ORBIT	0.37189028E 02	TIME	0.22962875E 01
RH0	0.17472959E-08	EI	0.86418749E-02	RIPEG	0.15014362E 03	RIPAPG	0.26484796E 03
A	0.66287178E 04	P	0.65224504E 04	AXIS	0.65755841E 04	RADIUS	0.63719590E 04
ADOT	-0.41668416E 02	PDOT	-0.10584679E 02	AXIDOT	-0.26126547E 02	MASS	0.60399999E 04
NODE	0.61444640E 02	ARGP	0.90291979E 02	DNODE	-0.75499392E 01	DARGP	0.11420231E 02
VPERIG	0.78494492E 01	PERIOD	0.88442247E 02	ORBIT	0.41366296E 02	TIME	0.25528480E 01
RH0	0.19801765E-08	EI	0.80804481E-02	RIPEG	0.14763916E 03	RIPAPG	0.25485864E 03
A	0.66187178E 04	P	0.65198807E 04	AXIS	0.65692793E 04	RADIUS	0.63719793E 04
ADOT	-0.46000609E 02	PDOT	-0.12472527E 02	AXIDOT	-0.30237567E 02	MASS	0.60399999E 04
NODE	0.59632730E 02	ARGP	0.93332718E 02	DNODE	-0.75751306E 01	DARGP	0.11458337E 02
VPERIG	0.78488757E 01	PERIOD	0.89315480E 02	ORBIT	0.45016393E 02	TIME	0.27768310E 01
RH0	0.22675510E-08	EI	0.75226466E-02	RIPEG	0.14505602E 03	RIPAPG	0.24483331E 03

A	0.66087178E 04	P	0.65172561E 04	AXIS	0.65629869E 04	RADIUS	0.63720200E 04
ADDT	-0.55973225E 02	PDOT	-0.14833832E 02	AXIDOT	-0.35403528E 02	MASS	0.60399999E 04
NODE	0.58054795E 02	ARGP	0.95719543E 02	DNODE	-0.76005523E 01	DARGP	0.11496790E 02
VPERIG	0.78483187E 01	PERIOD	0.88188218E 02	ORBIT	0.48174605E 02	TIME	0.29701240E 01
RHO	0.26253967E-08	EI	0.69680004E-02	RIPERG	0.14240667E 03	RIPAPG	0.23478466E 03
A	0.65987178E 04	P	0.65145827E 04	AXIS	0.65566503E 04	RADIUS	0.63720719E 04
ADDT	-0.66103096E 02	PDOT	-0.17819200E 02	AXIDOT	-0.41961148E 02	MASS	0.60399999E 04
NODE	0.56696904E 02	ARGP	0.97773523E 02	DNODE	-0.76261927E 01	DARGP	0.11535574E 02
VPERIG	0.78478073E 01	PERIOD	0.88060527E 02	ORBIT	0.50869267E 02	TIME	0.31349111E 01
RHO	0.30758083E-08	EI	0.64160102E-02	RIPERG	0.13970275E 03	RIPAPG	0.22472332E 03
A	0.65887178E 04	P	0.65118655E 04	AXIS	0.65502916E 04	RADIUS	0.63721281E 04
ADDT	-0.79264738E 02	PDOT	-0.21702515E 02	AXIDOT	-0.50483626E 02	MASS	0.60399999E 04
NODE	0.55543222E 02	ARGP	0.99518611E 02	DNODE	-0.76520441E 01	DARGP	0.11574678E 02
VPERIG	0.78473331E 01	PERIOD	0.87932458E 02	ORBIT	0.53137720E 02	TIME	0.32734323E 01
RHO	0.36504593E-08	EI	0.58663261E-02	RIPERG	0.13695270E 03	RIPAPG	0.21465692E 03
A	0.65787178E 04	P	0.65091074E 04	AXIS	0.65439127E 04	RADIUS	0.63721834E 04
ADDT	-0.79264738E 02	PDOT	-0.26856437E 02	AXIDOT	-0.61755563E 02	MASS	0.60399999E 04
NODE	0.54577845E 02	ARGP	0.10097887E 03	DNODE	-0.76781022E 01	DARGP	0.11614094E 02
VPERIG	0.78468911E 01	PERIOD	0.87804039E 02	ORBIT	0.55017389E 02	TIME	0.33880452E 01
RHO	0.43957919E-08	EI	0.53187103E-02	RIPERG	0.13418217E 03	RIPAPG	0.20459143E 03
A	0.65687178E 04	P	0.65063073E 04	AXIS	0.65375125E 04	RADIUS	0.63722347E 04
ADDT	-0.12024515E 03	PDOT	-0.33940001E 02	AXIDOT	-0.77092577E 02	MASS	0.60399999E 04
NODE	0.53783459E 02	ARGP	0.10218047E 03	DNODE	-0.77043711E 01	DARGP	0.11653829E 02
VPERIG	0.78464800E 01	PERIOD	0.87675259E 02	ORBIT	0.56546763E 02	TIME	0.34811621E 01
RHO	0.53830783E-08	EI	0.47732574E-02	RIPERG	0.13133202E 03	RIPAPG	0.19453058E 03
A	0.65487178E 04	P	0.65005544E 04	AXIS	0.65246361E 04	RADIUS	0.63723277E 04
ADDT	-0.20129748E 03	PDOT	-0.59263927E 02	AXIDOT	-0.13028070E 03	MASS	0.60399999E 04
NODE	0.52502015E 02	ARGP	0.10411882E 03	DNODE	-0.77576034E 01	DARGP	0.11734350E 02
VPERIG	0.78457771E 01	PERIOD	0.87416356E 02	ORBIT	0.58709557E 02	TIME	0.36124563E 01
RHO	0.86214397E-08	EI	0.36908918E-02	RIPERG	0.12552423E 03	RIPAPG	0.17441961E 03
A	0.65287178E 04	P	0.64944185E 04	AXIS	0.65115681E 04	RADIUS	0.63723896E 04
ADDT	-0.39824621E 03	PDOT	-0.12856697E 03	AXIDOT	-0.26340659E 03	MASS	0.60399999E 04
NODE	0.51731255E 02	ARGP	0.10528468E 03	DNODE	-0.78121534E 01	DARGP	0.11816864E 02
VPERIG	0.78453854E 01	PERIOD	0.87153862E 02	ORBIT	0.59921826E 02	TIME	0.36858271E 01
RHO	0.15900792E-07	EI	0.26337263E-02	RIPERG	0.11935028E 03	RIPAPG	0.15434387E 03
A	0.65087178E 04	P	0.64875169E 04	AXIS	0.64981174E 04	RADIUS	0.63724229E 04
ADDT	-0.11186879E 04	PDOT	-0.41531130E 03	AXIDOT	-0.76699963E 03	MASS	0.60399999E 04
NODE	0.51338927E 02	ARGP	0.10587813E 03	DNODE	-0.78688589E 01	DARGP	0.11902638E 02
VPERIG	0.78456540E 01	PERIOD	0.86883955E 02	ORBIT	0.60463034E 02	TIME	0.37184814E 01
RHO	0.39444161E-07	EI	0.16313130E-02	RIPERG	0.11242608E 03	RIPAPG	0.13430102E 03
A	0.64887178E 04	P	0.64790406E 04	AXIS	0.64838792E 04	RADIUS	0.63724351E 04
ADDT	-0.70584279E 04	PDOT	-0.36614551E 04	AXIDOT	-0.53599416E 04	MASS	0.60399999E 04
NODE	0.51198246E 02	ARGP	0.10609093E 03	DNODE	-0.79295006E 01	DARGP	0.11994366E 02
VPERIG	0.78473248E 01	PERIOD	0.86598551E 02	ORBIT	0.60608292E 02	TIME	0.37272170E 01
RHO	0.18488389E-06	EI	0.74624963E-03	RIPERG	0.10393823E 03	RIPAPG	0.11428174E 03
A	0.64687178E 04	P	0.64654747E 04	AXIS	0.64670962E 04	RADIUS	0.63724370E 04
ADDT	-0.13953651E 06	PDOT	-0.11068875E 06	AXIDOT	-0.12511238E 06	MASS	0.60399999E 04
NODE	0.51175778E 02	ARGP	0.10612491E 03	DNODE	-0.80017868E 01	DARGP	0.12103708E 02
VPERIG	0.78536133E 01	PERIOD	0.86262540E 02	ORBIT	0.60625134E 02	TIME	0.37282259E 01
RHO	0.26460587E-05	EI	0.25074344E-03	RIPERG	0.90364990E 02	RIPAPG	0.94273559E 02
A	0.64487178E 04	P	0.64478099E 04	AXIS	0.64482634E 04	RADIUS	0.63724373E 04
ADDT	-0.34856556E 07	PDOT	-0.32746775E 07	AXIDOT	-0.33801666E 07	MASS	0.60399999E 04
NODE	0.51174630E 02	ARGP	0.10612664E 03	DNODE	-0.90839223E 01	DARGP	0.12227948E 02
VPERIG	0.78636104E 01	PERIOD	0.85886586E 02	ORBIT	0.60625828E 02	TIME	0.37282673E 01
RHO	0.67216545E-04	EI	0.70477095E-04	RIPERG	0.72692387E 02	RIPAPG	0.74266540E 02

A	0.64287178E 04	P	0.64284943E 04	AXIS	0.64286062E 04	RADIUS	0.63724373E 04
ADDT	-0.36040654E 08	PDOT	-0.35568516E 08	AXIDOT	-0.35804585E 08	MASS	0.60399999E 04
NODE	0.51174583E 02	ARGP	0.10612672E 03	DNODE	-0.81708138E 01	DARGP	0.12359383E 02
VPERIG	0.78752603E 01	PERIOD	0.85493578E 02	ORBIT	0.60625864E 02	TIME	0.37282695E 01
RH0	0.72545402E-03	EI	0.17350844E-04	RIPERG	0.53371032E 02	RIPAPG	0.54259277E 02
A	0.64087178E 04	P	0.64086128E 04	AXIS	0.64086653E 04	RADIUS	0.63724373E 04
ADDT	-0.57522210E 09	PDOT	-0.57563592E 09	AXIDOT	-0.57542901E 09	MASS	0.60399999E 04
NODE	0.51174579E 02	ARGP	0.10612672E 03	DNODE	-0.82601909E 01	DARGP	0.12494577E 02
VPERIG	0.78874360E 01	PERIOD	0.85096096E 02	ORBIT	0.60625867E 02	TIME	0.37282697E 01
RH0	0.10391000E-01	EI	0.81952714E-05	RIPERG	0.33481811E 02	RIPAPG	0.34251953E 02
A	0.63887178E 04	P	0.63887154E 04	AXIS	0.63887166E 04	RADIUS	0.63724373E 04
ADDT	-0.12913613E 11	PDOT	-0.12713984E 11	AXIDOT	-0.12813799E 11	MASS	0.60399999E 04
NODE	0.51174578E 02	ARGP	0.10612672E 03	DNODE	-0.83508641E 01	DARGP	0.12631731E 02
VPERIG	0.78996825E 01	PERIOD	0.84699079E 02	ORBIT	0.60625867E 02	TIME	0.37282697E 01
RH0	0.24382363E-00	EI	0.18629493E-06	RIPERG	0.13577026E 02	RIPAPG	0.14244629E 02
A	0.63687178E 04	P	0.63691773E 04	AXIS	0.63689475E 04	RADIUS	0.63724373E 04
ADDT	-0.45995754E 11	PDOT	-0.46000738E 11	AXIDOT	-0.45998245E 11	MASS	0.60399999E 04
NODE	0.51174578E 02	ARGP	0.10612672E 03	DNODE	-0.84419879E 01	DARGP	0.12769567E 02
VPERIG	0.79116516E 01	PERIOD	0.84306248E 02	ORBIT	0.60625867E 02	TIME	0.37282697E 01
RH0	0.12254324E 01	EI	-0.36066525E-04	RIPERG	-0.59685668E 01	RIPAPG	-0.57626952E 01
A	0.63687178E 04	P	0.63691773E 04	AXIS	0.63689475E 04	RADIUS	0.63724373E 04
ADDT	-0.45995754E 11	PDOT	-0.46000738E 11	AXIDOT	-0.45998245E 11	MASS	0.60399999E 04
NODE	0.51174578E 02	ARGP	0.10612672E 03	DNODE	-0.84419879E 01	DARGP	0.12769567E 02
VPERIG	0.79116516E 01	PERIOD	0.84306248E 02	ORBIT	0.60625867E 02	TIME	0.37282697E 01
RH0	0.12254324E 01	EI	-0.36066525E-04	RIPERG	-0.59685668E 01	RIPAPG	-0.57626952E 01

EARTH ORBIT TRANSFORMATION

PHIB = 0.2850000000000000 02	DEG	LAPD8 = 0.8050000000000000 02	DEG	AZFIR = 0.1050000000000000 03	DEG
A = 0.6378165000000000 04	KM	B = 0.6356783999999999 04	KM	OMEGA = 0.1504167050000000 02	DEG/HR
RADIUS = 0.6378165000000000 04	KM	KERTH = 0.3986032000000000 06	KM3/SLC2	J = 0.1623450000000000 -02	
H = 0.5750000000000000 -05		D = 0.7875000000000000 -05		XG = 0.	KM
YG = 0.	KM	ZG = 0.	KM	XDG = 0.	KM/SEC
YDG = 0.	KM/SEC	ZDG = 0.	KM/SEC	TFM = 0.	HOURS

INPUT IN MET SYSTEM SHORT NO LONG

POSITION (KM) VELOCITY (KM/SEC) ANGLES (DEG)

EFP

XE = -0.3037077883473387 04	YE = -0.1046142628496821 04	ZE = 0.2505989924336480 04
XDE = 0.5957246665928864 01	YDE = 0.1620505487157563 01	ZDE = 0.3982714918979543 01

PLT

XPPL = -0.3037077883473385 04	YPL = -0.1046142628496822 04	ZPL = 0.2505989924336479 04
XDPL = 0.5979686903636780 01	YDPL = 0.1850067816184628 01	ZDPL = 0.4105741525364290 01

EFE

XEP = -0.2630237597954840 04	YEP = -0.5986299572715291 04	ZEP = 0.1089689476602931 04
XDEP = 0.5318120342908635 01	YDEP = -0.3161077262043163 01	ZDEP = -0.3962580881258863 01

SFE

XS = -0.2630237597954840 04	YS = -0.5986255572715291 04	ZS = 0.1089689476602931 04
XDS = 0.5754648197067024 01	YDS = -0.3352877214687555 01	ZDS = -0.3962580881258863 01

TIME = -0.

THETA = -0.

SFG

R = 0.6628827615152297 04	GCLAT = 0.9461594291796026 01	L2NG = 0.2462804560176325 03
VS = 0.7749826367686954 01	AZVS = 0.1213593542378151 03	ELVS = 0.6884420409938637 00

EFG

R = 0.6628827615152297 04	GCLAT = 0.9461594291796026 01	L2NG = 0.2462804560176325 03
VE = 0.7346894628261875 01	AZVE = 0.1232949670245073 03	ELVE = 0.7262007992049315 00

E0E

AXIS = 0.6620903169689641 04	ECCEN = 0.1207474821557146 -01	INC = 0.3261583446622047 02
ASNDD = 0.8137605735536910 02	ARGP = 0.6536622223696307 02	TAN2M = 0.9637668968299269 02

EANDM = 0.9568865963933066 02

MAN2M = 0.9500234656844450 02

M0E

AXIS = 0.6618566999999999 04	ECCEN = 0.1211000000000000 -01	INC = 0.3259999999999999 02
ASNDD = 0.8139999999999999 02	ARGP = 0.6040699999999999 02	TAN2M = 0.1018090000000000 03

EANDM = 0.1011289736909772 03

MAN2M = 0.1004481695590716 03

AUXILIARY CALCULATIONS

APBGE = 0.3226839064233206 03	KM	PERIGEE = 0.1627924309559598 03	KM	PERIOD = 0.8935813214091300 02	MIN
RANGE = 0.4058034132300353 04	KM	ALT = 0.2512432309216819 03	KM	TPITCH = 0.8938692960398236 02	DEG
ECV = -0.4641984480867217 -02	KM/SEC	ELEV = -0.3216647944953037 01	KM/SLC	MAP2GEE = 0.3205528463679984 03	KM
MPERIGEE = 0.1602511536299994 03	KM	MPERIOD = 0.8931064161151252 02	MIN	DARGP = 0.1117929829829709 02	DEG/DAY
CASNDD = -0.7393552696386070 01	DEG/DAY				

***** EARTH CONSTANTS *****

EARTH SECOND HARMONIC 0.16234499E-02 EARTH THIRD HARMONIC 0.57500000E-05 EARTH FOURTH HARMONIC 0.78749999E-05
 EARTH GRAVITATIONAL CONSTANT (KILOMETERS CUBED/SECONDS SQUARED) 0.39860319E 06
 EQUATORIAL RADIUS (KILOMETERS) 0.63781650E 04 ELLIPTICITY 0.29830000E 03

***** BALLISTIC PARAMETERS *****

ANGLE OF ATTACK FUNCTION

ALPHA(DEGREES) ANOMALY(DEGREES)
 0. 0.36000000E 03

COEFFICIENT OF DRAG FUNCTION

CN ALPHA(DEGREES)
 0.20000000E 01 0.36000000E 03

CDPRIME

1.00000000E 00 PERIGEE (KILOMETERS)

0.

EFFECTIVE DRAG AREA FUNCTION

AREA(METERS SQUARED) ALPHA(DEGREES)
 0.26040000E 02 0.36000000E 03

MASS CONSTANTS

INITIAL MASS(KILOGRAMS) 0.60399999E 04

***** DENSITY PARAMETERS *****

MBNTH= 0.40E 01 DAY= 0.80E 01 YEAR 0.1964E 04 DAYS ELAPSED SINCE DEC. 31 , 1957 0.22899999E 04
 1959 ARDC ATMOSPHERE

DENSITY CORRECTION

DC PERIGEE(KILOMETERS)

0.12000000E-00	0.50000000E 03
0.13000000E-00	0.40000000E 03
0.14000000E-00	0.34999999E 03
0.18400000E-00	0.30000000E 03
0.22000000E-00	0.27999999E 03
0.27500000E-00	0.26000000E 03
0.30400000E-00	0.25000000E 03
0.34000000E-00	0.23999999E 03
0.38500000E-00	0.23000000E 03
0.42500000E-00	0.22000000E 03
0.47000000E-00	0.20999999E 03
0.52000000E 00	0.20000000E 03
0.56500000E 00	0.19000000E 03
0.62000000E 00	0.18000000E 03
0.70000000E 00	0.16999999E 03
0.80000000E 00	0.16000000E 03
0.84000000E 00	0.15499999E 03
0.86000000E 00	0.15000000E 03
1.00000000E 00	0.14500000E 03
1.00000000E 00	0.

KP

YEAR

0.23400000E 01	0.19580000E 04
0.24800000E 01	0.19580000E 04
0.18900000E 01	0.19588999E 04
0.25099999E 01	0.19589999E 04
0.29700000E 01	0.19591000E 04
0.24199999E 01	0.19592000E 04
0.25600000E 01	0.19593000E 04
0.25900000E 01	0.19594000E 04

0.29200000E 01	0.19594999E 04
0.31599999E 01	0.19596000E 04
0.34999999E 01	0.19597000E 04
0.24600000E 01	0.19598000E 04
0.28900000E 01	0.19599000E 04
0.25699999E 01	0.19599999E 04
0.23199999E 01	0.19601000E 04
0.24400000E 01	0.19602000E 04
0.34199999E 01	0.19603000E 04
0.27899999E 01	0.19604000E 04
0.29200000E 01	0.19605000E 04
0.27100000E 01	0.19605999E 04
0.27500000E 01	0.19606999E 04
0.32299999E 01	0.19608000E 04
0.34400000E 01	0.19609000E 04
0.24900000E 01	0.19610000E 04
0.22700000E 01	0.19611000E 04
0.23199999E 01	0.19611999E 04
0.22899999E 01	0.19613000E 04
0.23999999E 01	0.19614000E 04
0.26899999E 01	0.19615000E 04
0.22600000E 01	0.19616000E 04
0.21799999E 01	0.19616999E 04
0.18499999E 01	0.19617999E 04
0.19199999E 01	0.19619000E 04
0.14900000E 01	0.19620000E 04
0.17299999E 01	0.19621000E 04
0.18099999E 01	0.19622000E 04
0.23100000E 01	0.19622999E 04
0.16000000E 01	0.19623999E 04
0.21799999E 01	0.19625000E 04
0.26199999E 01	0.19626000E 04
0.29399999E 01	0.19627000E 04
0.30800000E 01	0.19628000E 04
0.20100000E 01	0.19628999E 04
0.17500000E 01	0.19629000E 04
0.17200000E 01	0.19631000E 04
0.15400000E 01	0.19631200E 04
0.15099999E 01	0.19632100E 04
0.18600000E 01	0.19632900E 04
0.20800000E 01	0.19633800E 04
0.20599999E 01	0.19634600E 04
0.22300000E 01	0.19635399E 04
0.23499999E 01	0.19636200E 04
0.32600000E 01	0.19637100E 04
0.21999999E 01	0.19637900E 04
0.20200000E 01	0.19638800E 04
0.19800000E 01	0.19639600E 04
0.20599999E 01	0.19640400E 04
0.22099999E 01	0.19641200E 04
0.21600000E 01	0.19642100E 04
0.22499999E 01	0.19642900E 04
0.18099999E 01	0.19643800E 04
0.17299999E 01	0.19644599E 04
0.18900000E 01	0.19645400E 04
0.16800000E 01	0.19646200E 04
0.17600000E 01	0.19647100E 04
0.16700000E 01	0.19647899E 04
0.90000000E 00	0.19648800E 04
0.77000000E 00	0.19649599E 04
0.24999999E 01	0.19650000E 04
0.24999999E 01	0.20000000E 04

FIN

0.

Y12

0.

FIENB	YEAR
0.24360000E 03	0.19580000E 04
0.23070000E 03	0.19585000E 04
0.22650000E 03	0.19589999E 04
0.20890000E 03	0.19594999E 04
0.18049999E 03	0.19599999E 04
0.16100000E 03	0.19605000E 04
0.13079999E 03	0.19610000E 04
0.10479999E 03	0.19615000E 04
0.99300000E 02	0.19620000E 04
0.89699999E 02	0.19625000E 04
0.82699999E 02	0.19630000E 04
0.80800000E 02	0.19634999E 04
0.77899999E 02	0.19639999E 04
0.70000000E 02	0.19645000E 04
0.75000000E 02	0.19650000E 04
0.87000000E 02	0.19655000E 04
0.13100000E 03	0.19660000E 04
0.18600000E 03	0.19675000E 04
0.20000000E 03	0.19684999E 04
0.19000000E 03	0.19695000E 04
0.16300000E 03	0.19705000E 04
0.14200000E 03	0.19710000E 04
0.12800000E 03	0.19715000E 04
0.10800000E 03	0.19724999E 04
0.94000000E 02	0.19735000E 04
0.80999999E 02	0.19745000E 04
0.75000000E 02	0.19750000E 04
0.75000000E 02	0.19755000E 04

DIURNAL MEAN

***** SPECIAL EVENTS *****

EARTH IMPACT CUTOFF

***** INITIAL CONDITIONS *****

SHORT PRINTOUT

ANOMALY STEP(DLGRS) 0.99999999E 01

APOGEE STEPS(KM)	PERIGEE RADIUS(KM)
-0.49999999E 01	0.67780000E 04
-0.99999999E 01	0.65780000E 04
-0.20000000E 02	0.
0.	0.
0.	0.

AP0GEE, PERIGEE, MAJOR AXIS, AND, EARTH RADIUS (KM)
 AP0GEE, PERIGEE, AND MAJOR AXIS RATES (KM/DAY)
 LIFETIME SPENT (2RBIT AND DAY)

A	0.66987178E 04	P	0.65384161E 04	AXIS	0.66185670E 04	RADIUS	0.63734720E 04	TIME	0.
ADBT	-0.20172292E 02	PDBT	-0.40069964E 01	AXIDBT	-0.12089644E 02	2RBIT	0.		
A	0.66887178E 04	P	0.65363847E 04	AXIS	0.66125512E 04	RADIUS	0.63729899E 04	TIME	0.47668843E-00
ADBT	-0.21854386E 02	PDBT	-0.45366886E 01	AXIDBT	-0.13195537E 02	2RBIT	0.76963580E 01		
A	0.66787178E 04	P	0.65342648E 04	AXIS	0.66064913E 04	RADIUS	0.63726118E 04	TIME	0.91516171E 00
ADBT	-0.23836359E 02	PDBT	-0.51580800E 01	AXIDBT	-0.14497220E 02	2RBIT	0.14785457E 02		
A	0.66687178E 04	P	0.65320580E 04	AXIS	0.66003878E 04	RADIUS	0.63723329E 04	TIME	0.13158407E 01
ADBT	-0.26187366E 02	PDBT	-0.58897937E 01	AXIDBT	-0.16038579E 02	2RBIT	0.21272498E 02		
A	0.66587178E 04	P	0.65297680E 04	AXIS	0.65942429E 04	RADIUS	0.63721424E 04	TIME	0.16790955E 01
ADBT	-0.29008224E 02	PDBT	-0.67591456E 01	AXIDBT	-0.17883684E 02	2RBIT	0.27161858E 02		
A	0.66487178E 04	P	0.65273999E 04	AXIS	0.65880588E 04	RADIUS	0.63720265E 04	TIME	0.20055498E 01
ADBT	-0.32431474E 02	PDBT	-0.78004355E 01	AXIDBT	-0.20115954E 02	2RBIT	0.32462037E 02		
A	0.66387178E 04	P	0.65249590E 04	AXIS	0.65818384E 04	RADIUS	0.63719703E 04	TIME	0.22962875E 01
ADBT	-0.36582107E 02	PDBT	-0.90565055E 01	AXIDBT	-0.22819306E 02	2RBIT	0.37189028E 02		
A	0.66287178E 04	P	0.65224504E 04	AXIS	0.65755841E 04	RADIUS	0.63719590E 04	TIME	0.25528480E 01
ADBT	-0.41668416E 02	PDBT	-0.10584679E 02	AXIDBT	-0.26126547E 02	2RBIT	0.41366296E 02		
A	0.66187178E 04	P	0.65198807E 04	AXIS	0.65692993E 04	RADIUS	0.63719793E 04	TIME	0.27768318E 01
ADBT	-0.48006608E 02	PDBT	-0.12472527E 02	AXIDBT	-0.30239567E 02	2RBIT	0.45018393E 02		
A	0.66087178E 04	P	0.65172561E 04	AXIS	0.65629869E 04	RADIUS	0.63720200E 04	TIME	0.29701240E 01
ADBT	-0.55973225E 02	PDBT	-0.14833832E 02	AXIDBT	-0.35403528E 02	2RBIT	0.48174605E 02		
A	0.65987178E 04	P	0.65145827E 04	AXIS	0.65566503E 04	RADIUS	0.63720719E 04	TIME	0.31349111E 01
ADBT	-0.66103096E 02	PDBT	-0.17819200E 02	AXIDBT	-0.41961148E 02	2RBIT	0.50864267E 02		
A	0.65887178E 04	P	0.65118655E 04	AXIS	0.65502916E 04	RADIUS	0.63721281E 04	TIME	0.32734323E 01
ADBT	-0.79264738E 02	PDBT	-0.21702515E 02	AXIDBT	-0.50483626E 02	2RBIT	0.53137720E 02		
A	0.65787178E 04	P	0.65091074E 04	AXIS	0.65439127E 04	RADIUS	0.63721834E 04	TIME	0.33880452E 01
ADBT	-0.96654691E 02	PDBT	-0.26856437E 02	AXIDBT	-0.61755563E 02	2RBIT	0.55017389E 02		
A	0.65687178E 04	P	0.65063073E 04	AXIS	0.65375125E 04	RADIUS	0.63722347E 04	TIME	0.34811621E 01
ADBT	-0.12024515E 03	PDBT	-0.33940001E 02	AXIDBT	-0.77092577E 02	2RBIT	0.56546763E 02		
A	0.65487178E 04	P	0.65005544E 04	AXIS	0.65246361E 04	RADIUS	0.63723277E 04	TIME	0.36124563E 01
ADBT	-0.20129740E 03	PDBT	-0.59263927E 02	AXIDBT	-0.13028070E 03	2RBIT	0.58709557E 02		
A	0.65287178E 04	P	0.64944185E 04	AXIS	0.65115681E 04	RADIUS	0.63723896E 04	TIME	0.36858271E 01
ADBT	-0.39824621E 03	PDBT	-0.12856697E 03	AXIDBT	-0.26340659E 03	2RBIT	0.59921826E 02		
A	0.65087178E 04	P	0.64875169E 04	AXIS	0.64981174E 04	RADIUS	0.63724229E 04	TIME	0.37184814E 01
ADBT	-0.11186879E 04	PDBT	-0.41531130E 03	AXIDBT	-0.76697963E 03	2RBIT	0.60463034E 02		
A	0.64887178E 04	P	0.64790406E 04	AXIS	0.64833792E 04	RADIUS	0.63724351E 04	TIME	0.37272170E 01
ADBT	-0.70584279E 04	PDBT	-0.36614551E 04	AXIDBT	-0.53599416E 04	2RBIT	0.60608292E 02		
A	0.64687178E 04	P	0.64654747E 04	AXIS	0.64670962E 04	RADIUS	0.63724370E 04	TIME	0.37282259E 01
ADBT	-0.13953651E 06	PDBT	-0.11068825E 06	AXIDBT	-0.12511238E 06	2RBIT	0.60625134E 02		
A	0.64487178E 04	P	0.64478009E 04	AXIS	0.64482034E 04	RADIUS	0.63724373E 04	TIME	0.37282673E 01
ADBT	-0.34856556E 07	PDBT	-0.32746715E 07	AXIDBT	-0.33301066E 07	2RBIT	0.60625028E 02		

SECTION IV: GRAPHIC METHOD FOR LIFETIME PREDICTION

A lifetime model has been presented for making reasonably accurate predictions of orbital lifetime. Primary factors influencing earth orbital satellite lifetimes have been included. A method has been devised to provide a means of graphically predicting lifetime based on this model. This graphic technique allows a quick prediction of lifetime independent of computer runs.

Two sets of normalized lifetime curves have been generated, one using the 1959 ARDC density model as the basic reference and the other using the 1962 U. S. Standard atmospheric density model. These sets are presented in Figures 8, 9, and 10 for 1959 ARDC and 11, 12, and 13 for the 1962 U. S. Standard. Figures 9, 10, 12, and 13 are blown up altitude regions of Figures 8 and 11. A mean diurnal bulge and constant values of one (1) for vehicle mass, area and drag coefficients are assumed. The normalized lifetime read from these charts is L_1 . For both references the formula for computing lifetime is then:

$$\text{Lifetime} = L_1 \left[\frac{m}{C_D A} \right] (f_i, \omega) (f_d)$$

where

L_1 = normalized lifetime which is a function of apogee and perigee altitudes

m = orbiting mass in kg

C_D = orbital drag coefficient

A = effective drag area in square meters

f_i, ω = correction factor to the normalized reference for initial orbital inclination and argument of perigee. The normalized reference assumes values of

$$i = 30^\circ \quad \omega = 180^\circ$$

f_d = correction factor to the normalized reference for the actual calendar dates the satellite is in orbit and the initial perigee altitude. This correction is required to account for the variation of density with

solar and geomagnetic activity which varies with time. The value of f_d for future years is based upon current predictions of these effects.

The step-wise procedure to be followed in predicting lifetime is as follows:

1. Compute perigee and apogee altitudes in km. Use the earth radius defined at the sub perigee point in computing altitude (see Table 2). If the i and ω necessary to define this radius are not known, use the equatorial earth radius of 6378.165 km in computing altitude.

2. For the specified perigee altitude read the L_1 corresponding to the given apogee altitude, interpolating between lines of constant apogee altitude if required. Depending on altitude region of interest use Figures 8, 9, or 10 for ARDC reference and Figures 11, 12, or 13 for 1962 U. S. Standard.

3. Compute A, effective area. For attitude stabilized vehicles this area is the surface projection on a plane perpendicular to the direction of vehicle motion. Projected areas are computed as follows:

Nose-on ($\alpha = 0^\circ$)

Broadside ($\alpha = 90^\circ$)

$$\text{Cone } A = \frac{\pi D^2}{4}$$

$$A = DL/2$$

$$\text{Cylinder } A = \frac{\pi D^2}{4}$$

$$A = DL$$

A = projected area (m^2)

D = vehicle diameter (m)

L = vehicle length (m)

α = angle of attack

For random tumbling bodies A is computed as one-fourth the total surface area.

4. Determine drag coefficient, C_D , from Figure 14. These data are extracted from Reference 8. The following values are for a 200 km altitude:

Cone, nose-on = 2.06

Cylinder broadside = 2.2

Tumbling Body = 2.18

5. Compute the ratio $M/C_D A$ in $\frac{\text{kg}}{\text{m}^2}$

6. To obtain total lifetime in days based on 1959 ARDC or 1962 U. S. Standard reference, multiply $M/C_D A$ by the value read from the graph to obtain L_2 . ($i = 30^\circ$, $\omega = 180^\circ$)

$$L_2 = L_1 M/C_D A$$

If something more than the apogee and perigee values are known about the orbit or a prediction for later launch dates is desired, using the 1959 ARDC or 1962 U. S. Standard predictions computed in step 6 continue with the following steps.

7. For given values of i and ω read $f(i, \omega)$ in Figure 15, interpolating between lines of constant inclination if necessary. Note that the figure consists of two sets of curves, one for use when $L_2 < 30$ days and the other for use when $L_2 \geq 30$ days. Multiply L_2 by $f(i, \omega)$ to obtain L_3 .

$$L_3 = L_2 f(i, \omega)$$

L_3 is then lifetime in days for proper inclination and argument of perigee. Omit this step if i and ω are not defined and the mean radius was used in step 1.

8. For the given launch date and perigee altitude enter Figure 16 or Figure 17 for the 1959 or 1962 atmospheres respectively and obtain an average value of the ordinate for the given perigee altitude over the interval of time from the launch date (year and fraction) over the time (in years) corresponding to L_3 days. The same lifetime will be obtained regardless of which base is used. This average is f_d which is multiplied by L_3 to obtain the first lifetime estimate $L_3(1)$.

$$L_3(1) = L_3 f_d$$

These f_d correction factors are current only for the date of this publication. As new data become available and the solar activity prediction is updated, this f_d factor must be updated.

9. Step 8 is repeated using $L_3(1)$ instead of L_3 to perform the average. However, when the new value of f_d is obtained it is multiplied by L_3 not $L_3(1)$ to obtain $L_3(2)$.

$$L_3(2) = L_3 f_d$$

Depending upon the accuracy desired and the variations in successive values of f_d , step 8 may be repeated until $L_3(n)$ is obtained which differs insignificantly from $L_3(n-1)$.

Primary uncertainties associated with these predictions are a 25% uncertainty in C_D and uncertainty in prediction of f_d . The latter is a function of time and altitude. To obtain three sigma lifetime values for f_d uncertainty, Figures 18 and 19 or 20 and 21 should be used for the 1959 or 1962 atmospheres respectively in the same manner as given in step 8 for Figures 16 and 17 and nominal lifetime. Three sigma curves are given only for future dates as there is no prediction uncertainty associated with past solar activity behavior.

To assess the accuracy of the graphic technique, a total of 103 comparisons was made between lifetimes predicted using the computer deck and lifetimes predicted using the graphic technique. It was found that a maximum of three iterations as specified in step 9 was sufficient for convergence. For short lifetimes only one iteration was necessary. The ratio of the program value and the graphic value was computed for all cases. The results of this yielded a mean and standard deviation of 1.01 and .15 respectively. From the results of this comparison no systematic errors seemed to be present in the graphic technique.

As well as total lifetime, time spent in decaying from one circular altitude to another can also be obtained by subtracting the respective lifetime values. For elliptical orbits, the time spent in decaying from one apogee to another can be found in a like manner if the perigee could be assumed fixed. However, this assumption could cause a significant error since the perigee will in actuality experience a decay whose effect cannot be neglected.

TABLE II. EARTH RADIUS AS A FUNCTION OF INCLINATION (i)
AND ARGUMENT OF PERIGEE (ω)

i \ ω							
	0	15	30	45	60	75	90
	180	165	150	135	120	105	
	360	195	210	225	240	255	270
		345	330	315	300	285	
15	6378.2	6378.1	6377.9	6377.5	6377.1	6376.8	6376.7
30	6378.2	6377.9	6376.9	6375.5	6374.2	6373.2	6372.8
45	6378.2	6377.5	6375.5	6372.8	6370.2	6368.2	6367.5
60	6378.2	6377.1	6374.2	6370.2	6366.1	6363.3	6362.1
75	6378.2	6376.8	6373.2	6368.2	6363.3	6359.6	6358.2
90	6378.2	6376.7	6372.8	6367.5	6362.1	6358.2	6356.8

Computed from

$$R_E = 6378.165 \left[1 - \frac{1}{298.3} (\sin^2 i \sin^2 \omega) \right]$$

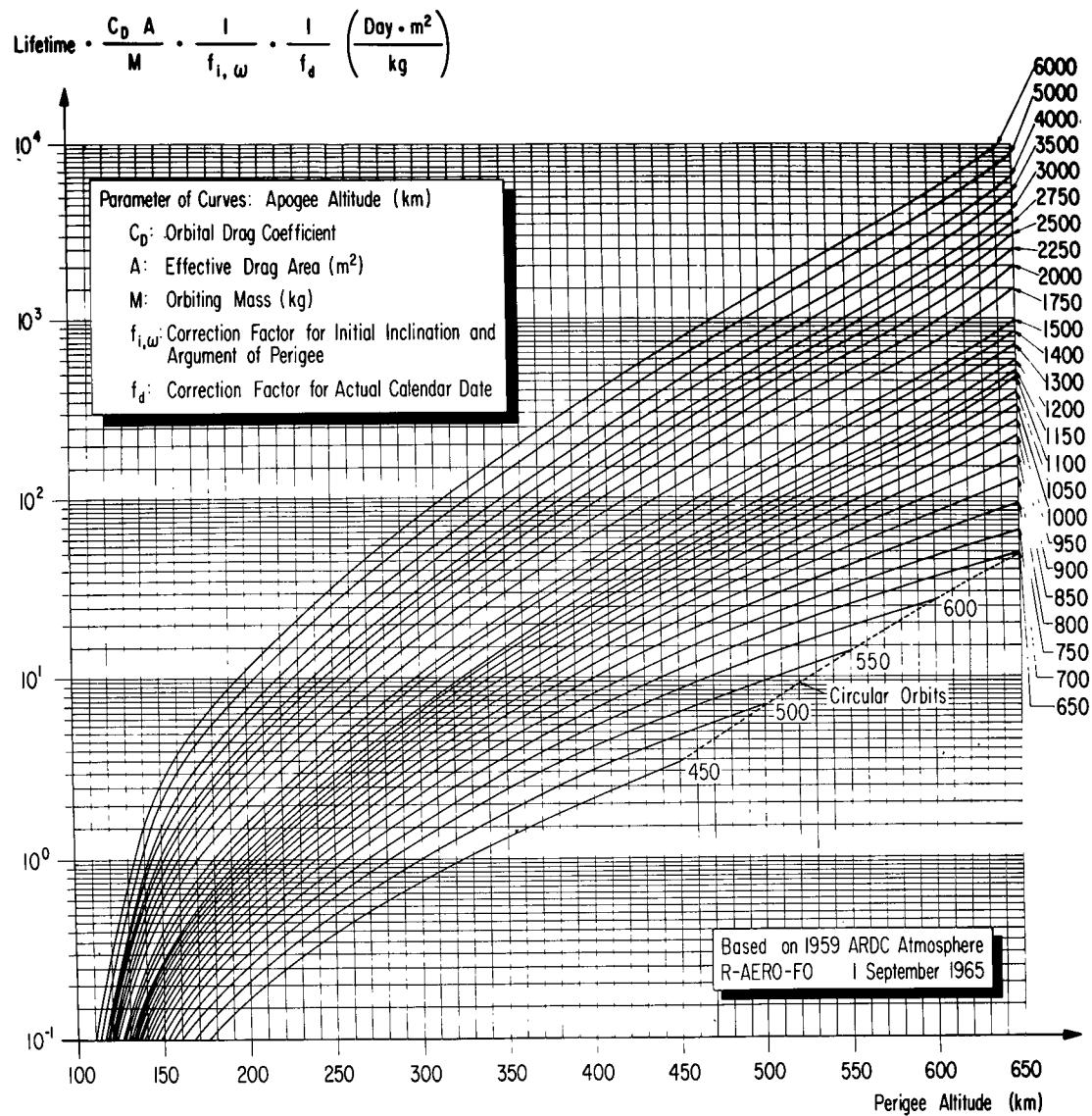


FIGURE 8. EARTH ORBITAL LIFETIME

Perigee: 100 - 650 km

Apogee: 450 - 600 km

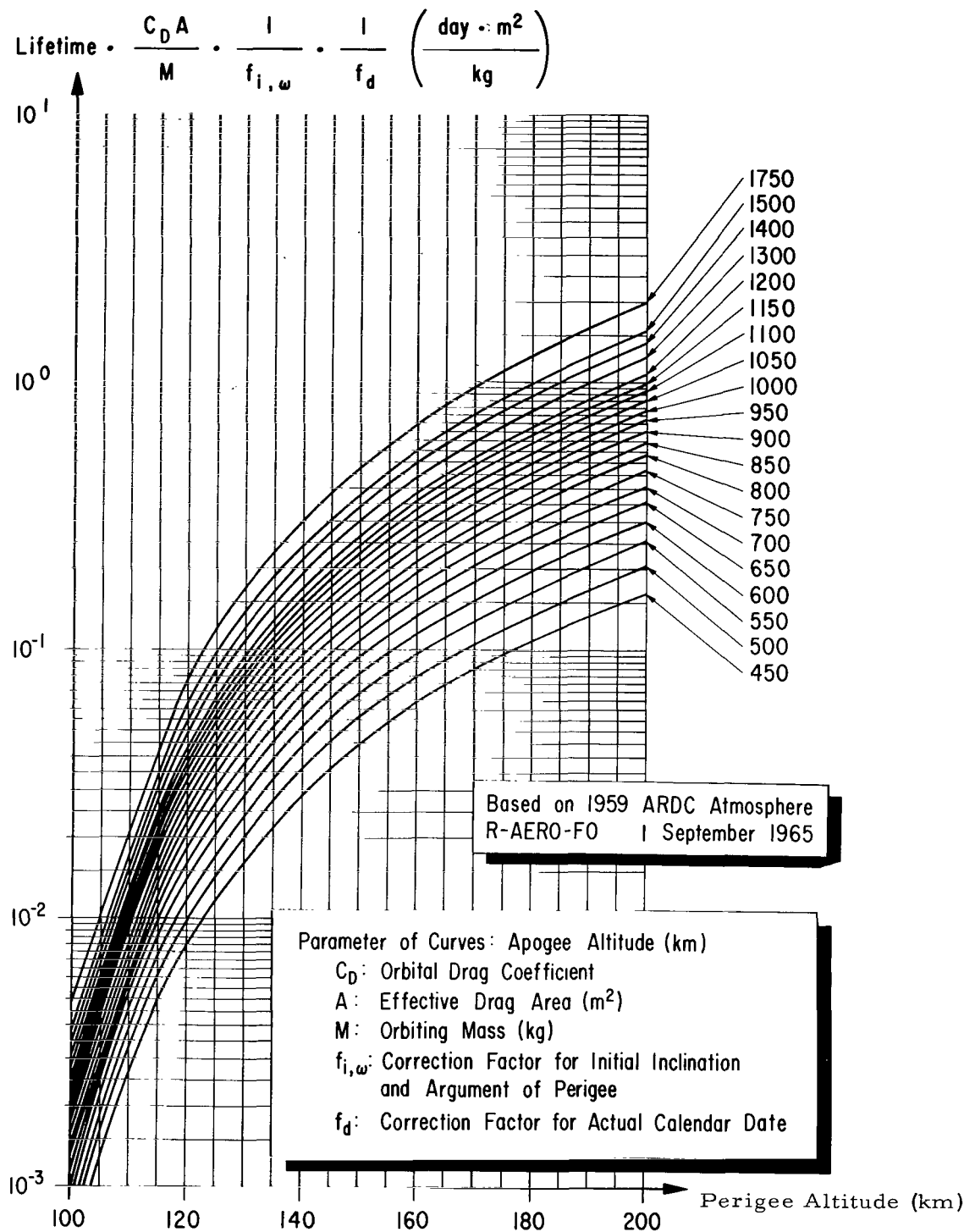


FIGURE 9. EARTH ORBITAL LIFETIME

Perigee: 100 - 200 km

Apogee: 450 - 1750 km

$$\text{Lifetime} \cdot \frac{C_D A}{M} \cdot \frac{1}{f_{i,\omega}} \cdot \frac{1}{f_d} \cdot \left(\frac{\text{day} \cdot \text{m}^2}{\text{kg}} \right)$$

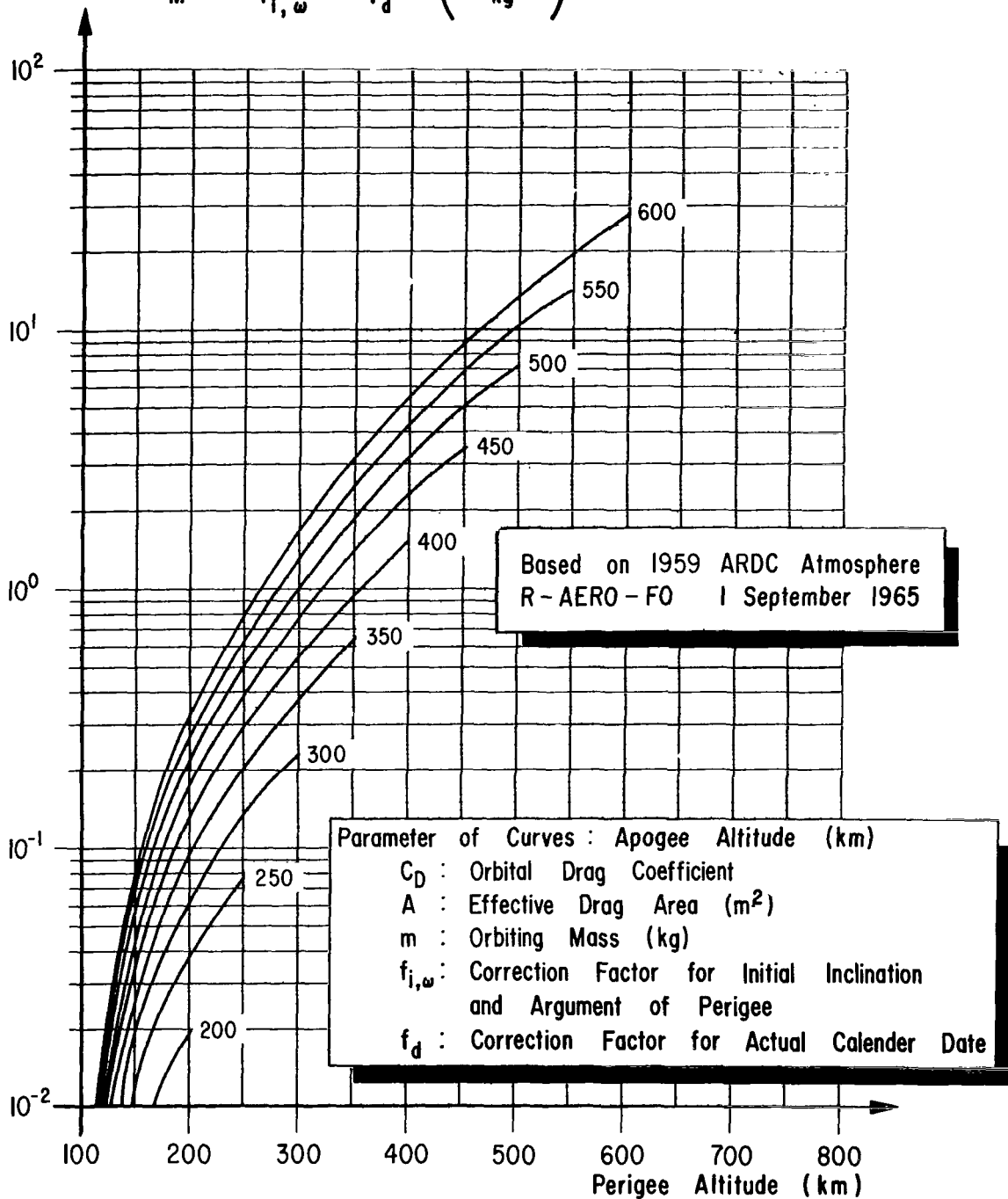


FIGURE 10. EARTH ORBITAL LIFETIME

Perigee: 100 - 600 km

Apogee: 200 - 600 km

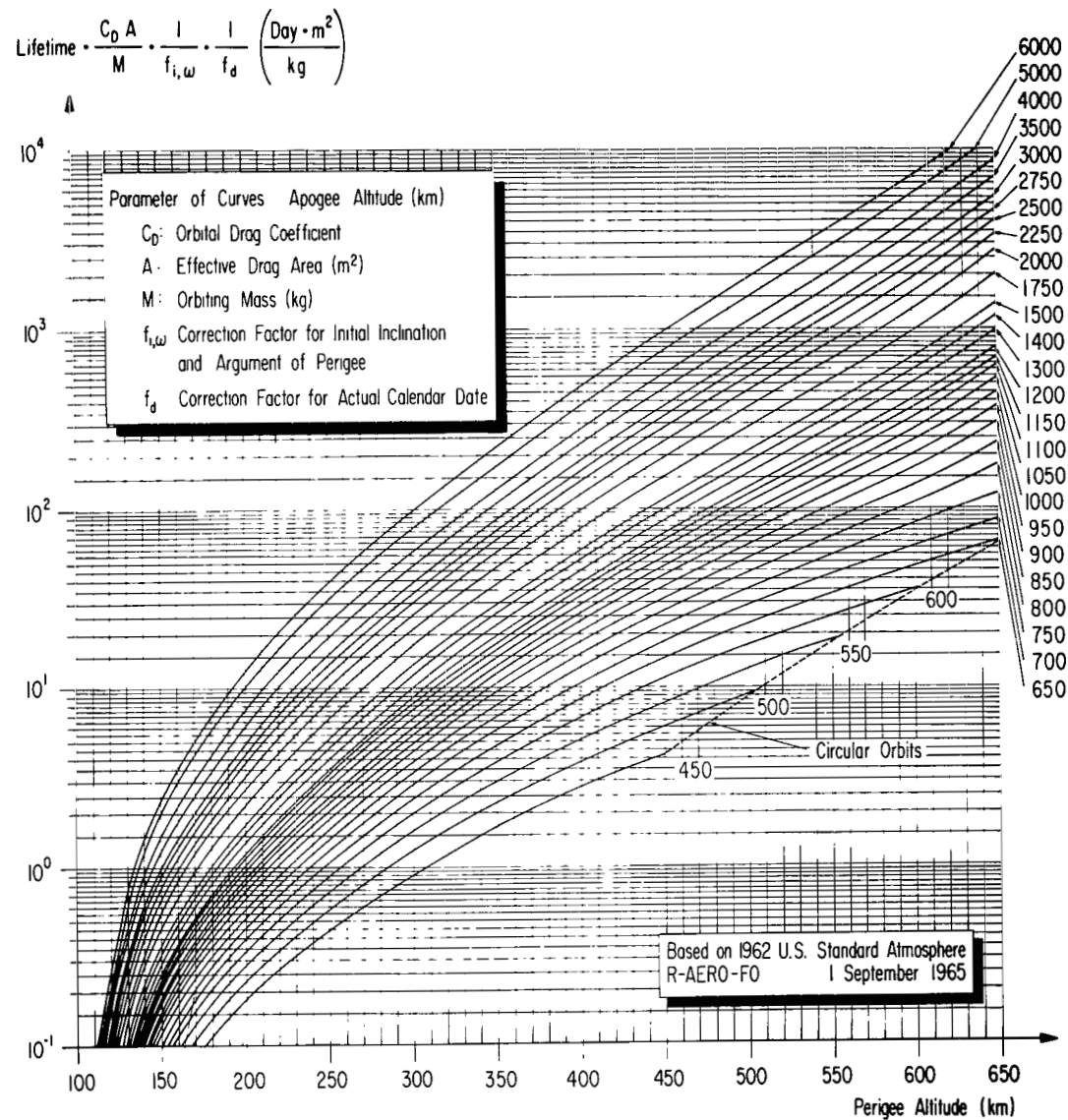


FIGURE 11. EARTH ORBITAL LIFETIME

Perigee: 100 - 650 km

Apogee: 450 - 6000 km

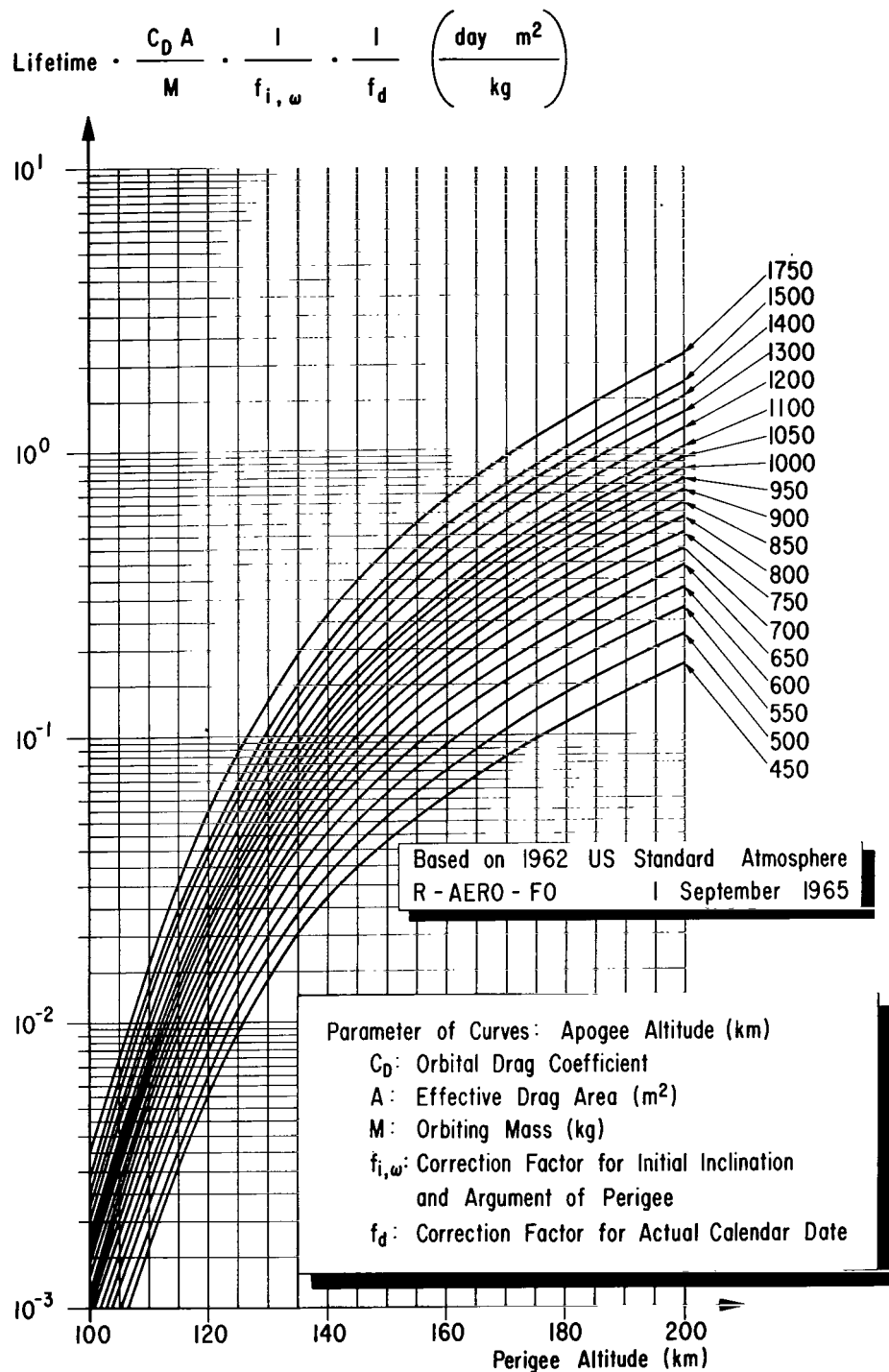


FIGURE 12. EARTH ORBITAL LIFETIME
 Perigee: 100 - 200 km
 Apogee: 450 - 1750 km

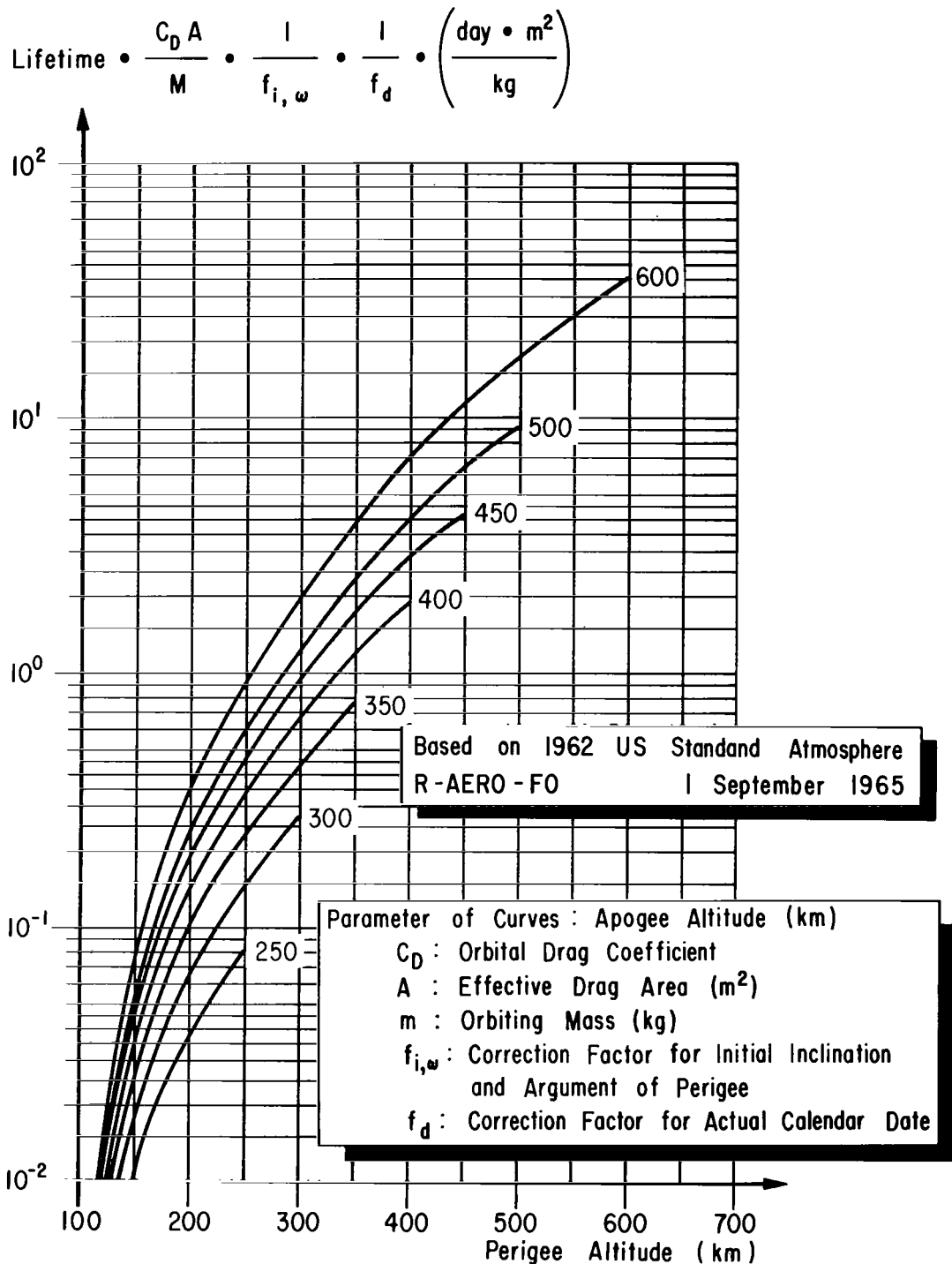


FIGURE 13. EARTH ORBITAL LIFETIME
 Perigee: 100 - 600 km
 Apogee: 250 - 600 km

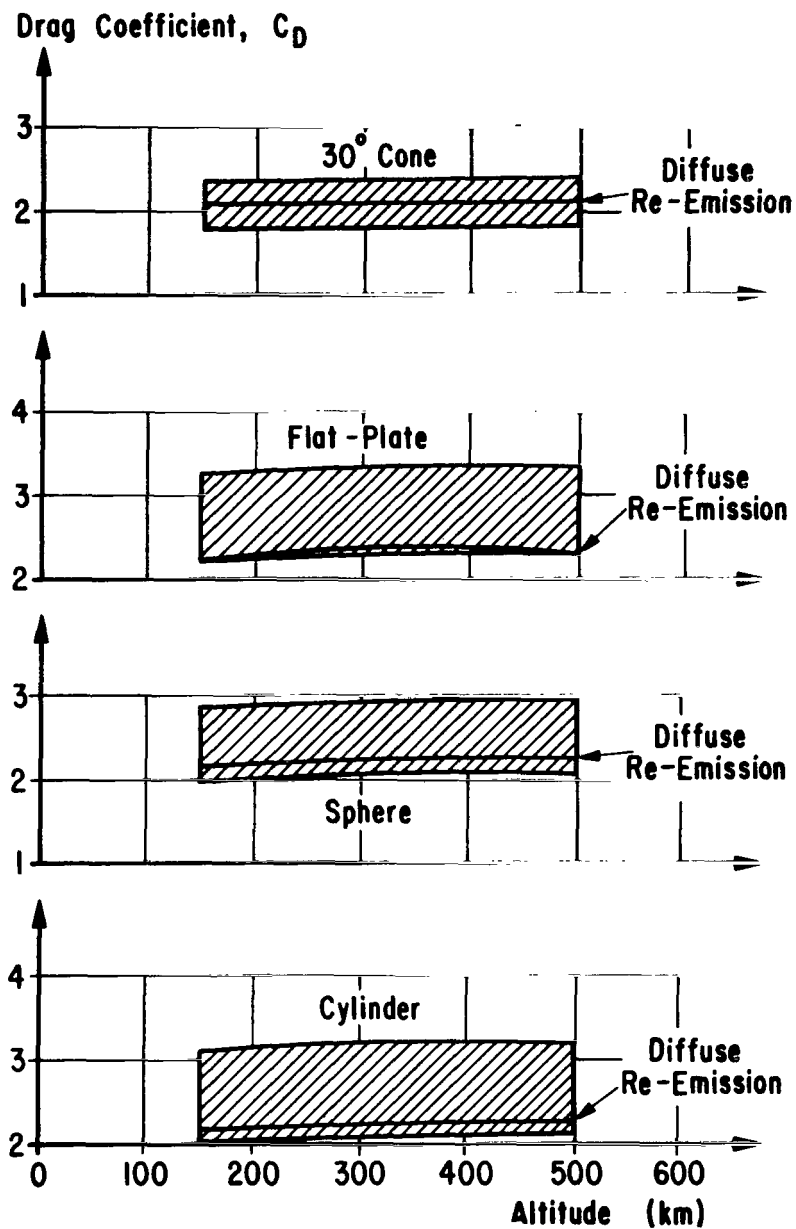


FIGURE 14. ORBITAL DRAG COEFFICIENT

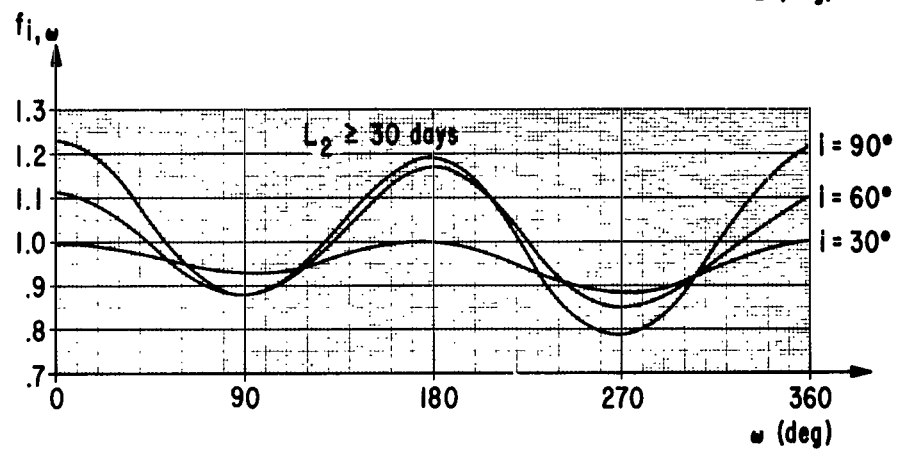
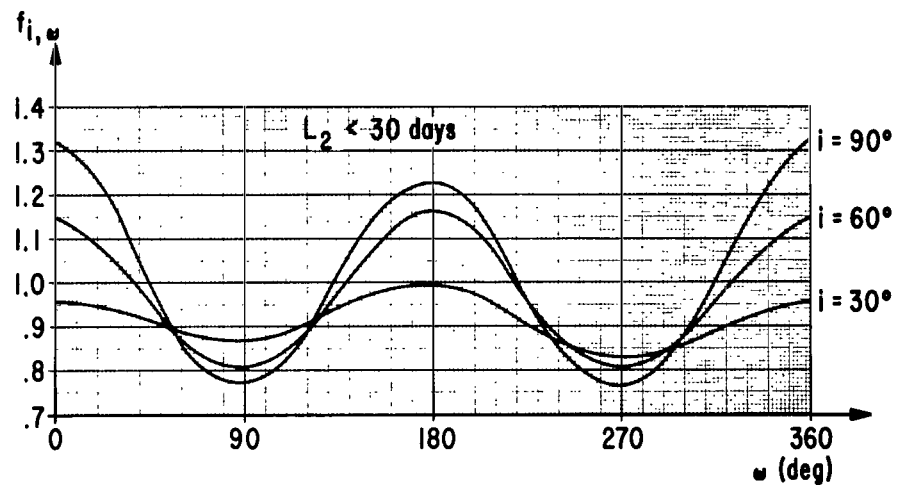


FIGURE 15. $f_{i, \omega}$ CORRECTION FACTOR

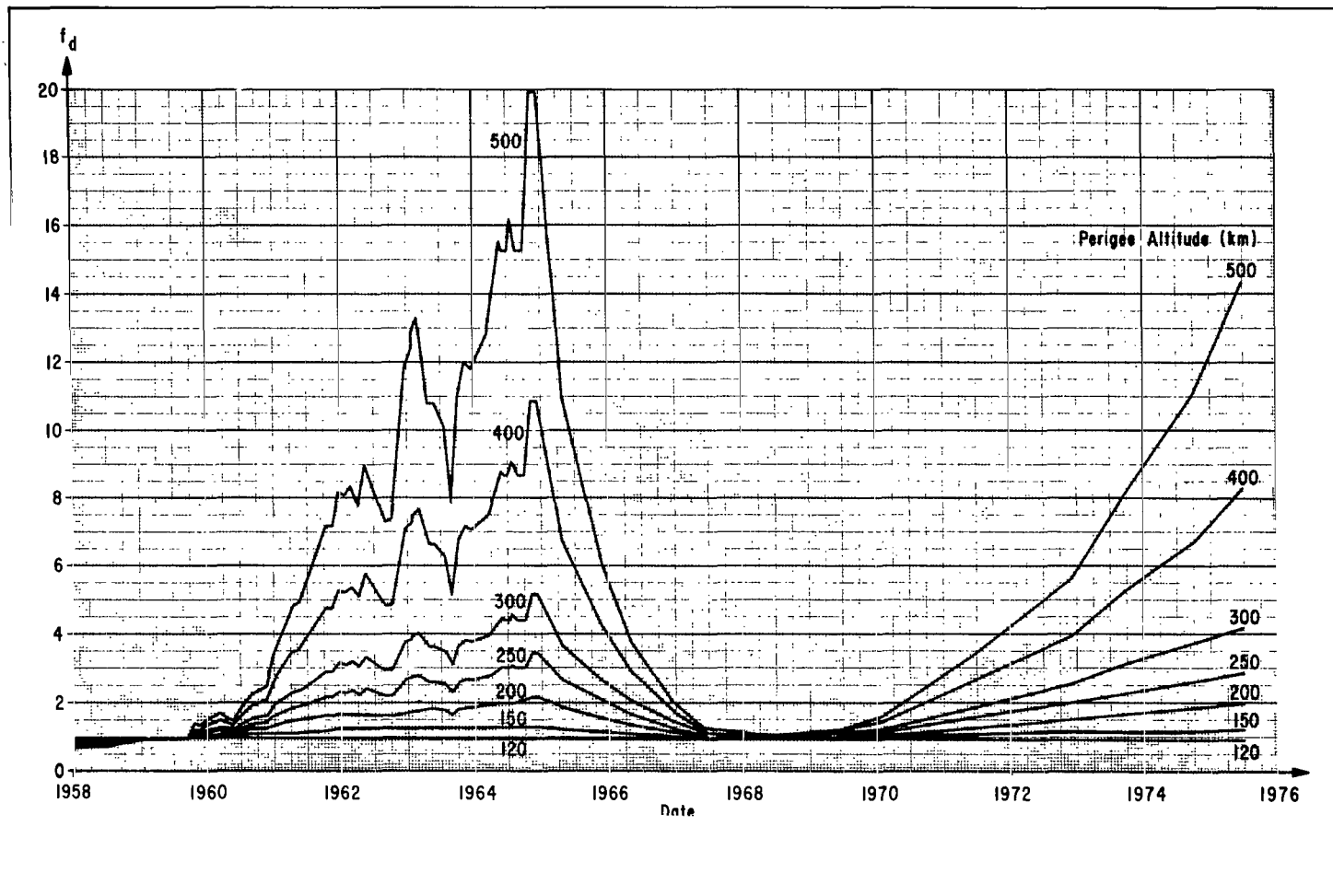


FIGURE 16. f_d CORRECTION FACTOR FOR NOMINAL LIFETIME: 1959 ARDC REFERENCE

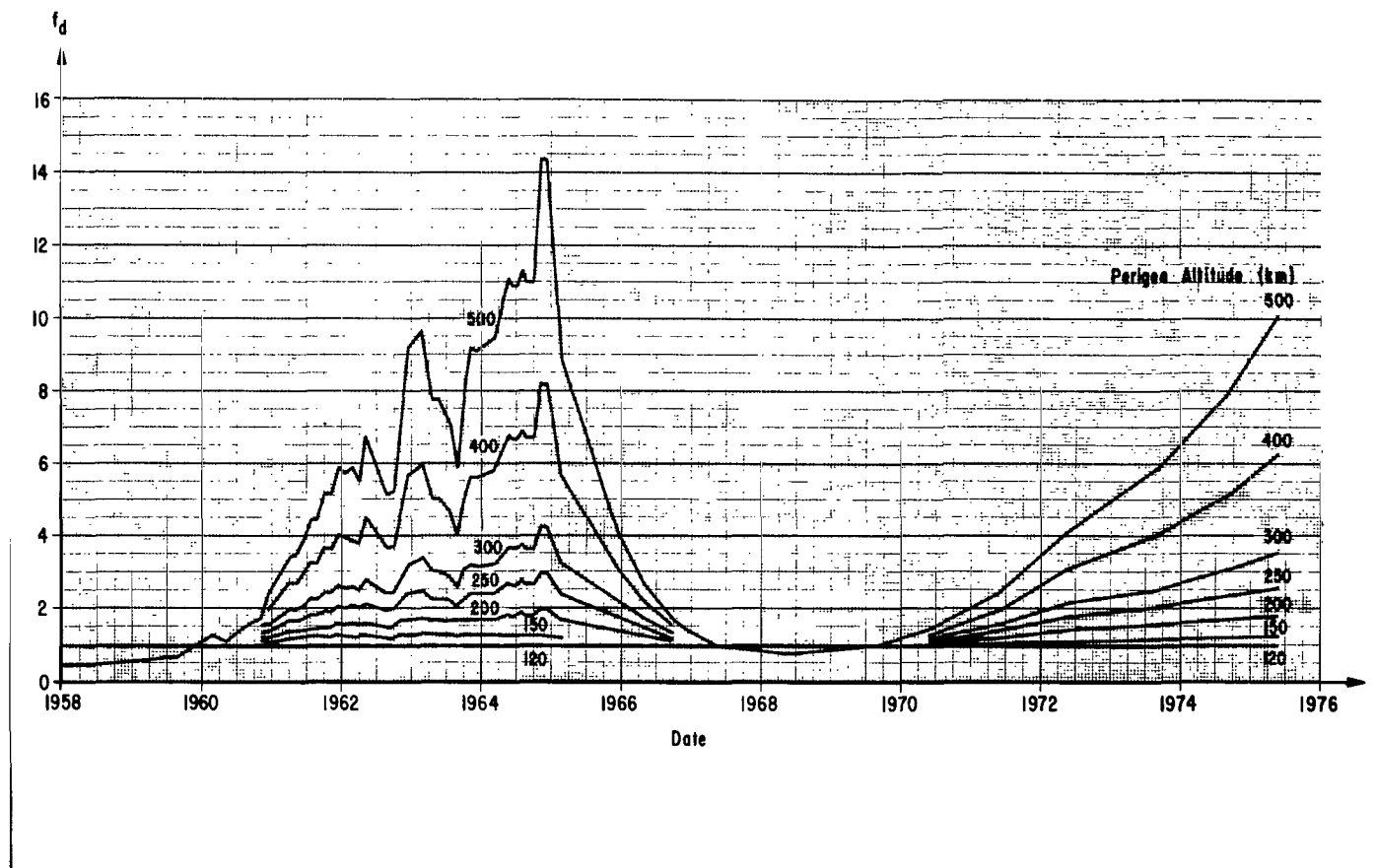


FIGURE 17. f_d CORRECTION FACTOR FOR NOMINAL LIFETIME: 1962 U. S. STANDARD REFERENCE

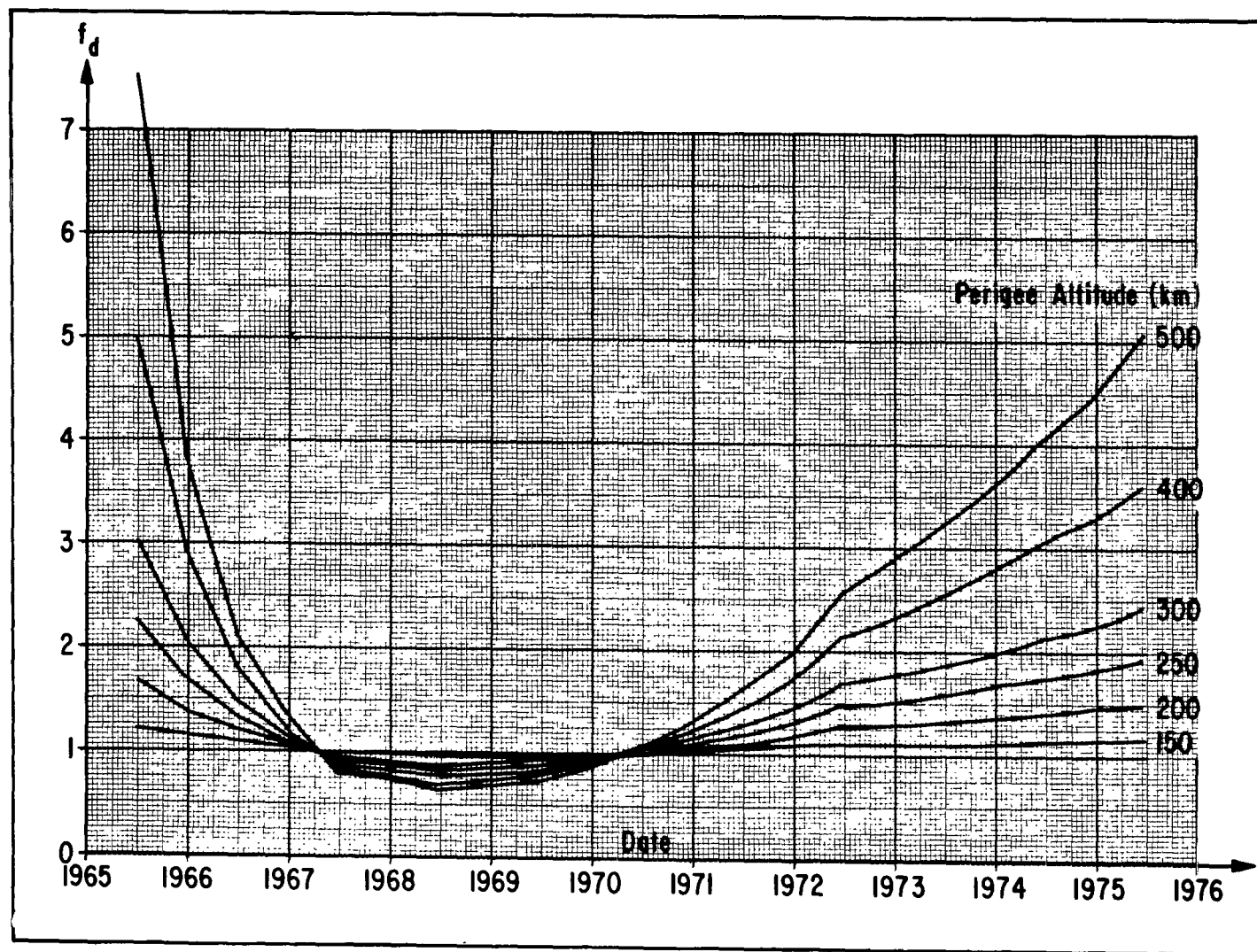


FIGURE 18. f_d CORRECTION FACTOR FOR -3σ LIFETIME: 1959 ARDC REFERENCE

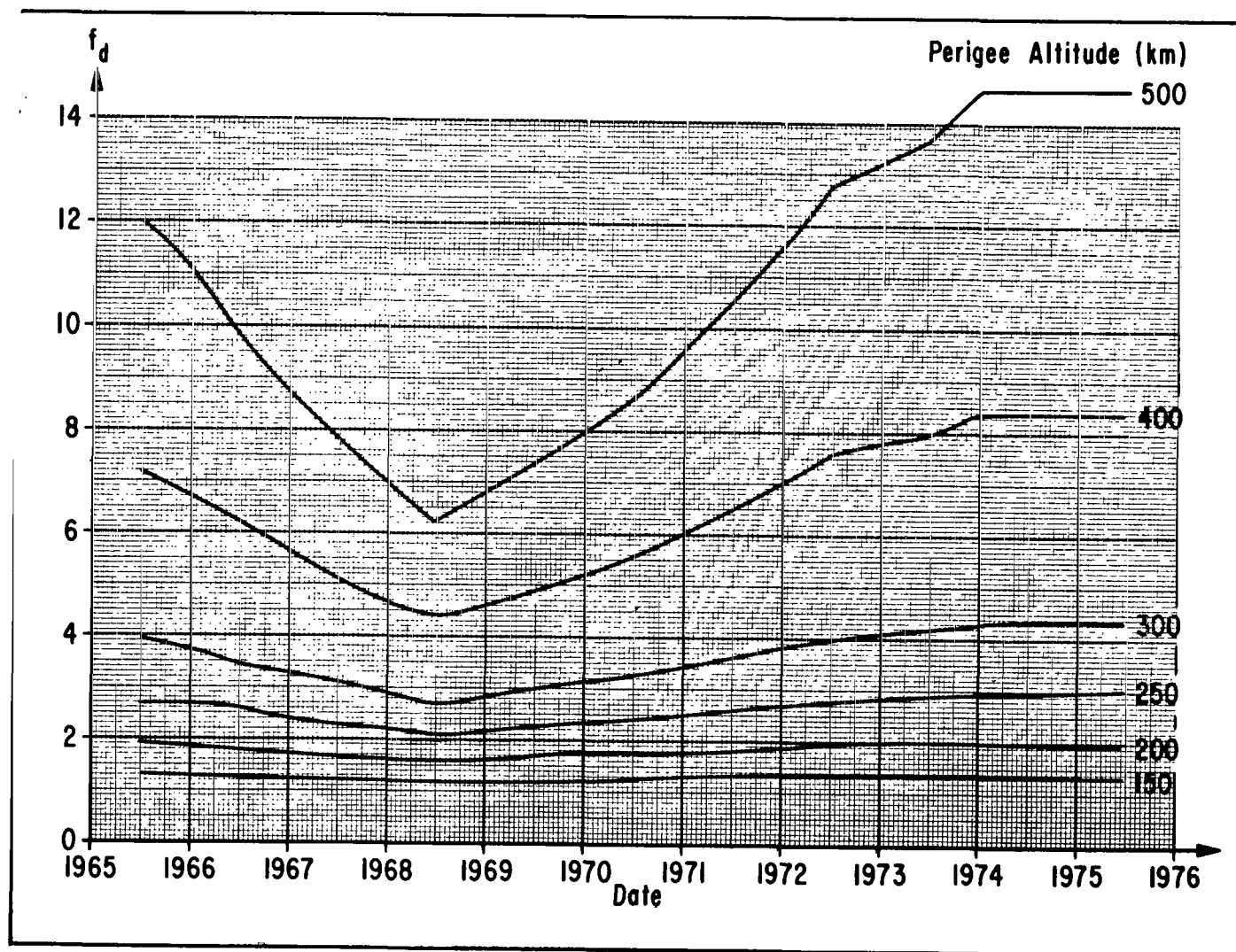


FIGURE 19. f_d CORRECTION FACTOR FOR $+3\sigma$ LIFETIME: 1959 ARDC REFERENCE

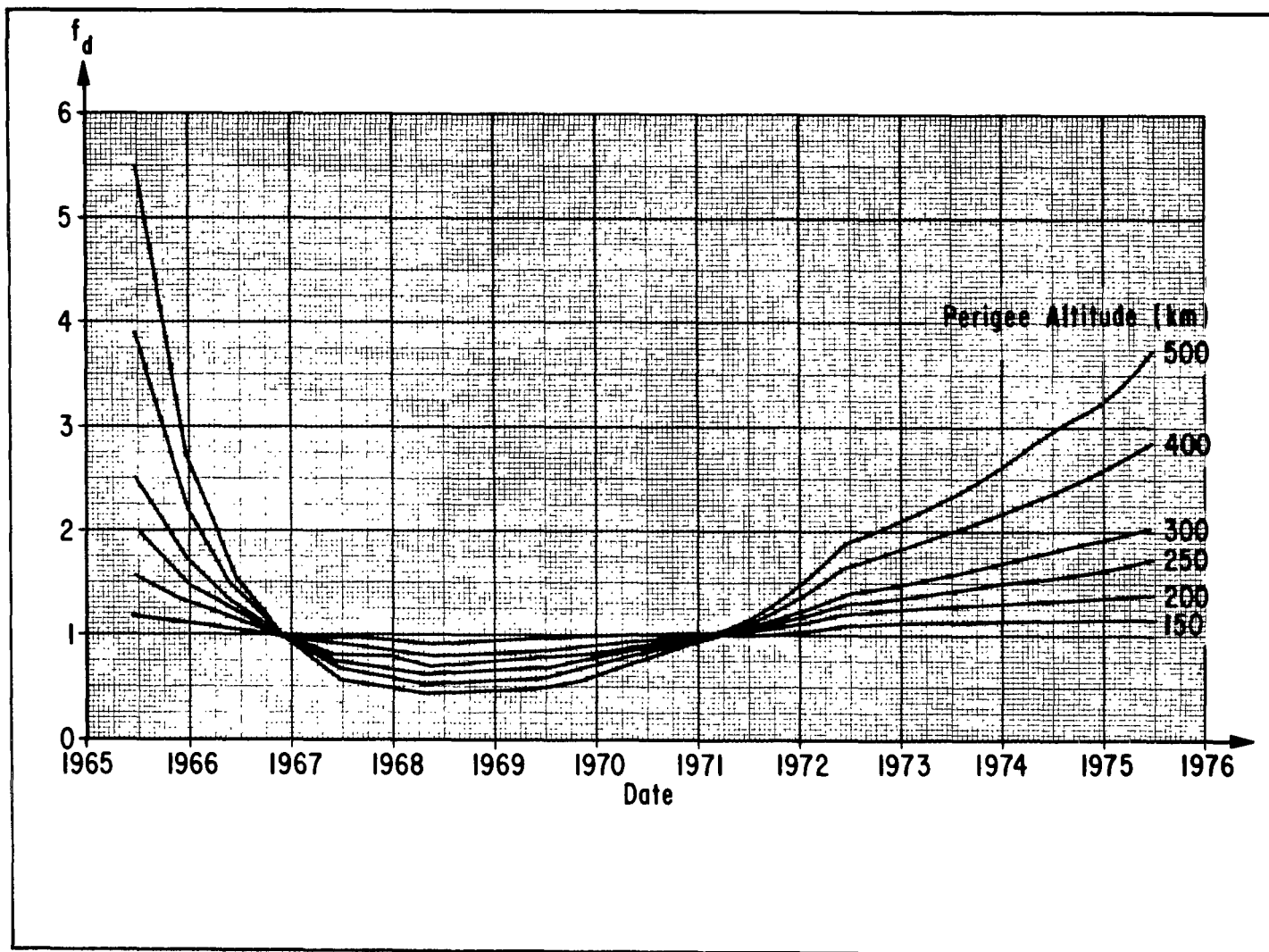


FIGURE 20. f_d CORRECTION FACTOR FOR -3σ LIFETIME: 1962 U. S. STANDARD REFERENCE

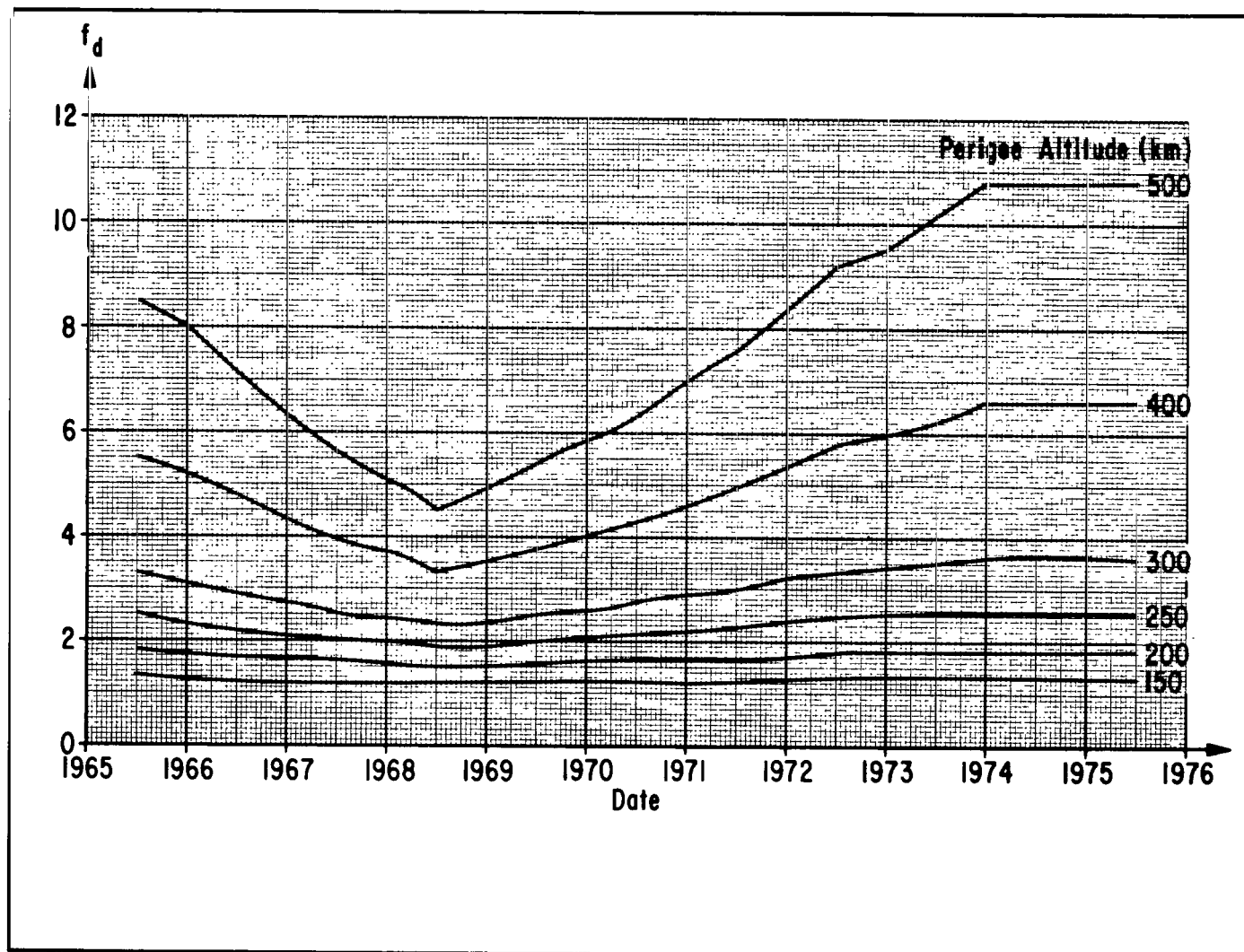
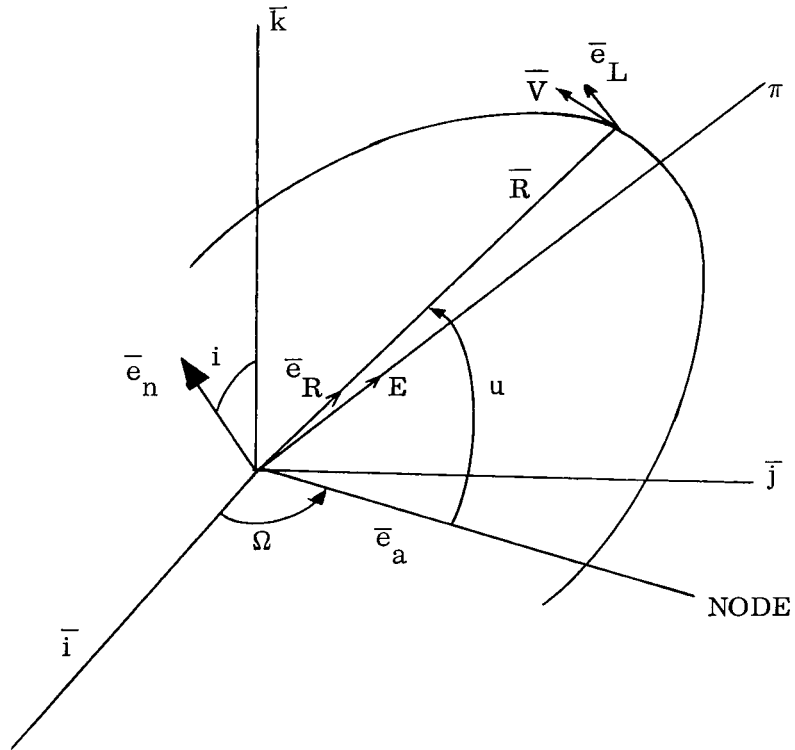


FIGURE 21. f_d CORRECTION FACTOR FOR $+3\sigma$ LIFETIME: 1962 U. S. STANDARD REFERENCE

APPENDIX A. DERIVATION OF THE DECAY EQUATIONS

$$\frac{d\lambda}{dt} = f(\lambda) \cdot \bar{\mathcal{F}}$$

A. Definitions



From the above geometry:

$$\cos i = \bar{e}_h \cdot \bar{k}$$

$$\bar{e}_R = \bar{e}_L \times \bar{e}_h$$

$$\cos \Omega = \bar{e}_\Omega \cdot \bar{i}$$

$$\begin{aligned}
\cos u &= \bar{\mathbf{e}}_{\Omega} \cdot \bar{\mathbf{e}}_{\mathbf{R}} \\
\sin \Omega &= \bar{\mathbf{e}}_{\Omega} \cdot \bar{\mathbf{j}} \\
\sin u &= \bar{\mathbf{e}}_{\Omega} \times \bar{\mathbf{e}}_{\mathbf{R}} \cdot \bar{\mathbf{e}}_{\mathbf{h}} \\
\bar{\mathbf{e}}_{\Omega} &= \frac{\bar{\mathbf{k}} \times \bar{\mathbf{e}}_{\mathbf{h}}}{\sin i} = \frac{\bar{\mathbf{k}} \times \bar{\mathbf{h}}}{h \sin i} \\
\bar{\mathbf{e}}_{\mathbf{R}} &= \frac{\bar{\mathbf{R}}}{R} \\
\bar{\mathbf{e}}_{\mathbf{h}} &= \frac{\bar{\mathbf{R}} \times \bar{\mathbf{V}}}{|\bar{\mathbf{R}} \times \bar{\mathbf{V}}|}
\end{aligned}
\quad
\begin{aligned}
\begin{pmatrix} \bar{\mathbf{e}}_{\mathbf{R}} \\ \bar{\mathbf{e}}_{\mathbf{L}} \\ \bar{\mathbf{e}}_{\mathbf{h}} \end{pmatrix} &= \mathbf{M} \begin{pmatrix} \bar{\mathbf{i}} \\ \bar{\mathbf{j}} \\ \bar{\mathbf{k}} \end{pmatrix} \\
\begin{pmatrix} \bar{\mathbf{i}} \\ \bar{\mathbf{j}} \\ \bar{\mathbf{k}} \end{pmatrix} &= \mathbf{M}^T \begin{pmatrix} \bar{\mathbf{e}}_{\mathbf{R}} \\ \bar{\mathbf{e}}_{\mathbf{L}} \\ \bar{\mathbf{e}}_{\mathbf{h}} \end{pmatrix}
\end{aligned}$$

The transformation matrix \mathbf{M} is given by

$$\mathbf{M} = \begin{pmatrix} \cos u \cos \Omega - \sin u \cos i \sin \Omega & \cos u \sin \Omega + \sin u \cos i \cos \Omega & \sin u \sin i \\ -\sin u \cos \Omega - \cos u \cos i \sin \Omega & -\sin u \sin \Omega + \cos u \cos i \cos \Omega & \cos u \sin i \\ \sin i \sin \Omega & -\sin i \cos \Omega & \cos i \end{pmatrix}$$

$$\bar{\mathbf{h}} \equiv \bar{\mathbf{R}} \times \bar{\mathbf{V}}$$

$$h \equiv R^2 \frac{d\theta}{dt}$$

$$\bar{\mathbf{e}} \equiv \frac{\bar{\mathbf{V}} \times (\bar{\mathbf{R}} \times \bar{\mathbf{V}})}{\mu} - \bar{\mathbf{e}}_{\mathbf{R}}$$

$$e = |\bar{\mathbf{e}}|$$

$$\sin \omega = \frac{(\bar{\mathbf{e}}_{\Omega} \times \bar{\mathbf{e}}) \cdot \bar{\mathbf{e}}_{\mathbf{h}}}{e}$$

$$\cos \omega = \frac{\bar{\mathbf{e}}_{\Omega} \cdot \bar{\mathbf{e}}}{e}$$

$$A = e \cos \omega = \bar{\mathbf{e}}_{\Omega} \cdot \bar{\mathbf{e}}$$

$$B = e \sin \omega = \bar{\mathbf{e}}_{\Omega} \times \bar{\mathbf{e}} \cdot \bar{\mathbf{e}}_h$$

$$p = \frac{\bar{\mathbf{h}} \cdot \bar{\mathbf{h}}}{\mu} = \frac{h^2}{\mu}$$

$$\bar{\mathbf{R}} = \frac{p \bar{\mathbf{e}}_R}{1 + e \cos (u - \omega)}$$

$$\bar{\mathbf{V}} = \sqrt{\frac{\mu}{p}} \{ [1 + e \cos (u - \omega)] \bar{\mathbf{e}}_R + e \sin (u - \omega) \bar{\mathbf{e}}_L \}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} \mathbf{R} \cdot \bar{\mathbf{i}} \\ \mathbf{R} \cdot \bar{\mathbf{j}} \\ \mathbf{R} \cdot \bar{\mathbf{k}} \end{pmatrix} = \frac{p}{1 + \cos \theta} \begin{pmatrix} \bar{\mathbf{e}}_R \cdot \bar{\mathbf{i}} \\ \bar{\mathbf{e}}_R \cdot \bar{\mathbf{j}} \\ \bar{\mathbf{e}}_R \cdot \bar{\mathbf{k}} \end{pmatrix} \quad \theta = u - \omega$$

$$\psi \equiv 1 + e \cos \theta \equiv 1 + A \cos u + B \sin u$$

$$\begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{z} \end{pmatrix} = \begin{pmatrix} \bar{\mathbf{V}} \cdot \bar{\mathbf{i}} \\ \bar{\mathbf{V}} \cdot \bar{\mathbf{j}} \\ \bar{\mathbf{V}} \cdot \bar{\mathbf{k}} \end{pmatrix} = \sqrt{\frac{\mu}{p}} \left\{ [1 + e \cos \theta] \begin{pmatrix} \bar{\mathbf{e}}_L \cdot \bar{\mathbf{i}} \\ \bar{\mathbf{e}}_L \cdot \bar{\mathbf{j}} \\ \bar{\mathbf{e}}_L \cdot \bar{\mathbf{k}} \end{pmatrix} + e \sin \theta \begin{pmatrix} \bar{\mathbf{e}}_R \cdot \bar{\mathbf{i}} \\ \bar{\mathbf{e}}_R \cdot \bar{\mathbf{j}} \\ \bar{\mathbf{e}}_R \cdot \bar{\mathbf{k}} \end{pmatrix} \right\}$$

Consider now $\bar{\mathbf{R}}$ to be "radius" and $\bar{\mathbf{V}}$ to be "velocity." In Newtonian motion the two are related to some "force" $\bar{\mathbf{F}}$ as follows:

$$\bar{\mathbf{V}} = \frac{d\bar{\mathbf{R}}}{dt}$$

or in alternate form:

$$\frac{d\bar{\mathbf{V}}}{dt} = \frac{\bar{\mathbf{F}}}{M} \quad \text{or} \quad \frac{d\bar{\mathbf{V}}}{dt} = \frac{-\mu\bar{\mathbf{R}}}{R^3} + \bar{\mathcal{F}}$$

Since the definitions express the orbital elements most directly as functions of $\bar{\mathbf{h}}$ and $\bar{\mathbf{e}}$, their derivatives are facilitated with expressions for $\frac{d\bar{\mathbf{h}}}{dt}$ and $\frac{d\bar{\mathbf{e}}}{dt}$.

$$\begin{aligned} \frac{d\bar{\mathbf{h}}}{dt} &= \frac{d}{dt} (\bar{\mathbf{R}} \times \bar{\mathbf{V}}) = \frac{d\bar{\mathbf{R}}}{dt} \times \bar{\mathbf{V}} + \bar{\mathbf{R}} \times \frac{d\bar{\mathbf{V}}}{dt} \\ &= \bar{\mathbf{V}} \times \bar{\mathbf{V}} + \bar{\mathbf{R}} \times \left(\bar{\mathcal{F}} - \frac{\mu\bar{\mathbf{R}}}{R^3} \right) \\ &= \bar{\mathbf{R}} \times \left(\bar{\mathcal{F}} - \frac{\mu\bar{\mathbf{R}}}{R^3} \right) \\ &= \bar{\mathbf{R}} \times \bar{\mathcal{F}} - \bar{\mathbf{R}} \times \frac{\mu\bar{\mathbf{R}}}{R^3} \end{aligned}$$

$$\frac{d\bar{\mathbf{h}}}{dt} = \bar{\mathbf{R}} \times \bar{\mathcal{F}}$$

$$\begin{aligned} \mu \frac{d\bar{\mathbf{e}}}{dt} &= \frac{d}{dt} (\bar{\mathbf{V}} \times \bar{\mathbf{h}}) - \mu \frac{d}{dt} \bar{\mathbf{e}}_R \\ &= \frac{d\bar{\mathbf{V}}}{dt} \times \bar{\mathbf{h}} + \bar{\mathbf{V}} \times \frac{d\bar{\mathbf{h}}}{dt} - \mu \frac{d}{dt} \left(\frac{\bar{\mathbf{R}}}{R} \right) \end{aligned}$$

$$\begin{aligned}
&= \frac{d\bar{V}}{dt} \times \bar{h} + \bar{V} \times \frac{d\bar{h}}{dt} - \frac{\mu}{R^2} \left[R \frac{d\bar{R}}{dt} - \bar{R} \frac{dR}{dt} \right] \\
&= \frac{d\bar{V}}{dt} \times \bar{h} + \bar{V} \times (\bar{R} \times \bar{\mathcal{F}}) - \frac{\mu}{R^3} \left(\bar{R} \times \frac{d\bar{R}}{dt} \right) \times \bar{R} \\
&= \frac{d\bar{V}}{dt} \times \bar{h} + \bar{V} \times (\bar{R} \times \bar{\mathcal{F}}) - \frac{\mu}{R^3} (\bar{h} \times \bar{R}) \\
&= \left(\frac{d\bar{V}}{dt} + \frac{\mu \bar{R}}{R^3} \right) \times \bar{h} + \bar{V} \times (\bar{R} \times \bar{\mathcal{F}}) \\
&= \bar{\mathcal{F}} \times (\bar{R} \times \bar{V}) + \bar{V} \times (\bar{R} \times \bar{\mathcal{F}})
\end{aligned}$$

1. The derivation of $\frac{di}{dt}$

$$\begin{aligned}
\cos i &= \bar{e}_h \cdot \bar{k} \\
-\sin i \frac{di}{dt} &= \bar{k} \cdot \frac{d\bar{e}_h}{dt} + \bar{e}_h \cdot \frac{d\bar{k}}{dt} = \bar{k} \cdot \frac{d\bar{e}_h}{dt} + 0 \\
&= \frac{1}{h^3} \left(\bar{h} \times \frac{d\bar{h}}{dt} \times \bar{h} \cdot \bar{k} \right) \\
&= \frac{1}{h^3} \left(\bar{h} \times \frac{d\bar{h}}{dt} \right) \cdot (-\bar{e}_\Omega h \sin i) \\
\frac{di}{dt} &= \frac{1}{h^2} \left(\bar{h} \times \frac{d\bar{h}}{dt} \right) \cdot \bar{e}_\Omega
\end{aligned}$$

$$\begin{aligned}
\frac{d\mathbf{i}}{dt} &= \frac{d\mathbf{h}}{dt} \cdot \frac{(\bar{\mathbf{e}}_{\Omega} \times \bar{\mathbf{h}})}{h^2} \\
&= (\bar{\mathbf{R}} \times \bar{\mathcal{F}}) \cdot \frac{(\bar{\mathbf{e}}_{\Omega} \times \bar{\mathbf{e}}_h)}{h} \\
&= \frac{\mathbf{R}}{h} (\bar{\mathbf{e}}_R \times \bar{\mathbf{e}}_h) \times \bar{\mathbf{e}}_R \cdot \bar{\mathcal{F}}
\end{aligned}$$

$$\frac{d\mathbf{i}}{dt} = \frac{\mathbf{R}}{h} \cos u (\bar{\mathbf{e}}_h \cdot \bar{\mathcal{F}})$$

2. The derivation of $\frac{d\Omega}{dt}$

$$\begin{aligned}
\cos \Omega &= \bar{\mathbf{e}}_{\Omega} \cdot \bar{\mathbf{i}} \\
-\sin \Omega \frac{d\Omega}{dt} &= \bar{\mathbf{i}} \cdot \frac{d\bar{\mathbf{e}}_{\Omega}}{dt} + 0
\end{aligned}$$

$$\frac{d\bar{\mathbf{e}}_{\Omega}}{dt} = \frac{d}{dt} \left(\frac{\bar{\mathbf{k}} \times \bar{\mathbf{h}}}{h \sin i} \right)$$

$$= \frac{\bar{\mathbf{k}}}{h \sin i} \times \frac{d\bar{\mathbf{h}}}{dt} - \frac{\bar{\mathbf{k}} \times \bar{\mathbf{h}}}{h^2 \sin^2 i} \frac{d}{dt} (h \sin i)$$

$$= \frac{\bar{\mathbf{k}}}{h \sin i} \times \frac{d\bar{\mathbf{h}}}{dt} - \frac{\bar{\mathbf{e}}_{\Omega}}{h \sin i} \frac{d}{dt} (\bar{\mathbf{k}} \times \bar{\mathbf{h}} \cdot \bar{\mathbf{e}}_{\Omega})$$

$$= \frac{1}{h \sin i} \left[\left(\bar{\mathbf{k}} \times \frac{d\bar{\mathbf{h}}}{dt} \right) - \bar{\mathbf{e}}_{\Omega} \left\{ (\bar{\mathbf{k}} \times \bar{\mathbf{h}}) \cdot \frac{d\bar{\mathbf{e}}_{\Omega}}{dt} + \bar{\mathbf{e}}_{\Omega} \cdot \frac{d}{dt} (\bar{\mathbf{k}} \times \bar{\mathbf{h}}) \right\} \right]$$

$$= \frac{1}{h \sin i} \left[\bar{k} \times \frac{d\bar{h}}{dt} - \bar{e}_\Omega \left\{ 0 + \bar{e}_\Omega \cdot \bar{k} \times \frac{d\bar{h}}{dt} \right\} \right]$$

$$\frac{d\bar{e}_\Omega}{dt} = \frac{1}{h \sin i} \left[\bar{k} \times \frac{d\bar{h}}{dt} - \bar{e}_\Omega \left(\bar{k} \times \frac{d\bar{h}}{dt} \cdot \bar{e}_\Omega \right) \right]$$

$$\frac{d\bar{e}_\Omega}{dt} = \frac{1}{h \sin i} \left[\bar{e}_\Omega \times \left(\bar{k} \times \frac{d\bar{h}}{dt} \right) \right] \times \bar{e}_\Omega$$

$$-\sin \Omega \frac{d\Omega}{dt} = \frac{d\bar{e}_\Omega}{dt} \cdot \bar{i}$$

$$= \frac{1}{h \sin i} \left[\bar{e}_\Omega \times \left(\bar{k} \times \frac{d\bar{h}}{dt} \right) \right] \times \bar{e}_\Omega \cdot \bar{i}$$

$$= \frac{1}{h \sin i} \left[\bar{e}_\Omega \times \left(\bar{k} \times \frac{d\bar{h}}{dt} \right) \right] \cdot \bar{e}_\Omega \times \bar{i}$$

$$= \frac{1}{h \sin i} \left[\bar{e}_\Omega \times \left(\bar{k} \times \frac{d\bar{h}}{dt} \right) \right] \cdot (-k \sin \Omega)$$

$$\frac{d\Omega}{dt} = \frac{1}{h \sin i} \left[\bar{e}_\Omega \times \left(\bar{k} \times \frac{d\bar{h}}{dt} \right) \right] \cdot \bar{k}$$

$$= \frac{\bar{k} \times \bar{e}_\Omega}{h \sin i} \cdot \bar{k} \times \frac{d\bar{h}}{dt}$$

$$= \frac{(\bar{k} \times \bar{e}_\Omega)}{h \sin i} \times \bar{k} \cdot \frac{d\bar{h}}{dt}$$

$$= \frac{\bar{e}_\Omega}{h \sin i} \cdot (\bar{k} \times \bar{f})$$

$$\begin{aligned}
\frac{d\Omega}{dt} &= \frac{\bar{e}_\Omega}{h \sin i} \cdot (R \bar{e}_R \times \bar{\mathcal{F}}) \\
&= \frac{R \bar{e}_\Omega}{h \sin i} \cdot (\bar{e}_R \times \bar{\mathcal{F}}) \\
&= \frac{R}{h \sin i} (\bar{e}_\Omega \times \bar{e}_R) \cdot \bar{\mathcal{F}} \\
\frac{d\Omega}{dt} &= \frac{R}{h \sin i} \sin u (\bar{e}_h \cdot \bar{\mathcal{F}})
\end{aligned}$$

3. The derivation of $\frac{dp}{dt}$

$$\begin{aligned}
\frac{dp}{dt} &= \frac{d}{dt} \left(\frac{\bar{h} \cdot \bar{h}}{\mu} \right) \\
&= \frac{2}{\mu} \bar{h} \cdot \frac{d\bar{h}}{dt} \\
&= \frac{2}{\mu} \bar{h} \cdot (\bar{R} \times \bar{\mathcal{F}}) \\
&= \frac{2}{\mu} h \bar{e}_h \cdot (R \bar{e}_R \times \bar{\mathcal{F}})
\end{aligned}$$

$$\begin{aligned}
\frac{dp}{dt} &= \frac{2hR}{\mu} \bar{e}_h \cdot \bar{e}_R \times \bar{\mathcal{F}} \\
&= \frac{2hR}{\mu} \bar{e}_h \times \bar{e}_R \cdot \bar{\mathcal{F}}
\end{aligned}$$

$$\frac{dp}{dt} = \frac{2hR}{\mu} (\bar{e}_h \cdot \bar{f})$$

$$\frac{1}{p} \frac{dp}{dt} = \frac{2R}{h} (\bar{e}_h \cdot \bar{f})$$

4. The derivation of $\frac{dA}{dt}$

$$A = \bar{e}_\Omega \cdot \bar{e}$$

$$\frac{dA}{dt} = \bar{e} \cdot \frac{d\bar{e}_\Omega}{dt} + \bar{e}_\Omega \cdot \frac{d\bar{e}}{dt}$$

$$= \bar{e} \cdot \left[\frac{1}{h \sin i} \bar{e}_\Omega \times \left(\bar{k} \times \frac{d\bar{h}}{dt} \right) \right] \times \bar{e}_\Omega + \bar{e}_\Omega \cdot \frac{d\bar{e}}{dt}$$

$$= \bar{e} \cdot \left[\frac{d\Omega}{dt} \bar{k} \right] \times \bar{e}_\Omega + \bar{e}_\Omega \cdot \frac{d\bar{e}}{dt}$$

$$= \frac{d\Omega}{dt} \bar{k} \cdot (\bar{e}_\Omega \times \bar{e}) + \bar{e}_\Omega \cdot \frac{d\bar{e}}{dt}$$

$$= \frac{d\Omega}{dt} \bar{k} \cdot B \bar{e}_h + \bar{e}_\Omega \cdot \frac{d\bar{e}}{dt}$$

$$= B \frac{d\Omega}{dt} (\bar{R} \cdot \bar{e}_h) + \bar{e}_\Omega \cdot \frac{d\bar{e}}{dt}$$

$$\frac{dA}{dt} = B \frac{d\Omega}{dt} \cos i + \bar{e}_\Omega \cdot \frac{d\bar{e}}{dt}$$

$$\frac{d\bar{\mathbf{e}}}{dt} = \frac{1}{\mu} \{ \bar{\mathcal{F}} \times (\bar{\mathbf{R}} \times \bar{\mathbf{V}}) + \bar{\mathbf{V}} \times (\bar{\mathbf{R}} \times \bar{\mathcal{F}}) \}$$

$$\bar{\mathbf{e}}_{\Omega} \cdot \frac{d\bar{\mathbf{e}}}{dt} = \frac{\bar{\mathbf{e}}_{\Omega}}{dt} \cdot \{ \bar{\mathbf{R}} (\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) - \bar{\mathbf{V}} (\bar{\mathbf{R}} \cdot \bar{\mathcal{F}}) + \bar{\mathbf{R}} (\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) - \bar{\mathcal{F}} (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \}$$

$$\bar{\mathbf{e}}_{\Omega} = \bar{\mathbf{e}}_{\mathbf{R}} \cos u - \bar{\mathbf{e}}_{\mathbf{L}} \sin u$$

$$\bar{\mathbf{e}}_{\Omega} \cdot \bar{\mathbf{e}}_{\mathbf{R}} = \cos u$$

$$\bar{\mathbf{e}}_{\Omega} \cdot \bar{\mathbf{e}}_{\mathbf{L}} = -\sin u$$

$$\bar{\mathbf{R}} \cdot \bar{\mathbf{e}}_{\Omega} = R \cos u$$

$$\bar{\mathbf{V}} \cdot \bar{\mathbf{e}}_{\Omega} = \frac{-\mu}{h} [(1 + A \cos u + B \sin u) \bar{\mathbf{e}}_{\mathbf{L}} + (A \sin u - B \cos u) \bar{\mathbf{e}}_{\mathbf{R}}] \cdot \bar{\mathbf{e}}_{\Omega}$$

$$= \frac{\mu}{h} [(1 + A \cos u + B \sin u) \bar{\mathbf{e}}_{\mathbf{L}} + (A \sin u - B \cos u) \bar{\mathbf{e}}_{\mathbf{R}}] \cdot [\bar{\mathbf{e}}_{\mathbf{R}} \cos u - \bar{\mathbf{e}}_{\mathbf{L}} \sin u]$$

$$= \frac{\mu}{h} [-(1 + A \cos u + B \sin u) \sin u + (A \sin u - B \cos u) \cos u]$$

$$= \frac{\mu}{h} [-\sin u - A \sin u \cos u - B \sin^2 u + A \sin u \cos u - B \cos^2 u]$$

$$\bar{\mathbf{V}} \cdot \bar{\mathbf{e}}_{\Omega} = \frac{\mu}{h} [B + \sin u]$$

$$\bar{\mathbf{V}} \cdot \bar{\mathbf{R}} = \frac{\mu}{h} [(1 + A \cos u + B \sin u) \bar{\mathbf{e}}_{\mathbf{L}} + (A \sin u - B \cos u) \bar{\mathbf{e}}_{\mathbf{R}}] \cdot R \bar{\mathbf{e}}_{\mathbf{R}}$$

$$\bar{\mathbf{V}} \cdot \bar{\mathbf{R}} = \frac{\mu R}{h} [A \sin u - B \cos u]$$

$$\begin{aligned}
\bar{e} \cdot \frac{d\bar{e}}{dt} &= \frac{1}{\mu} \{ 2(\bar{V} \cdot \bar{\mathcal{F}}) (\bar{R} \cdot e_{\Omega}) - (\bar{R} \cdot \bar{\mathcal{F}}) (\bar{V} \cdot \bar{e}_{\Omega}) - (\bar{\mathcal{F}} \cdot \bar{e}_{\Omega}) (\bar{V} \cdot \bar{R}) \} \\
&= \frac{1}{\mu} \{ 2R \cos u (\bar{V} \cdot \bar{\mathcal{F}}) + \frac{\mu}{h} (B + \sin u) (\bar{R} \cdot \bar{\mathcal{F}}) - \frac{\mu R}{h} [A \sin u - B \cos u] (\bar{\mathcal{F}} \cdot \bar{e}_R) \} \\
&= \frac{1}{\mu} \{ 2R \cos u \bar{V} + \frac{\mu}{h} (B + \sin u) R \bar{e}_R - \frac{\mu}{h} R [A \sin u - B \cos u] \bar{e}_{\Omega} \} \cdot \bar{\mathcal{F}} \\
&= \frac{1}{\mu} \left\{ \frac{2\mu R}{h} \cos u [1 + A \cos u + B \sin u] \bar{e}_L + \frac{2\mu R}{h} \cos u [A \sin u - B \cos u] \bar{e}_R \right. \\
&\quad \left. - \frac{\mu R}{h} [B + \sin u] \bar{e}_R - \frac{\mu R}{h} [A \sin u - B \cos u] [\bar{e}_R \cos u - e_L \sin u] \right\} \cdot \bar{\mathcal{F}} \\
&= \frac{R}{h} \{ (2 \cos u [1 + A \cos u + B \sin u] + [A \sin u - B \cos u] \sin u) \bar{e}_L \\
&\quad + (2[A \sin u - B \cos u] \cos u + [B + \sin u] - [A \sin u - B \cos u] \cos u) \bar{e}_R \} \cdot \bar{\mathcal{F}} \\
&= \frac{R}{h} \{ (2\psi \cos u + A \sin^2 u - B \sin u \cos u) \bar{e}_L + (A \sin u \cos u - B \cos^2 u \\
&\quad + \sin u) \bar{e}_R \} \cdot \bar{\mathcal{F}}
\end{aligned}$$

$$\bar{e} \cdot \frac{d\bar{e}}{dt} = \frac{R}{h} \{ [A + (1 + \psi) \cos u] \bar{e}_L + \psi \sin u \bar{e}_R \} \cdot \bar{\mathcal{F}}$$

$$\frac{dA}{dt} = B \frac{d\Omega}{dt} \cos i + \bar{e}_{\Omega} \cdot \frac{d\bar{e}}{dt}$$

$$\frac{dA}{dt} = B \frac{d\Omega}{dt} \cos i + \frac{R}{h} \{ [A + (1 + \psi) \cos u] \bar{e}_L + \psi \sin u \bar{e}_R \} \cdot \bar{\mathcal{F}}$$

5. The derivation of $\frac{dB}{dt}$

$$B = \bar{e}_\Omega \times \bar{e} \cdot \bar{e}_h$$

$$\begin{aligned} \frac{dB}{dt} &= \frac{d}{dt} (\bar{e}_\Omega \times \bar{e}) \cdot \bar{e}_h + \frac{d\bar{e}_h}{dt} \cdot (\bar{e}_\Omega \times \bar{e}) \\ &= \left[\frac{d\bar{e}_\Omega}{dt} \times \bar{e} + \bar{e}_\Omega \times \frac{d\bar{e}}{dt} \right] \cdot \bar{e}_h + \frac{d\bar{e}_h}{dt} \cdot (\bar{e}_\Omega \times \bar{e}) \\ &= \bar{e}_h \cdot \frac{d\bar{e}_\Omega}{dt} \times \bar{e} + \bar{e}_h \cdot \bar{e}_\Omega \times \frac{d\bar{e}}{dt} + \frac{d\bar{e}_h}{dt} \cdot (\bar{e}_\Omega \times \bar{e}) \end{aligned}$$

$$\frac{dB}{dt} = \bar{e}_h \cdot \frac{d\bar{e}_\Omega}{dt} \times \bar{e} + \bar{e}_h \cdot \bar{e}_\Omega \times \frac{d\bar{e}}{dt} + \frac{d\bar{e}_h}{dt} \cdot B \bar{e}_h$$

$$\frac{d\bar{e}_\Omega}{dt} = \frac{d\Omega}{dt} \bar{k} \times \bar{e}_\Omega$$

$$\begin{aligned} \frac{dB}{dt} &= \bar{e}_h \cdot \left(\frac{d\Omega}{dt} \bar{k} \times \bar{e}_\Omega \right) \times \bar{e} + \bar{e}_h \cdot \bar{e}_\Omega \times \frac{d\bar{e}}{dt} \\ &= \frac{d\Omega}{dt} (\bar{k} \times \bar{e}_\Omega) \times \bar{e} \cdot \bar{e}_h + \bar{e}_h \cdot \bar{e}_\Omega \times \frac{d\bar{e}}{dt} \\ &= \frac{d\Omega}{dt} (\bar{k} \times \bar{e}_\Omega) \cdot (\bar{e} \times \bar{e}_h) + \bar{e}_h \cdot \bar{e}_\Omega \times \frac{d\bar{e}}{dt} \\ &= \frac{d\Omega}{dt} [(\bar{k} \cdot \bar{e})(\bar{e}_\Omega \cdot \bar{e}_h) - (\bar{k} \cdot \bar{e}_h)(\bar{e}_\Omega \cdot \bar{e})] + \bar{e}_h \cdot \bar{e}_\Omega \times \frac{d\bar{e}}{dt} \end{aligned}$$

$$= -\frac{d\Omega}{dt} (\bar{\mathbf{k}} \cdot \bar{\mathbf{e}}_h) (\bar{\mathbf{e}}_\Omega \cdot \bar{\mathbf{e}}) + \bar{\mathbf{e}}_h \cdot \bar{\mathbf{e}}_\Omega \times \frac{d\bar{\mathbf{e}}}{dt}$$

$$\frac{dB}{dt} = -\frac{d\Omega}{dt} A \cos i + \bar{\mathbf{e}}_h \cdot \bar{\mathbf{e}}_\Omega \times \frac{d\bar{\mathbf{e}}}{dt}$$

$$\frac{dB}{dt} = -\frac{d\Omega}{dt} A \cos i - \bar{\mathbf{e}}_\Omega \cdot \frac{d\bar{\mathbf{e}}}{dt} \times \bar{\mathbf{e}}_h$$

$$\frac{dB}{dt} = -\frac{d\Omega}{dt} A \cos i + \bar{\mathbf{e}}_h \times \bar{\mathbf{e}}_\Omega \cdot \frac{d\bar{\mathbf{e}}}{dt}$$

$$\bar{\mathbf{e}}_\Omega = \bar{\mathbf{e}}_R \cos u - \bar{\mathbf{e}}_L \sin u$$

$$\bar{\mathbf{e}}_h \times \bar{\mathbf{e}}_\Omega = \bar{\mathbf{e}}_h \times [\bar{\mathbf{e}}_R \cos u - \bar{\mathbf{e}}_L \sin u]$$

$$= \bar{\mathbf{e}}_h \times \bar{\mathbf{e}}_R \cos u - \bar{\mathbf{e}}_h \times \bar{\mathbf{e}}_L \sin u$$

$$\bar{\mathbf{e}}_h \times \bar{\mathbf{e}}_\Omega = \bar{\mathbf{e}}_L \cos u + \bar{\mathbf{e}}_R \sin u$$

$$\bar{\mathbf{e}}_h \times \bar{\mathbf{e}}_\Omega \cdot \frac{d\bar{\mathbf{e}}}{dt} = [\bar{\mathbf{e}}_L \cos u + \bar{\mathbf{e}}_R \sin u] \cdot \frac{d\bar{\mathbf{e}}}{dt}$$

$$= \bar{\mathbf{e}}_L \cdot \frac{d\bar{\mathbf{e}}}{dt} \cos u + \bar{\mathbf{e}}_R \cdot \frac{d\bar{\mathbf{e}}}{dt} \sin u$$

$$\frac{d\bar{\mathbf{e}}}{dt} = \frac{1}{\mu} [2\bar{\mathbf{R}} (\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) - \bar{\mathbf{V}} (\bar{\mathbf{R}} \cdot \bar{\mathcal{F}}) - \bar{\mathcal{F}} (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}})]$$

$$\bar{\mathbf{e}}_L \cdot \frac{d\bar{\mathbf{e}}}{dt} = \frac{1}{\mu} [2(\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) (\bar{\mathbf{R}} \cdot \bar{\mathbf{e}}_L) - (\bar{\mathbf{R}} \cdot \bar{\mathcal{F}}) (\bar{\mathbf{V}} \cdot \bar{\mathbf{e}}_L) - (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) (\bar{\mathcal{F}} \cdot \bar{\mathbf{e}}_L)]$$

$$= \frac{1}{\mu} [2\bar{V}(\bar{R} \cdot \bar{e}_L) - \bar{R}(\bar{V} \cdot \bar{e}_L) - (\bar{V} \cdot \bar{R})\bar{e}_L] \cdot \bar{\mathcal{F}}$$

$$\bar{R} \cdot \bar{e}_L = 0$$

$$\bar{R} \cdot \bar{V} = \frac{\mu R}{h} [A \sin u - B \cos u]$$

$$\bar{V} \cdot \bar{e}_L = \frac{\mu}{h} \{ [1 + A \cos u + B \sin u] \bar{e}_L + [A \sin u - B \cos u] \bar{e}_R \} \cdot \bar{e}_L$$

$$\bar{V} \cdot \bar{e}_L = \frac{\mu}{h} [1 + A \cos u + B \sin u]$$

$$\begin{aligned} \bar{e}_R \cdot \frac{d\bar{e}}{dt} &= \frac{1}{\mu} \{ 2(\bar{V} \cdot \bar{\mathcal{F}}) (\bar{R} \cdot \bar{e}_R) - (\bar{R} \cdot \bar{\mathcal{F}}) (\bar{V} \cdot \bar{e}_R) - (\bar{V} \cdot \bar{R}) (\bar{\mathcal{F}} \cdot \bar{e}_R) \} \\ &= \frac{1}{\mu} \{ 2\bar{V}(\bar{R} \cdot \bar{e}_R) - \bar{R}(\bar{V} \cdot \bar{e}_R) - (\bar{V} \cdot \bar{R})\bar{e}_R \} \cdot \bar{\mathcal{F}} \end{aligned}$$

$$\bar{V} \cdot \bar{e}_R = \frac{\mu}{h} \{ [1 + A \cos u + B \sin u] \bar{e}_L + [A \sin u - B \cos u] \bar{e}_R \} \cdot \bar{e}_R$$

$$\bar{V} \cdot \bar{e}_R = \frac{\mu}{h} [A \sin u - B \cos u]$$

$$\begin{aligned} \bar{e}_L \cdot \frac{d\bar{e}}{dt} \cos u + \bar{e}_R \cdot \frac{d\bar{e}}{dt} \sin u &= \frac{1}{\mu} \cos u \left\{ -\frac{\mu}{h} \bar{R} [1 + A \cos u + B \sin u] \right. \\ &\quad \left. - \frac{\mu R}{h} [A \sin u - B \cos u] \bar{e}_L \right\} \cdot \bar{\mathcal{F}} + \frac{1}{\mu} \sin u \left\{ 2R\bar{V} - \frac{\mu R}{h} [A \sin u - B \cos u] \right. \\ &\quad \left. - \frac{\mu R}{h} [A \sin u - B \cos u] \bar{e}_R \right\} \cdot \bar{\mathcal{F}} \end{aligned}$$

$$\bar{e}_L \cdot \frac{d\bar{e}}{dt} \cos u + \bar{e}_R \cdot \frac{d\bar{e}}{dt} \sin u = \frac{R}{h} \{ -[\psi] \cos u \bar{e}_R - [A \sin u - B \cos u] \cos u \bar{e}_L$$

$$+ 2 \sin u \psi \bar{e}_L + [A \sin u - B \cos u] \sin u \bar{e}_R$$

$$- [A \sin u - B \cos u] \sin u \bar{e}_R - [A \sin u - B \cos u] \sin u \bar{e}_R \} \cdot \bar{\mathcal{F}}$$

$$\bar{e}_L \cdot \frac{d\bar{e}}{dt} \cos u + \bar{e}_R \cdot \frac{d\bar{e}}{dt} \sin u = \frac{R}{h} \{ (-\psi \cos u + [A \sin u - B \cos u] \sin u$$

$$- [A \sin u - B \cos u] \sin u) \bar{e}_R + (-[A \sin u - B \cos u] \cos u$$

$$+ 2\psi \sin u \bar{e}_L) \cdot \bar{\mathcal{F}}$$

$$\bar{e}_L \cdot \frac{d\bar{e}}{dt} \cos u + \bar{e}_R \cdot \frac{d\bar{e}}{dt} \sin u = \frac{R}{h} \{ -\psi \cos u \bar{e}_R + (-[A \sin u - B \cos u] \cos u$$

$$+ 2\psi \sin u) \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\bar{e}_L \cdot \frac{d\bar{e}}{dt} \cos u + \bar{e}_R \cdot \frac{d\bar{e}}{dt} \sin u$$

$$= \frac{R}{h} \{ -\psi \cos u \bar{e}_R + (-A \sin u \cos u + B \cos^2 u + 2\psi \sin u) \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$= \frac{R}{h} \{ -\psi \cos u \bar{e}_R + (-\sin u \cos u + B - B \sin^2 u + 2\psi \sin u) \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$= \frac{R}{h} \{ -\psi \cos u \bar{e}_R + [\sin u (-\cos u - B \sin u + 2\psi) + B] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$= \frac{R}{h} \{ -\psi \cos u + [(1 + \psi) \sin u + B] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\begin{aligned}\frac{dB}{dt} &= -\frac{d\Omega}{dt} A \cos i + \bar{\mathbf{e}}_h \times \bar{\mathbf{e}}_\Omega \cdot \frac{d\bar{\mathbf{e}}}{dt} \\ &= -\frac{d\Omega}{dt} A \cos i + \bar{\mathbf{e}}_L \cdot \frac{d\bar{\mathbf{e}}}{dt} \cos u + \bar{\mathbf{e}}_R \cdot \frac{d\bar{\mathbf{e}}}{dt} \sin u\end{aligned}$$

$$\frac{dB}{dt} = -\frac{d\Omega}{dt} A \cos i + \frac{R}{h} \{ -\psi \cos u \bar{\mathbf{e}}_R + [(1 + \psi) \sin u + B] \bar{\mathbf{e}}_L \} \cdot \bar{\mathcal{F}}$$

6. The derivation of $\frac{de}{dt}$

$$\begin{aligned}\frac{de}{dt} &= \frac{d}{dt} (\bar{\mathbf{e}} \cdot \bar{\mathbf{e}})^{\frac{1}{2}} \\ &= \frac{1}{e} \bar{\mathbf{e}} \cdot \frac{d\bar{\mathbf{e}}}{dt} \\ &= \frac{1}{\mu e} \left[\frac{\bar{\mathbf{V}} \times (\bar{\mathbf{R}} \times \bar{\mathbf{V}})}{\mu} - \bar{\mathbf{e}}_R \right] \cdot \left[\bar{\mathcal{F}} \times (\bar{\mathbf{R}} \times \bar{\mathbf{V}}) + \bar{\mathbf{V}} \times (\bar{\mathbf{R}} \times \bar{\mathcal{F}}) \right] \\ &= \frac{1}{\mu e} \left\{ \left[\frac{(\bar{\mathbf{V}} \cdot \bar{\mathbf{V}}) \bar{\mathbf{R}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \bar{\mathbf{V}}}{\mu} - \bar{\mathbf{e}}_R \right] \cdot \left[2(\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{R}} - (\bar{\mathbf{R}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{V}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \bar{\mathcal{F}} \right] \right\} \\ &= \frac{1}{\mu e} \left\{ \frac{(\bar{\mathbf{V}} \cdot \bar{\mathbf{V}}) \bar{\mathbf{R}}}{\mu} \cdot [2(\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{R}} - (\bar{\mathbf{R}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{V}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \bar{\mathcal{F}}] \right. \\ &\quad - \frac{(\bar{\mathbf{V}} \cdot \bar{\mathbf{R}})}{\mu} \bar{\mathbf{V}} \cdot [2(\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{R}} - (\bar{\mathbf{R}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{V}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \bar{\mathcal{F}}] \\ &\quad \left. - \bar{\mathbf{e}}_R \cdot [2(\bar{\mathbf{V}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{R}} - (\bar{\mathbf{R}} \cdot \bar{\mathcal{F}}) \bar{\mathbf{V}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \bar{\mathcal{F}}] \right\}\end{aligned}$$

$$= \frac{1}{\mu e} \left\{ \frac{(\bar{\mathbf{V}} \cdot \bar{\mathbf{V}})}{\mu} [2R^2 \bar{\mathbf{V}} - 2\bar{\mathbf{R}} (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}})] - \frac{(\bar{\mathbf{V}} \cdot \bar{\mathbf{R}})}{\mu} [(\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \bar{\mathbf{V}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{V}}) \bar{\mathbf{R}}] \right. \\ \left. - [2 (\bar{\mathbf{R}} \cdot \bar{\mathbf{e}}_R) \bar{\mathbf{V}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{e}}_R) \bar{\mathbf{R}} - (\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) \bar{\mathbf{e}}_R] \right\} \bar{\mathcal{F}}$$

$$\bar{\mathbf{V}} = \frac{\mu}{h} \{ [1 + e \cos \theta] \bar{\mathbf{e}}_L + e \sin \theta \bar{\mathbf{e}}_R \}$$

$$\bar{\mathbf{R}} = R \bar{\mathbf{e}}_R$$

$$(\bar{\mathbf{V}} \cdot \bar{\mathbf{R}}) = \frac{\mu R}{h} e \sin \theta$$

$$(\bar{\mathbf{V}} \cdot \bar{\mathbf{V}}) = \frac{\mu^2}{h^2} \{ [1 + e \cos \theta]^2 + e^2 \sin^2 \theta \}$$

$$= \frac{\mu^2}{h^2} \{ 1 + e^2 + 2e \cos \theta \}$$

$$(\bar{\mathbf{V}} \cdot \bar{\mathbf{e}}_R) = \frac{\mu}{h} e \sin \theta$$

$$\frac{de}{dt} = \frac{1}{\mu e} \left\{ \frac{\mu}{h^2} [1 + e^2 + 2e \cos \theta] \left[2R^2 \frac{\mu}{h} ([1 + e \cos \theta] \bar{\mathbf{e}}_L + e \sin \theta \bar{\mathbf{e}}_R) \right. \right. \\ \left. \left. - \frac{2R^2 \mu}{h} e \sin \theta \bar{\mathbf{e}}_R \right] - \frac{R e \sin \theta}{h} \left[\frac{\mu R e \sin \theta}{h} \frac{\mu}{h} ([1 + e \cos \theta] \bar{\mathbf{e}}_L + e \sin \theta \bar{\mathbf{e}}_R) \right. \right. \\ \left. \left. - \frac{\mu^2}{h^2} R [1 + e^2 + 2e \cos \theta] \bar{\mathbf{e}}_R \right] - \frac{2\mu R}{h} ([1 + e \cos \theta] \bar{\mathbf{e}}_L + e \sin \theta \bar{\mathbf{e}}_R) \right\}$$

$$\begin{aligned}
& + \frac{\mu R}{h} \sin\theta \bar{e}_R + \frac{\mu R}{h} \sin\theta \bar{e}_R \left\} \cdot \bar{f} \\
& = \frac{R}{h} \left\{ \frac{2\mu R}{eh^2} [1 + e^2 + 2e\cos\theta] [(\psi \bar{e}_L + \sin\theta \bar{e}_R) - \sin\theta \bar{e}_R] \right. \\
& \quad - \frac{\mu R \sin\theta}{h^2} [\sin\theta (\psi \bar{e}_L + \sin\theta \bar{e}_R) - (1 + e^2 + 2e\cos\theta) \bar{e}_R] \\
& \quad \left. - \frac{2}{e} (\psi \bar{e}_L + \sin\theta \bar{e}_R) + 2\sin\theta \bar{e}_R \right\} \cdot \bar{f} \\
& \frac{de}{dt} = \frac{R}{h} \left\{ \frac{2}{\psi e} [1 + e^2 + 2e\cos\theta] [(\psi \bar{e}_L + \sin\theta \bar{e}_R) - \sin\theta \bar{e}_R] \right. \\
& \quad - \frac{\sin\theta}{\psi} [\sin\theta (\psi \bar{e}_L + \sin\theta \bar{e}_R) - [1 + e^2 + 2e\cos\theta] \bar{e}_R] \\
& \quad \left. - \frac{2}{e} (\psi \bar{e}_L + \sin\theta \bar{e}_R) + 2\sin\theta \bar{e}_R \right\} \cdot \bar{f} \\
& = \frac{R}{h} \left\{ \left[\frac{2}{\psi e} [1 + e^2 + 2e\cos\theta] \psi - \frac{e\sin^2\theta}{\psi} \psi - \frac{2\psi}{e} \right] \bar{e}_L \right. \\
& \quad \left. + \left[-\frac{e^2\sin^3\theta}{\psi} + \frac{\sin\theta}{\psi} [1 + e^2 + 2e\cos\theta] \right] \bar{e}_R \right\} \cdot \bar{f} \\
& = \frac{R}{h} \left\{ \left[\frac{2}{e} [1 + e^2 + 2e\cos\theta] - e\sin^2\theta - \frac{2}{e} [1 + e\cos\theta] \right] \bar{e}_L \right. \\
& \quad \left. + \frac{\sin\theta}{\psi} \left[-e^2\sin^2\theta + [1 + e^2 + 2e\cos\theta] \right] \bar{e}_R \right\} \cdot \bar{f}
\end{aligned}$$

$$\begin{aligned}
&= \frac{R}{h} \left\{ [2e + 2\cos\theta - e\sin^2\theta] \bar{e}_L + \left[-\frac{e\sin^2\theta}{\psi} \right. \right. \\
&\quad \left. \left. + \frac{\sin\theta}{\psi} [1 + e^2 + 2e\cos\theta] \right] \bar{e}_R \right\} \cdot \bar{\mathcal{F}} \\
\frac{de}{dt} &= \frac{R}{h} \left\{ [e + (1 + \psi)\cos\theta] \bar{e}_L + \psi\sin\theta \bar{e}_R \right\} \cdot \bar{\mathcal{F}}
\end{aligned}$$

7. The derivation of $\frac{d\omega}{dt}$

$$\cos\omega = \frac{\bar{e}_\Omega \cdot \bar{e}}{e}$$

$$-\sin\omega \frac{d\omega}{dt} = \frac{1}{e} \frac{d}{dt} (\bar{e}_\Omega \cdot \bar{e}) - \frac{1}{e^2} (\bar{e}_\Omega \cdot \bar{e}) \frac{de}{dt}$$

$$-\sin\omega \frac{d\omega}{dt} = \frac{1}{e} \frac{dA}{dt} - \frac{\cos\omega}{e} \frac{de}{dt}$$

$$-\sin\omega \frac{d\omega}{dt} = \frac{dA}{dt} - \cos\omega \frac{de}{dt}$$

$$= B \frac{d\Omega}{dt} \cos i + \frac{R}{h} \{ [A + (1 + \psi)\cos u] \bar{e}_L + \psi\sin u \bar{e}_R \} \cdot \bar{\mathcal{F}}$$

$$-\cos\omega \frac{R}{h} \{ \psi\sin\theta \bar{e}_R + [e + (1 + \psi)\cos\theta] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\frac{d\omega}{dt} = \frac{R}{he} \cot\omega \{ \psi \sin\theta \bar{e}_R + [e + (1 + \psi) \cos\theta] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$- \frac{d\Omega}{dt} \cos i - \frac{R}{he} \csc\omega \{ \psi \sin u \bar{e}_R + [A + (1 + \psi) \cos u] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\frac{d\omega}{dt} = - \frac{d\Omega}{dt} \cos i + \frac{R}{he} \{ \psi \sin\theta \cot\omega \bar{e}_R + \cot\omega [e + (1 + \psi) \cos\theta] \bar{e}_L$$

$$- \psi \sin u \csc\omega \bar{e}_R - \csc\omega [A + (1 + \psi) \cos u] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\frac{d\omega}{dt} = - \frac{d\Omega}{dt} \cos i + \frac{R}{he} \{ [\psi \sin\theta \cot\omega - \psi \sin u \csc\omega] \bar{e}_R$$

$$+ \left(\cot\omega [e + (1 + \psi) \cos\theta] - \csc\omega [A + (1 + \psi) \cos u] \right) \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\frac{d\omega}{dt} = - \frac{d\Omega}{dt} \cos i + \frac{R}{he} \{ -\psi \cos\theta \bar{e}_R + (1 + \psi) \sin\theta \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

8. A derivation of $\frac{dr}{dt} \frac{p}{dt}$

$$\frac{dr}{dt} \frac{p}{dt} = \frac{d}{dt} \frac{p}{1 + e}$$

$$= \frac{1}{1 + e} \frac{dp}{dt} - \frac{p}{(1 + e)^2} \frac{de}{dt}$$

$$\begin{aligned}
&= 2 \frac{1}{1+e} \frac{Rp}{h} (\bar{\mathbf{e}}_L \cdot \bar{\mathcal{F}}) - \frac{p}{(1+e)^2} \frac{R}{h} \{ \psi \sin \theta \bar{\mathbf{e}}_R + \\
&\quad + [e + (1 + \psi) \cos \theta] \bar{\mathbf{e}}_L \} \cdot \bar{\mathcal{F}} \\
&= \frac{R}{h} \frac{p}{(1+e)^2} \{ 2(1+e)(\bar{\mathbf{e}}_L \cdot \bar{\mathcal{F}}) - \psi \sin \theta \bar{\mathbf{e}}_R - [e \\
&\quad + (1 + \psi) \cos \theta] \bar{\mathbf{e}}_L \} \cdot \bar{\mathcal{F}} \\
&= \frac{R}{h} \frac{p}{(1+e)^2} \left\{ (2(1+e) - [e + (1 + \psi) \cos \theta]) \bar{\mathbf{e}}_L - \psi \sin \theta \bar{\mathbf{e}}_R \right\} \cdot \bar{\mathcal{F}}
\end{aligned}$$

$$\frac{dr_p}{dt} = \frac{R}{h} \frac{p}{(1+e)^2} \{ -\psi \sin \theta \bar{\mathbf{e}}_R + [2(1 - \cos \theta) + e \sin^2 \theta] \bar{\mathbf{e}}_L \} \cdot \bar{\mathcal{F}}$$

9. A derivation of $\frac{dr_a}{dt}$

$$\begin{aligned}
\frac{dr_a}{dt} &= \frac{d}{dt} \left(\frac{p}{1-e} \right) \\
&= \frac{1}{1-e} \frac{dp}{dt} + \frac{p}{(1-e)^2} \frac{de}{dt} \\
&= \frac{2}{1-e} \frac{pR}{h} (\bar{\mathbf{e}}_L \cdot \bar{\mathcal{F}}) + \frac{p}{(1-e)^2} \frac{R}{h} \{ [e + (1 + \psi) \cos \theta] \bar{\mathbf{e}}_L \\
&\quad + \psi \sin \theta \bar{\mathbf{e}}_R \} \cdot \bar{\mathcal{F}}
\end{aligned}$$

$$= \frac{pR}{h(1-e)^2} \{ 2(1-e) \bar{e}_L + [e + (1+\psi) \cos\theta] \bar{e}_L + \psi \sin\theta \bar{e}_R \} \cdot \bar{\mathcal{F}}$$

$$= \frac{pR}{h(1-e)^2} \{ [2(1-e) + e + (1+\psi) \cos\theta] \bar{e}_L + \psi \sin\theta \bar{e}_R \} \cdot \bar{\mathcal{F}}$$

$$= \frac{pR}{h(1-e)^2} \{ [(2-e) + (1+\psi) \cos\theta] \bar{e}_L + \psi \sin\theta \bar{e}_R \} \cdot \bar{\mathcal{F}}$$

$$\frac{dr_a}{dt} = \frac{pR}{h(1-e)^2} \{ \psi \sin\theta \bar{e}_R + [2(1+\cos\theta) - e \sin^2\theta] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

B. The description and substitution of $\bar{\mathcal{F}}$ in the decay equations $\frac{d\lambda}{dt}$

Define $\bar{\mathcal{F}}$ as follows:

$$\bar{\mathcal{F}} = \bar{\mathcal{F}}_G + \bar{\mathcal{F}}_D + \bar{\mathcal{F}}_S$$

Where $\bar{\mathcal{F}}_G$ is the gravitational perturbing force due to earth oblateness

$\bar{\mathcal{F}}_D$ is the perturbing force due to drag

$\bar{\mathcal{F}}_S$ is the perturbing force due to solar radiation pressure

$$\bar{\mathcal{F}}_G = \frac{\mu}{R^2} \sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N \{ (N+1) P_N \bar{e}_R - P'_N [\cos i \bar{e}_h + \sin i \cos u \bar{e}_L] \}$$

R_{eq} = earth's equatorial radius

R, β are the geocentric radius and latitude of the satellite

$P_N(\sin\beta)$ is the N^{th} Legendre polynomial

J_N are empirically determined constants

$$P'_N = \frac{\partial}{\partial \sin\beta} (P_N \sin\beta)$$

$$\bar{\mathcal{F}}_D = -\frac{\mu\rho B}{p} [1 + e^2 + 2e\cos\theta]^{\frac{1}{2}} \left[[1 + e\cos\theta] \bar{e}_L + e\sin\theta \bar{e}_R \right]$$

$$B = \frac{C_D A}{2m}$$

A = reference area

m = mass of satellite

C_D = drag coefficient

$$\bar{\mathcal{F}}_S = -\frac{A}{m} \text{Pr} [L \bar{e}_R + M \bar{e}_L + N \bar{e}_h]$$

$$\begin{pmatrix} L \\ M \\ N \end{pmatrix} = \begin{bmatrix} \cos u \cos \Omega - \sin u \cos i \sin \Omega & \cos u \sin \Omega + \sin u \cos i \cos \Omega \\ -\sin u \cos \Omega - \cos u \cos i \sin \Omega & -\sin u \sin \Omega + \cos u \cos i \cos \Omega \\ \sin i \sin \Omega & -\sin i \cos \Omega \end{bmatrix}$$

$$\begin{bmatrix} \sin u \sin i \\ \cos u \sin i \\ \cos i \end{bmatrix} \begin{bmatrix} l_S \\ m_S \\ n_S \end{bmatrix}$$

l_S, m_S, n_S are the direction cosines of the sun

P_R = solar radiation pressure

A reference area

$$P_2 = \frac{1}{2} (3\sin^2\beta - 1) = \frac{1}{2} (3\sin^2i \sin^2u - 1)$$

$$P_3 = \frac{1}{2} (5\sin^3\beta - 3\sin\beta) = \frac{1}{2} (5\sin^3i \sin^3u - 3\sin i \sin u)$$

$$P'_2 = 3\sin\beta = 3\sin i \sin u$$

$$P'_3 = \frac{3}{2} (5\sin^2\beta - 1) = \frac{3}{2} (5\sin^2i \sin^2u - 1)$$

1. Substitution of the above expression for $\bar{\mathcal{F}}$ in the $\frac{d\lambda}{dt}$

$$\frac{di}{dt} = \frac{R}{h} \cos u (\bar{\mathcal{F}} \cdot \bar{e}_h)$$

$$\frac{di}{d\theta} = \frac{R^3}{h^2} \cos u (\bar{\mathcal{F}} \cdot \bar{e}_h)$$

$$\frac{di}{d\theta} = \frac{R^3}{h^2} \cos u (\bar{\mathcal{F}}_G + \bar{\mathcal{F}}_D + \bar{\mathcal{F}}_S) \cdot \bar{e}_h$$

$$\bar{\mathcal{F}}_G \cdot \bar{e}_h = -\frac{\mu}{R^2} \sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N P'_N \cos i$$

$$\bar{\mathcal{F}}_D \cdot \bar{e}_h = 0$$

$$\bar{\mathcal{F}}_S \cdot \bar{e}_h = -\frac{A}{m} P_R N$$

$$\begin{aligned}
\frac{di}{d\theta} &= \frac{R^3}{h^2} \cos u \left\{ -\frac{\mu}{R^2} \cos i \sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N P'_N - \frac{A}{m} P_{RN} \right\} \\
&= \frac{R^3}{h^2} \cos u \left\{ -\frac{\mu}{R^2} \cos i \left[J_2 \left(\frac{R_{eq}}{R} \right)^2 P'_2 + J_3 \left(\frac{R_{eq}}{R} \right)^3 P'_3 \right] - \frac{A}{m} P_{RN} \right\} \\
&= \frac{R^3}{h^2} \cos u \left\{ -\frac{\mu}{R^2} \cos i \left[3J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin i \sin u + \frac{3}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 (5\sin^2 i \sin^2 u \right. \right. \\
&\quad \left. \left. - 1) \right] - \frac{A}{m} P_{rN} \right\} \\
&= -\frac{3\mu J_2}{Rh^2} \cos u \sin u \cos i \sin i R_{eq}^2 - \frac{15}{2} \frac{\mu J_3}{h^2 R^2} \cos u \sin^2 u \sin^2 i \cos i R_{eq}^3 \\
&\quad + \frac{3}{5} \frac{\mu}{h^2 R^2} J_3 \cos u \cos i R_{eq}^3 - \frac{P_{AN}}{mh^2} R^3 \cos u
\end{aligned}$$

$$\begin{aligned}
\frac{di}{d\theta} &= -\frac{3J_2}{p^2} R_{eq}^2 \cos i \sin i \cos u \sin u [1 + e \cos \theta] \\
&= \frac{15}{2p^3} J_3 R_{eq}^3 \sin^2 i \cos i \cos u \sin^2 u [1 + e \cos \theta]^2 \\
&\quad + \frac{3}{2} \frac{J_3}{p^3} R_{eq}^3 \cos i \cos u [1 + e \cos \theta]^2 - \frac{ANR^3}{mh^2} \cos u P_r
\end{aligned}$$

Define \tilde{i} so that $\tilde{i} = i - \Delta i$ where Δi is the purely periodic portion of i . A characteristic of any periodic function is that its derivative is also periodic. The only portion of the above expression that is not necessarily periodic is the term involving solar radiation pressure, P_r . I.e. P_r is assumed to have a constant positive value in sunlight and a value of zero in the earth's shadow.

The process of removing the periodic portions of the $\frac{d\lambda}{dt}$ is done by averaging in the following way:

$$\frac{d\tilde{\lambda}}{dt} = \frac{1}{4\pi^2} \int_0^{2\pi} \int_0^{2\pi} \left[\frac{d\lambda}{dt} \right]_G d\theta d\omega$$

It is easily shown that terms containing $\sin^N u$, $\cos^N u$, $\sin^N u \cos^N u$, N ODD will vanish over $[0, 2\pi]$ when averaged in the above manner. This aid then makes the integration a process of inspection.

$$\frac{d\tilde{i}}{d\theta} = - \frac{ANR^3 P_r \cos u}{mh^2}$$

$$\frac{d\tilde{i}}{dt} = \frac{di}{d\theta} \frac{\mu^{\frac{1}{2}}}{a^{\frac{3}{2}}}$$

$$\frac{d\tilde{i}}{dt} = - \frac{ANR^3 P_r \cos u}{m\mu a (1 - e^2)} \frac{\mu^{\frac{1}{2}}}{a^{\frac{3}{2}}}$$

$$\frac{d\tilde{i}}{dt} = - \frac{ANR^3 P_r \cos u}{m\mu^{\frac{1}{2}} a^{\frac{5}{2}} (1 - e^2)}$$

$$2. \text{ Derivation of } \frac{d\tilde{\Omega}}{dt}$$

$$\frac{d\Omega}{dt} = \frac{R}{h} \frac{\sin u}{\sin i} (\vec{\mathcal{F}} \cdot \vec{e}_h)$$

$$\frac{d\Omega}{d\theta} = \frac{R^3}{h^2} \frac{\sin u}{\sin i} (\vec{\mathcal{F}} \cdot \vec{e}_h)$$

$$\frac{d\Omega}{d\theta} = \frac{R^3}{h^2} \frac{\sin u}{\sin i} (\bar{\mathcal{F}}_G + \bar{\mathcal{F}}_D + \bar{\mathcal{F}}_S) \cdot \bar{e}_h$$

$$\left. \begin{array}{l} \bar{\mathcal{F}}_G \cdot \bar{e}_h \\ \bar{\mathcal{F}}_D \cdot \bar{e}_h \\ \bar{\mathcal{F}}_S \cdot \bar{e}_h \end{array} \right\} \text{ are the same expressions as given in } \frac{di}{dt}$$

On substitution then the expression for $\frac{d\Omega}{d\theta}$ becomes

$$\frac{d\Omega}{d\theta} = \frac{R^3}{h^2} \frac{\sin u}{\sin i} \left\{ -\frac{\mu}{R^2} \cos i \left[3J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin i \sin u \right. \right. \\ \left. \left. + \frac{3}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 (5\sin^2 i \sin^2 u - 1) \right] - \frac{A}{m} P_r N \right\}$$

$$\frac{d\Omega}{d\theta} = \frac{3J_2 R_{eq}^2}{p^2} \cos i \sin^2 u [1 + e \cos \theta] - \frac{15J_3}{2p^3} R_{eq}^3 \sin i \cos i \sin^3 u [1 \\ + e \cos \theta]^2 + \frac{3}{2} \frac{J_3}{p^3} R_{eq}^3 \csc i \sin u [1 + e \cos \theta]^2 - \frac{ANR^3}{mh^2 \sin i} \sin u P_r$$

Averaging as before, only the first term of the above expression will remain since it contains a secular term. The term involving solar radiation pressure is retained

$$\frac{d\Omega}{d\theta} = -\frac{3}{p^2} J_2 R_{eq}^2 \cos i \left\{ \frac{1}{2} \cdot \frac{1}{2} + \frac{1}{2} \cdot \frac{1}{2} \right\} - \frac{ANR^3 \sin u P_r}{mh^2 \sin i}$$

$$\frac{d\tilde{\Omega}}{d\theta} = -\frac{3}{2} \frac{J_2}{p^2} R_{eq}^2 \cos i - \frac{AMR^3 \sin u P_r}{mh^2 \sin i}$$

$$\frac{d\tilde{\Omega}}{d\theta} = -\frac{3}{2} J_2 \cos i - \frac{ANR^3 \sin u P_r}{mh^2 \sin i}, \quad \bar{J}_2 = J_2 \left(\frac{R_{eq}}{p} \right)^2$$

$$\frac{d\tilde{\Omega}}{dt} = -\frac{3}{2} \frac{\mu^{\frac{1}{2}}}{a^{\frac{3}{2}}} \bar{J}_2 \cos i - \frac{ANR^3 \sin u}{m\mu^{\frac{1}{2}} a^{\frac{5}{2}} (1-e^2) \sin i}$$

3. Derivation of $\frac{d\tilde{\omega}}{dt}$

$$\frac{d\omega}{dt} = -\frac{d\Omega}{dt} \cos i + \frac{R}{eh} \{ -\psi \cos \theta \bar{e}_R + (1+\psi) \sin \theta \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\frac{d\omega}{dt} = -\frac{d\Omega}{dt} \cos i + \frac{R}{eh} \{ -\psi \cos \theta \bar{e}_R + (1+\psi) \sin \theta \bar{e}_L \} \cdot (\bar{\mathcal{F}}_G + \bar{\mathcal{F}}_D + \bar{\mathcal{F}}_S)$$

$$\bar{e}_R \cdot \bar{\mathcal{F}}_G = \frac{\mu}{R^2} \sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N (N+1) P_N$$

$$\bar{e}_L \cdot \bar{\mathcal{F}}_G = -\frac{\mu}{R^2} \sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N P_N' \sin i \cos u$$

$$\bar{e}_R \cdot \bar{\mathcal{F}}_D = -\frac{\mu e \rho B}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \sin \theta$$

$$\bar{e}_L \cdot \bar{\mathcal{F}}_D = -\frac{\mu \rho B}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 + e \cos \theta]$$

$$\bar{e}_R \cdot \bar{f}_S = -\frac{A}{m} P_R L$$

$$\bar{e}_L \cdot \bar{f}_S = -\frac{A}{m} P_R M$$

$$\frac{d\omega}{dt} = -\frac{d\Omega}{dt} \cos i - \frac{R}{eh} \psi \cos \theta \left(\bar{e}_R \cdot \bar{f}_G + \bar{e}_R \cdot \bar{f}_D + \bar{e}_R \cdot \bar{f}_S \right)$$

$$+ \frac{R}{eh} (1 + \psi) \sin \theta \left(\bar{e}_L \cdot \bar{f}_G + \bar{e}_L \cdot \bar{f}_D + \bar{e}_L \cdot \bar{f}_S \right)$$

$$\frac{d\omega}{dt} = -\frac{d\Omega}{dt} \cos i - \frac{R\psi \cos \theta}{eh} \left\{ \frac{\mu}{R^2} \sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N (N+1) P_N \right.$$

$$\left. - \frac{\mu e \rho B}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \sin \theta - \frac{A}{m} P_R L \right\} +$$

$$+ \frac{R(1 + \psi) \sin \theta}{eh} \left\{ - \frac{\mu}{R^2} \sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N P_N' \sin i \cos u \right.$$

$$\left. - \frac{\mu \rho B}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 + e \cos \theta] - \frac{A}{m} P_R M \right\}$$

$$\sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^{N+1} (N+1) P_N = 3J_2 \left(\frac{R_{eq}}{R} \right)^2 \left(\frac{1}{2} \right) (3\sin^2 i \sin^2 u - 1)$$

$$\begin{aligned}
& + 4J_3 \left(\frac{R_{eq}}{R} \right)^3 \left(\frac{1}{2} \right) (5\sin^3 i \sin^3 u - 5\sin i \sin u) \\
& = \frac{9}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin^2 u - \frac{3}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 + 10J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^3 u \\
& \quad - 6J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \sin u
\end{aligned}$$

$$\begin{aligned}
\sum_{N=2}^3 J_N \left(\frac{R_{eq}}{R} \right)^N P'_N \sin i \cos u &= 3J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin u \cos u \\
&+ \frac{15}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^2 u \cos u - \frac{3}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \cos u
\end{aligned}$$

$$\frac{d\omega}{d\theta} = \frac{d\omega}{dt} \frac{dt}{d\theta} = \frac{R^2}{h} \frac{d\omega}{dt}$$

$$\begin{aligned}
\frac{d\omega}{d\theta} &= -\frac{d\Omega}{d\theta} \cos i - \frac{\mu R^3 \psi \cos \theta}{eh^2} \frac{1}{R^2} \left[\frac{9}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin^2 u - \frac{3}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 \right. \\
&\quad \left. + 10J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^3 u - 6J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \sin u \right] \\
&\quad - \frac{e\rho B}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \sin \theta - \frac{AP_r L}{m\mu} \Bigg\} \\
&+ \frac{\mu R^3 (1 + \psi)}{eh^2} \sin \theta \left\{ \frac{1}{R^2} \left[-3J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin u \cos u \right. \right. \\
&\quad \left. \left. - \frac{15}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^2 u \cos u + \frac{3}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \cos u \right] \right\}
\end{aligned}$$

$$\begin{aligned}
& - \frac{\rho B}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 + e \cos \theta] - \frac{AP_r M}{\mu m} \Bigg\} \\
\frac{d\omega}{d\theta} = & - \frac{d\Omega}{d\theta} \cos i - \frac{\cos \theta}{e} \left\{ \frac{9}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin^2 u - \frac{3}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 \right. \\
& + 10 J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^3 u - 6 J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \sin u \\
& - \frac{e \rho B R^2}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \sin \theta - \frac{AP_r L R^2}{m \mu} \Bigg\} \\
& + \frac{\sin \theta}{\psi e} \left\{ - 3 J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \cos u - \frac{15}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^2 u \cos u \right. \\
& + \frac{3}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \cos u - \frac{\rho B R^2}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 + e \cos \theta] \\
& - \frac{AP_r M R^2}{\mu m} \Bigg\} + \frac{\sin \theta}{e} \left\{ - 3 J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin u \cos u \right. \\
& - \frac{15}{2} J_2 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^2 u \cos u + \frac{3}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \cos u \\
& - \frac{\rho B R^2}{p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 + e \cos \theta] - \frac{AP_r M R^2}{\mu m} \Bigg\}
\end{aligned}$$

For convenience the effects due to the three perturbing forces will be considered separately below. For $\left[\frac{d\omega}{d\theta} \right]_G$ only the first, second and third terms of the expression remain, and become

$$\left[\frac{d\tilde{\omega}}{d\theta} \right]_G = \frac{3}{2p^2} J_2 R_{eq}^2 \cos^2 i - \frac{9}{4p^2} J_2 R_{eq}^2 \sin^2 i + \frac{3}{2p^2} J_2 R_{eq}^2$$

$$\left[\frac{d\tilde{\omega}}{d\theta} \right]_G = \frac{3}{2} \bar{J}_2 \cos^2 i - \frac{9}{4} \bar{J}_2 \sin^2 i + \frac{3}{2} J_2$$

$$\left[\frac{d\tilde{\omega}}{d\theta} \right]_G = \frac{3}{4} \bar{J}_2 [4 - 5\sin^2 i]$$

$$\frac{d\tilde{\omega}}{dt} = \frac{\mu^{\frac{1}{2}}}{a^{\frac{3}{2}}} \frac{d\tilde{\omega}}{d\theta}$$

$$\left[\frac{d\tilde{\omega}}{dt} \right]_G = \frac{3\mu^{\frac{1}{2}}}{4a^{\frac{3}{2}}} \bar{J}_2 [4 - 5\sin^2 i]$$

The effects due to drag become

$$\left[\frac{d\omega}{d\theta} \right]_D = \frac{\rho B R^2 \sin \theta}{ep} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \{e \cos \theta - 1 - (1 + e \cos \theta)\}$$

$$\left[\frac{d\omega}{d\theta} \right]_D = \frac{\rho B R^2 \sin \theta}{ep} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} (-2)$$

$$\left[\frac{d\omega}{d\theta} \right]_D = - \frac{2\rho B R^2}{ep} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \sin \theta$$

$$\left[\frac{d\omega}{dt} \right]_D = - \frac{2\rho B \mu^{\frac{1}{2}} a^{\frac{1}{2}} (1 - e^2)^2}{e a (1 - e^2)} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \sin \theta$$

$$\left[\frac{d\omega}{dt} \right]_D = - \frac{2\rho B \mu^{\frac{1}{2}} (1 - e^2)}{e a^{\frac{1}{2}}} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \sin \theta$$

$\left[\frac{d\omega}{dt} \right]_D$ will vanish over $[0, 2\pi]$ if we consider $\rho = \rho(R)$ to be an even function of θ . Thus $\left[\frac{d\omega}{dt} \right]_D = 0$.

The effects of solar radiation pressure remain

$$\left[\frac{d\omega}{d\theta} \right]_S = \frac{A P_r L R^2 \cos \theta}{\mu m e} - \frac{A P_r M R^2 \sin \theta}{\mu m \psi e} - \frac{A P_r M R^3 \sin \theta}{\mu m e}$$

$$\left[\frac{d\omega}{d\theta} \right]_S = \frac{A P_r R^2}{\mu m e} \left[L \cos \theta - \frac{M \sin \theta}{1 + e \cos \theta} - M \sin \theta \right]$$

$$\left[\frac{d\omega}{dt} \right]_S = \frac{A P_r R^2}{\mu^{\frac{1}{2}} a^{\frac{3}{2}} m e} \left[L \cos \theta - \frac{M \sin \theta}{1 + e \cos \theta} - M \sin \theta \right]$$

$$\frac{d\tilde{\omega}}{dt}_S = \frac{3}{4} \frac{\mu^{\frac{1}{2}}}{a^{\frac{3}{2}}} \mathcal{J}_2 [4 - 5 \sin^2 i] + \frac{A P_r R^2}{m \mu^{\frac{1}{2}} a^{\frac{3}{2}} e} \left[L \cos \theta - \frac{M \sin \theta}{1 + e \cos \theta} - M \sin \theta \right]$$

4. Derivation of $\frac{d\tilde{r}_p}{dt}$

$$\frac{dr_p}{dt} = - \frac{r_p^2}{p} \frac{R}{h} \{ \psi \sin \theta \bar{e}_R - [2(1 - \cos \theta) + e \sin^2 \theta] \bar{e}_L \} \cdot \bar{\mathcal{F}}$$

$$\frac{dr_p}{d\theta} = - \frac{r_p^2}{p} \frac{R^3}{h^2} \{ \psi \sin \theta \bar{e}_R \cdot (\bar{\mathcal{F}}_G + \bar{\mathcal{F}}_D + \bar{\mathcal{F}}_S) - [2(1 - \cos \theta)$$

$$+ e \sin^2 \theta] \bar{e}_L \cdot (\bar{\mathcal{F}}_G + \bar{\mathcal{F}}_D + \bar{\mathcal{F}}_S) \}$$

$$\left[\frac{dr_p}{d\theta} \right]_G = - \frac{r^2 R^3}{ph^2} \{ \psi \sin \theta (\bar{e}_R \cdot \bar{\mathcal{F}}_G) - [2(1 - \cos \theta) + e \sin^2 \theta] \bar{e}_L \cdot \bar{\mathcal{F}}_G \}$$

$$\begin{aligned} \left[\frac{dr_p}{d\theta} \right]_G = - \frac{\mu r^2 R}{ph^2} & \left\{ \sin \theta \left[\frac{9}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin^2 u - \frac{3}{2} J_2 \left(\frac{R_{eq}}{R} \right)^2 \right. \right. \\ & + 10 J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^3 u - 6 J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin i \sin u \left. \right] \\ & + \left[2(1 - \cos \theta) + e \sin^2 \theta \right] \left[3 J_2 \left(\frac{R_{eq}}{R} \right)^2 \sin^2 i \sin u \cos u \right. \\ & \left. \left. + \frac{15}{2} J_3 \left(\frac{R_{eq}}{R} \right)^3 \sin^3 i \sin^2 u \cos u \right] \right\} \end{aligned}$$

On integration of the above expression for $\left[\frac{dr_p}{d\theta} \right]_G$ all terms will vanish due to the odd powers of the trigonometric terms involving u

$$\left[\frac{dr_p}{dt} \right]_D = - \frac{r^2 R}{ph} \{ \psi \sin \theta (\bar{e}_R \cdot \bar{\mathcal{F}}_D) - [2(1 - \cos \theta) + e \sin^2 \theta] (\bar{e}_L \cdot \bar{\mathcal{F}}_D) \}$$

The drag effects $\left[\frac{dr_p}{dt} \right]_D$ are

$$\left[\frac{dr_p}{dt} \right]_D = - \frac{\mu r_p^2 R \rho B}{h p^2} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \{ -\psi \sin^2 \theta + [2(1 - \cos \theta) + e \sin^2 \theta] \}$$

$$\left[\frac{dr_p}{dt} \right]_D = - \frac{\mu r_p^2 R \psi \rho B}{h p^2} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [2(1 - \cos \theta)]$$

$$\left[\frac{dr_p}{dt} \right]_D = - \frac{2\mu r_p^2 \rho B}{h p} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 - \cos \theta]$$

$$\left[\frac{dr_p}{dt} \right]_D = - \frac{2\mu^{\frac{1}{2}} r_p^2 \rho B}{a^{\frac{3}{2}} (1 - e^2)^{\frac{3}{2}}} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 - \cos \theta]$$

$$\left[\frac{dr_p}{dt} \right]_S = - \frac{r_p^2 R}{p h} \{ \psi \sin \theta (\bar{e}_R \cdot \bar{f}_S) - [2(1 - \cos \theta) + e \sin^2 \theta] (\bar{e}_L \cdot \bar{f}_S) \}$$

$$\left[\frac{dr_p}{dt} \right]_S = - \frac{r_p^2 R}{p h} \left\{ - \frac{\psi \sin \theta A P_r L}{m} + [2(1 - \cos \theta) + e \sin^2 \theta] \frac{A P_r M}{m} \right\}$$

$$\left[\frac{dr_p}{dt} \right]_S = - \frac{r_p^2 A P_r}{\mu^{\frac{1}{2}} a^{\frac{1}{2}} (1 - e^2)^{\frac{1}{2}} m} \left\{ -L \sin \theta + \frac{[2(1 - \cos \theta) + e \sin^2 \theta] M}{[1 + e \cos \theta]} \right\}$$

Hence the final expression for $\frac{d\tilde{r}_p}{dt}$ is

$$\frac{d\tilde{r}_p}{dt} = - \frac{2\mu^{\frac{1}{2}} r_p^2 \rho B [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}}}{a^2 (1 - e^2)^{\frac{3}{2}}} [1 - \cos \theta]$$

$$- \frac{r_p^2 A P_r}{m \mu^{\frac{1}{2}} a^2 (1 - e^2)^{\frac{1}{2}}} \left\{ -L \sin \theta + \frac{[2(1 - \cos \theta) + e \sin^2 \theta] M}{1 + \cos \theta} \right\}$$

5. Derivation of $\frac{dr_a}{dt}$

$$\frac{dr_a}{dt} = \frac{r_a^2 R}{hp} \{ \psi \sin \theta \bar{e}_R + [2(1 + \cos \theta) - e \sin^2 \theta] \bar{e}_L \} \cdot \bar{f}$$

$$\left[\frac{dr_a}{dt} \right]_G = \frac{r_a^2 R}{hp} \{ \psi \sin \theta (\bar{e}_R \cdot \bar{f}_G) + [2(1 + \cos \theta) - e \sin^2 \theta] (\bar{e}_L \cdot \bar{f}_G) \}$$

Since the above expression is identical to $\left[\frac{dr_p}{d\theta} \right]_G$ insofar as trigonometric terms are involved, it vanishes over $[0, 2\pi]$ in the same manner.

$$\left[\frac{dr_a}{dt} \right]_D = - \frac{\mu r_a^2 \rho B}{hp^2} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} \{ \psi e \sin^2 \theta + [2(1 + \cos \theta) - e \sin^2 \theta] \psi \}$$

$$\left[\frac{dr_a}{dt} \right]_D = - \frac{\mu r_a^2 \rho B}{hp} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [2(1 + \cos \theta)]$$

$$\left[\frac{dr_a}{dt} \right]_D = - \frac{2\mu^{\frac{1}{2}} r_a^2 \rho_B}{a^{\frac{3}{2}} (1 - e^2)^{\frac{3}{2}}} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 + \cos \theta]$$

$$\left[\frac{dr_a}{dt} \right]_S = \frac{r_a^2 R}{h p} \{ \psi \sin \theta (\bar{e}_R \cdot \bar{f}_S) + [2(1 + \cos \theta) - e \sin^2 \theta] (\bar{e}_L \cdot \bar{f}_S) \}$$

$$\left[\frac{dr_a}{dt} \right]_S = \frac{r_a^2 R}{h p} \left\{ \psi \sin \theta \left(- \frac{AP_r L}{m} \right) + [2(1 + \cos \theta) - e \sin^2 \theta] \left(- \frac{AP_r M}{m} \right) \right\}$$

$$\left[\frac{dr_a}{dt} \right]_S = - \frac{r_a^2 AP_r}{m \mu^{\frac{1}{2}} a^{\frac{3}{2}} (1 - e^2)^{\frac{3}{2}}} \left\{ L \sin \theta + \frac{M [2(1 + \cos \theta) - e \sin^2 \theta]}{[1 + e \cos \theta]} \right\}$$

Hence the final expression for $\frac{d\tilde{r}_a}{dt}$ is

$$\begin{aligned} \frac{d\tilde{r}_a}{dt} &= - \frac{2\mu^{\frac{1}{2}} r_a^2 \rho_B}{a^{\frac{3}{2}} (1 - e^2)^{\frac{3}{2}}} [1 + e^2 + 2e \cos \theta]^{\frac{1}{2}} [1 + \cos \theta] \\ &\quad - \frac{r_a^2 AP_r}{m \mu^{\frac{1}{2}} a^{\frac{3}{2}} (1 - e^2)^{\frac{3}{2}}} \left\{ L \sin \theta + \frac{M [2(1 + \cos \theta) - e \sin^2 \theta]}{1 + e \cos \theta} \right\} \end{aligned}$$

APPENDIX B

COMPUTER PROGRAM SOURCE LISTING

KILGØ HPC	06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	
INTERNAL FORMULA NUMBER(S)		
1001	BETA=TAN2PI((CL,CM)-TAN2PI((CLS,CMS)-180.*GAMMA/PI	#110
2002	IF(BETA) 2000,2001,2001	#111
2000	BETA=BETA*260.	#112
	GØ TØ 2002	#113
2001	CØNTINUE	#114
700	AMP=HKM/4000.+(.91+.44*SIG+.38*SIG2)*EXP (-(2.-HKM/(405.+143.*SIG	
	1)**2)	#115
710	AMPS=.245+.0425*SIG-.0625*SIG2	#116
	U=AMP*[-.08*EXP (-(BETA-250.)/55.))**2)+AMPS*EXP (-(BETA-135.)/	
	134.))**2))+AMP*4.E-6*BETA	#117
	FACT=1.+(1.-CN**2)*L	#118
	RHØA=RHØA*FACT	#119
3000	RETURN	#120
	END	#121

KILGØ TAN2PI	06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	
INTERNAL FORMULA NUMBER(S)		
	FUNCTION TAN2PI(X,Y)	
C	TAN2PI=ARCTAN(Y/X)	C985
C	TAN2PI EQUAL ØR LESS THAN 2PI	C986
C	TAN2PI EQUAL ØR GREATER THAN ZERO	C987
	RADDEG=57.2957795	C988 #1
	IF(Y)1,2,3	C989 #2
2	IF(X)5,4,6	C990 #3
4	TAN2PI=1.0E+30	C991 #4
	GØ TØ 20	C992 #5
5	TAN2PI=180.0	C993 #6
	GØ TØ 20	C994 #7
6	TAN2PI=0.0	C995 #8
	GØ TØ 20	C996 #9
1	IF(X)7,8,9	C997 #10
7	TAN2PI=180.+RADDEG*ATAN(Y/X)	#11
	GØ TØ 20	C999 #12
8	TAN2PI=270.0	C9991 #13
	GØ TØ 20	C9992 #14
9	TAN2PI=360.+RADDEG*ATAN(Y/X)	#15
	GØ TØ 20	C999C #16
3	IF(X)7,10,11	C999E #17
10	TAN2PI=90.0	C999F #18
	GØ TØ 20	C999I #19
11	TAN2PI=RADDEG*ATAN(Y/X)	#20
20	RETURN	C999H #21
	END	C999J #22

```

REAL IØMET, MASS, INTERA, INTERP
DIMENSION FTENB(153), FTEN(153), AP(153)
DIMENSION MAT1(9), MAT2(9), MAT3(9), EFP(8), EFE(8), SFE(8),
1SFG(8), EFG(8), ØET(8), ØEM(8), ØEE(8), MØT(8), MØM(8), MØE(8), AMAT(9),
1BMAT(9), CMAT(9), A1MAT(9), W1MAT(9), WMAT(9), TEMP(20), IØMET(2),
1SYIC(13), PLT(8), WDØMAT(9), WDMAT(9), WSUB1(9), WSUB1T(9)
DIMENSION COPRIM(25),
1ATTACK(45), CN(45), AREA(45), MASS(25), INTERA(6), INTERP(6),
1DAPØGE(10), CDA(50), CUTØFF(2), DATE(3), CØRREC(110)
DOUBLE PRECISION KERTH, KAPPA, PHIØ, LAMØ, AØ, BØ, ØMEGA, AE,
1JJ, FH, DD, TTT, THETA, RRR, PSI,
1LAMØ, VE, ALPV, EV, XS, YS, ZS, XDS, YDS, ZDS, AXIS, ECCEN, INC,
1ASNØD, ARGP, ANØM, ECANØM, MNANØM, XE, YE, ZE, XDE, YDE, ZDE, XEP, YEP, ZEP,
1XDEP, YDEP, ZDEP, XP, YP, ZP, VP, ALPP, EP, RPHIØ, RLAMØ, RØMEGA, RPSIØ, RO,
1BETA, AMAT, BMAT, CMAT, A1MAT, WMAT, W1MAT, RKAPPA, RTHETA, XEC, YEC, ZEC,
1TEMP, RRRE, PSIE, LAMDE, VEE, AUPVE, EVB, MAT1, MAT2, MAT3, EFP, EFE, SFE, SFG,
1EFG, ØET, ØEM, ØEE, MØT, MØM, MØE, A1, A2, A3, C1, C3, LR, CØSE, SR, SN, C2V,
1B1, B2, B3, AXISØ, ECCB, INCB, ASNB, ARGB, ANMB, ECAB, MNAB,
1PITCH, RANGE, ALT, ECV, EEV, PERIGE, APØGEE, PERIØD, MVAPØG, MVPERG,
1MVPERD, BØMEG, LØMEG, PLT, XG, YG, ZG, XDG, YDG, ZDG, TFM
1, XPL, YPL, ZPL, XDPL, YCPL, ZDPL, WDØMAT, WDMAT, WSUB1, WSUB1T
DOUBLE PRECISION TØLX, DPR, RIE
COMMON/HBLK/KERTH, XAØ, XBØ, XAE, XJJ, XHH, XØD, XDANØM, XF, XPRINT,
1XATMØS, XDIURN, XLAG, XMVA, XMVP, XCØPM(25), XMASS(25),
2XATTK(45), XCN(45), XAREA(45), XINTA(6), XINTP(6), XDAPØ(10),
3XCD(50), XCUT(2), XXCAT(3), XCØR(110), XIN, XASN, XARG
4, XECLPT, XAMPR, XFTENB(153), XFTEN(153), XAP(153), XSA, XSR
COMMON/BLK/KERTH, AØ, BØ, AE, JJ, HH, DD, TTT, RRR, PSI, LAMØ, VE, ALPV,
1EV, XS, YS, ZS, XDS, YDS, ZDS, AXIS, ECCEN, INC, ASNØD, ARGP, ANØM, ECANØM,
1MNANØM, XE, YE, ZE, XDE, YDE, ZDE, XEP, YEP, ZEP, XDEP, YDEP, ZDEP, XP, YP, ZP,
1VP, ALPP, EP, RPHIØ, RLAMØ, RØMEGA, RPSIØ, RO, BETA, AMAT, BMAT, CMAT,
1LAMØ, KAPPA, ØMEGA, PHIØ, THETA, XG, YG, ZG, XDG, YDG, ZDG, TFM,
1XPL, YPL, ZPL, XEPL, YCPL, ZDPL, WDØMAT, WDMAT, WSUB1, WSUB1T,
1A1MAT, WMAT, W1MAT, RKAPPA, RTHETA, XEG, YEC, ZEC, TEMP, RRRE, PSIE, LAMDE,
1VEE, ALPVE, EVE, MAT1, MAT2, MAT3, A1, A2, A3, C1, C3, LR, CØSE, SR, SN, C2V,
1B1, B2, B3, AXISØ, ECCB, INCB, ASNB, ARGB, ANMB, ECAB, MNAB,
1SHØRT, XLØNG
DATA IØMET/6HSHØRT /, IØMET(2)/6HNLØNG/
DATA CN/6HALPHA /, CN(2)/1., CN(3)/360., CN(4)/6HEND /,
1CØPRIM/1., CØPRIM(2)/0., CØPRIM(3)/6HEND /, ATTACK/0.,
2ATTACK(2)/360., ATTACK(3)/6HEND /, AREA/6HALPHA /, AREA(2)
3/1., AREA(3)/360., AREA(4)/6HEND /, MASS/6HCØN /, MASS(2)
4/1., MASS(3)/C., DAPØGE/-20., DAPØGE(2)/C., PRINT/6HNRMAL/,
5ATMØS/6HARDC /, DIURNL/6HMEAN /, ECLIPT/23.4436/
DATA(CØRREC(1), I=1, 41)/
1 .12, 500., .13, 400., .142, 350., .184, 300., .22, 280., .275, 260.,
1.304, 250., .34, 240., .385, 230., .425, 220., .47, 210., .52, 200., .565,
1190., .62, 180., .7, 170., .8, 160., .84, 155., .86, 150., 1., 145., 1., 0.,
16HEND /
DATA (DATE(1), I=1, 3)/9., 18., 1964., SA/0./
DATA SØ/100./, AMPR/C./
DATA XG/0., YG/0., ZG/0., XDG/0., YDG/0., ZDG/0.,
1ZDG/0., TFM/0., XLAG/C./
DATA(DAPØGE(1), I=1, 10)/-5., .6778., .1C., .6578., -20., 0., 0., 0., 0., C./
DATA KERTH/358603.2CØ/

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KILGØ CNTRL	EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
1KAPPA/105.D0/,PHI0/28.5D0/,LAMD0/80.5D0/,A0/6378.165D0/,			
2B0/6356.784D0/,0MEGA/15.04106705D0/,AE/6378.165D0/,			
3JJ/.00162345D0/,HH/.000C0575D0/,DD/.000C7875D0/,			
4DAN0M/10./,F/298.3/,			
8		PRINT/6H0RML/,	
9INC/30./,W0/180./,CAP0/180./			
DATA(AP(I),I=1,141)/			
12.34,1958.,2.48,1958.8,1.89,1958.9,2.51,1959.,2.97,1959.1,2.42,			
21959.2,2.56,1959.3,2.59,1959.4,2.52,1959.5,3.16,1959.6,3.50,1959.7			
3,2.46,1959.8,2.89,1959.9,2.57,1960.,2.32,1960.1,2.44,1960.2,3.42,1			
1960.3,2.79,			
11960.4,2.92,1960.5,2.71,1960.6,2.75,1960.7,3.23,1960.8,3.44,1960.9			
1,2.49,1961.,2.27,1961.1,2.32,1961.2,2.29,1961.3,2.40,1961.4,2.69,1			
1961.5,2.26,			
11961.6,2.18,1961.7,1.85,1961.8,1.92,1961.9,1.49,1962.,1.73,1962.1,			
11.81,1962.2,2.31,1962.3,1.60,1962.4,2.18,1962.5,2.62,1962.6,2.94,1			
1962.7,3.08,			
11962.8,2.01,1962.9,1.75,1962.,1.72,1963.1,1.54,1963.12,1.51,1963.2			
11,1.86,1963.29,2.08,1963.38,2.06,1963.46,2.23,1963.54,2.35,1963.62			
1,3.26,			
11963.71,2.20,1963.75,2.02,1963.88,1.98,1963.96,2.06,1964.04,2.21,			
11964.12,2.16,1964.21,2.25,1964.29,1.81,1964.38,1.73,1964.46,1.89,			
11964.54,1.68,1964.62,1.78,1964.71,1.67,1964.79,.90,1964.88,.77,196			
14.96,2.5,1965.,2.5,2000.,6HEND			
DATA(RTENB(I),I=1,57)/			
1243.6,1958.,230.7,1958.5,226.5,1959.,208.9,1959.5,180.5,1960.,			
2161.,1960.5,130.8,1961.,104.8,1961.5,99.3,1962.,89.7,1962.5,			
382.7,1963.,80.8,1963.5,77.9,1964.,70.,1964.5,75.,1965.,			
487.,1965.5,131.,1966.5,186.,1967.5,200.,1968.5,190.,1969.5,			
5163.,1970.5,142.,1971.,128.,1971.5,108.,1972.5,94.,1973.5,			
681.,1974.5,75.,1975.,75.,1975.5,			
46HEND			
DATA (FTEN(I),I=1,3)/0.,0.,6HEND			
D0 1 I=1,8			11
FFP(I)=0.			12
EFE(I)=0.			13
SFE(I)=0.			14
SFG(I)=0.			15
PLT(I)=0.			16
FFG(I)=0.			17
DET(I)=0.			18
DEM(I)=0.			19
DEE(I)=0.			20
MOT(I)=0.			21
MOM(I)=0.			22
1 MOE(I)=0.			23
75 CALL MAVRIK(IERR,5KERTH,KERTH,5HKAPPA,KAPPA,4HPHI0,PHI0,			14
15HLAMD0,LAMD0,2HAE,A0,2H00,80,5H0MEGA,0MEGA,2HAE,AE,			
12HJJ,JJ,2HFF,H,2HCC,DD,5HI0MET,I0MET,3HEFP,EFP,3HEFE,EFE,			
13HSFE,SFE,3HSFG,SFG,3HEFG,EFG,3H0ET,0ET,3H0EM,0EM,			
13H0EE,0EE,3HM0T,M0T,3HM0M,M0M,3H0E,M0E,3HPLT,PLT,2HXC,XG,			
12HYC,YG,2HZG,ZG,3HXC,XDG,3HYDG,YDG,3HZDG,ZDG,3HTFM,TFM,			
15HDAN0M,DAN0M,1HF,F,6HCDPRIM,CDPRIM,6HATTACK,ATTACK,			
12HCN,CN,4HARE,AREA,4HMASS,MASS,6HINTER,INTER,			
16HINTER,INTER,6HCAPOGE,CAP0GE,3HCD,CDA,5HPRINT,PRINT,			
16HCUT0FF,CUT0FF,4HCATE,DATE,5HATM0S,ATM0S,6HC0RREC,C0RREC,			

KILGØ CNTRL 06/18/65
EXTERNAL FORMULA NUMBER - SOURCE STATEMENT - INTERNAL FORMULA NUMBER(S)

16HDIURNL,DIURNL,3HLAG,XLAG,4HFTEN,F TEN,5HFTENB,FTENB,2HKP,AP,			
16HECLIPT,ECLIPT,2HSA,SA,2HSØ,SØ,4HAMPR,AMPR)			
IF(IERR)76,77,76			
76 WRITE(6,78)			
78 FORMAT(1H017HCARD FORMAT ERROR)			
CALL PDUMP			
GØTØ75			
77 CØNTINUE			
IF(ØET.EQ.-0.)GØ TØ 4			
IF(ØET(2).GT.1.)GØ TØ 3			
DØ 2 I=3,8			
IF(ØET(1).NE.-0.)GØ TØ 200			
2 CØNTINUE			
MVAPØG=ØET*(1.+ØET(2))			
MVPERG=ØET*(1.-ØET(2))			
SWIT=1.			
GØ TØ 100			
3 DØ 300 I=3,8			
IF(ØET(1).NE.-0.)GØ TØ 301			
300 CØNTINUE			
MVAPØG=ØET			
MVPERG=ØET(2)			
SWIT=1.			
GØ TØ 100			
301 TEMP=(ØET+ØET(2))/2.			
ØET(2)=(ØET-ØET(2))/(ØET+ØET(2))			
ØET=TEMP			
GØTØ200			
4 IF(ØEM.EQ.-0.)GØ TØ 7			
IF(ØEM(2).GT.1.)GØTØ 6			
DØ 5 I=3,8			
IF(ØEM(1).NE.-0.)GØTØ 200			
5 CØNTINUE			
MVAPØG=ØEM*(1.+ØEM(2))			
MVPERG=ØEM*(1.-ØEM(2))			
SWIT=1.			
GØ TØ 100			
6 DØ 302 I=3,8			
302 CØNTINUE			
MVAPØG=ØEM			
MVPERG=ØEM(2)			
IF (ØEM(1).NE.-0.) GØ TØ 303			
SWIT=1.			
GØ TØ 100			
303 TEMP=(ØEM+ØEM(2))/2.			
ØEM(2)=(ØEM-ØEM(2))/(ØEM+ØEM(2))			
ØEM=TEMP			
GØTØ200			
7 IF(ØEE.EQ.-0.)GØ TØ 10			
IF(ØEE(2).GT.1.)GØTØ 9			
DØ 8 I=3,8			
IF(ØEE(1).NE.-0.)GØTØ200			
8 CØNTINUE			
MVAPØG=ØEE*(1.+ØEE(2))			
MVPERG=ØEE*(1.-ØEE(2))			
SWIT=1.			

KILG8 CNTRL		06/12/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	G0T0100	✓57	
9	D0 304 I=3,8	✓58	
	IF(0EE(1)).NE.-0.)G0T0305	✓59 ,100 ✓101	
304	C0NTINUE	✓102 ,103	
	MVAP0G=0EE	✓104	
	MVPERG=0EE(2)	✓105	
	SWIT=1.	✓106	
	G0T0100	✓107	
305	TEMP=(0EE+0EE(2))/2.	✓108	
	0EE(2)=(0EE-0EE(2))/(0EE+0EE(2))	✓109	
	0EE=TEMP	✓110	
	G0T0200	✓111	
10	IF(M0T.EQ.-0.)G0 T0 13	✓112 ,113 ✓114	
	IF(M0T(2).GT.1.)G0 T0 12	✓115 ,116 ✓117	
	D0 11 I=3,8	✓118	
	IF(M0T(1)).NE.-0.)G0T0200	✓119 ,120 ✓121	
11	C0NTINUE	✓122 ,123	
	MVAP0G=M0T*(1.+M0T(2))	✓124	
	MVPERG=M0T*(1.-M0T(2))	✓125	
	SWIT=1.	✓126	
	G0T0100	✓127	
12	D0 306 I=3,8	✓128	
	IF(M0T(1)).NE.-0.)G0T0307	✓129 ,130 ✓131	
306	C0NTINUE	✓132 ,133	
	MVAP0G=M0T	✓134	
	MVPERG=M0T(2)	✓135	
	SWIT=1.	✓136	
	G0T0100	✓137	
307	TEMP=(M0T+M0T(2))/2.	✓138	
	M0T(2)=(M0T-M0T(2))/(M0T+M0T(2))	✓139	
	M0T=TEMP	✓140	
	G0T0200	✓141	
13	IF(M0M.EQ.-0.)G0T0 16	✓142 ,143 ✓144	
	IF(M0M(2).GT.1.)G0T015	✓145 ,146 ✓147	
	D014 I=3,8	✓148	
	IF(M0M(1)).NE.-0.)G0T0200	✓149 ,150 ✓151	
14	C0NTINUE	✓152 ,153	
	MVAP0G=M0M*(1.+M0M(2))	✓154	
	MVPERG=M0M*(1.-M0M(2))	✓155	
	SWIT=1.	✓156	
	G0T0100	✓157	
15	D0 308 I=3,8	✓158	
	IF(M0M(1)).NE.-0.)G0T0309	✓159 ,160 ✓161	
308	C0NTINUE	✓162 ,163	
	MVAP0G=M0M	✓164	
	MVPERG=M0M(2)	✓165	
	SWIT=1.	✓166	
	G0T0100	✓167	
309	TEMP=(M0M+M0M(2))/2.	✓168	
	M0M(2)=(M0M-M0M(2))/(M0M+M0M(2))	✓169	
	M0M=TEMP	✓170	
	G0T0200	✓171	
16	IF(M0E.EQ.-0.)G0T0 200	✓172 ,173 ✓174	
	IF(M0E(2).GT.1.)G0T0 18	✓175 ,176 ✓177	
	D0 17 I=3,8	✓178	
	IF(M0E(1)).NE.-0.)G0T0200	✓179 ,180 ✓181	

KILGØ CNTRL	EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
17	CONTINUE		182, 183
	MVAPØG=MØE*(1.+MØE(2))		184
	MVPERG=MØE*(1.-MØE(2))		185
	SWIT=1.		186
	GØTØ100		187
18	DØ 310 I=3,8		188
	IF(MØE(1).NE.-0.)GØTØ311		189, 190, 191
310	CONTINUE		192, 193
	MVAPØG=MØE		194
	MVPERG=MØE(2)		195
	SWIT=1.		196
	GØTØ100		197
311	TEMP=(MØE+MØE(2))/2.		198
	MØE(2)=(MØE-MØE(2))/(MØE+MØE(2))		199
	MØE=TEMP		200
	GØTØ200		201
200	SWIT=0.		202
	CALL TRFM(KERTH,KAPPA,PHIØ,LAMDØ,AØ,BØ,ØMEGA,AE,JJ,HH,		
	IDD,IØMET,EFP,EFE,SFE,SFG,EFG,ØET,ØEM,ØEE,MØT,MØM,MØE,		
	IPLT,XG,YG,ZG,XDG,YDG,ZDG,TFM,MVAPØG,MVPERG,INCB,ASNB,ARCB)		
	MVAPØG=MVAPØG+AE		203
	MVPERG=MVPERG+AE		204
100	XKERTH=KERTH		205
	XAMPR=AMPR		206
	XAØ=AØ		207
	XBØ=BØ		208
	XAE=AB		209
	XJJ=JJ		210
	XHH=HH		211
	XSA=SA		212
	XSR=SØ		213
	XDD=DD		214
	XDANØM=DANØM		215
	XF=F		216
	XPRINT=PRINT		217
	XATMØS=ATMØS		218
	XDIURN=DIURNL		219
	XXLAG=XLAG		220
	XMVA=MVAPØG		221
	XMVP=MVPERG		222
	DØ 50 I=1,25		223
	XCDPM(I)=CDPRIM(I)		224
50	XMASS(I)=MASS(I)		225
	XECLPT=ECLIPT		226, 227
	DØ 60 I=1,153		228
	XFTENB(I)=FTENB(I)		229
	XFTEN(I)=FTEN(I)		230
60	XAP(I)=AP(I)		231
	DØ 51 I=1,45		232, 233
	XATTK(I)=ATTACK(I)		234
	XCN(I)=CN(I)		235
51	XAREA(I)=AREA(I)		236
	DØ 52 I=1,6		237, 238
	XINTAL(I)=INTERA(I)		239
52	XINTP(I)=INTERP(I)		240
	DØ 53 I=1,10		241, 242
			243

KILGB CNTRL		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
53	XDAP0(I)=DAP0GE(I)	,244	,245
	D0 54 I=1,50	,246	
54	XCCA(I)=CDA(I)	,247	,248
	XCUT=GUT0FF	,249	
	XCUT(2)=CUT0FF(2)	,250	
	D0 55 I=1,3	,251	
55	XXDAT(I)=DATE(I)	,252	,253
	D0 56 I=1,110	,254	
56	XCOR(I)=CORREC(I)	,255	,256
	IF(SWIT)57,57,58	,257	
57	XIN=INCB	,258	
	XASN=ASNB	,259	
	XARG=ARGB	,260	
	G0 T0 59	,261	
58	XIN=INC	,262	
	XASN=CAP0	,263	
	XARG=W0	,264	
59	CALL UIFE	,265	
	G0T0 75	,266	
	END	,267	

KILGØ LIFE 06A18Z65
EXTERNAL FORMULA NUMBER - SOURCE STATEMENT - INTERNAL FORMULA NUMBER(S)

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SUBROUTINE LIFE
REAL JJ,KERTH,INTA,INTP,MASS,MT,INTERA,INTERP,INC,NI
DIMENSION DATE(3),XM0NTH(12)
DIMENSION C0RREC(11C),S0LAR(3C1)
DIMENSION TN(6),INTERA(6),TNI(6),INTERP(6),
1C0SE(365),E(365),CCPRIM(25),AREA(45),CN(45),
2ATTACK(45),STAPA(365),STEPP(365),MASS(25)
DIMENSION FTENB(153),FTEN(153),API(153)
COMMON /ARCC/TEMPT,TEPK,PRESS,P0M0,
1PSP0,RH0,RH0SR0,VISC,VISC0L,KVISC,V0,G
DATA DPR/57.2957795/,PI/3.14159291/,SNBCI/6HSINE /
1,BCITIM/6HTIME /
DATA AID/6PA /,PID/6HP /,DETID/6HDETAIL/,
1SH0ID/6HSH0RT /
DATA ENDID/6HEND /
DATA XM0NTH(I),I=1,12/31.,28.,31.,30.,31.,30.,31.,31.,
130.,31.,30.,31./
DATA ARDID/6HARDC /,LSSID/6HUSSTD /,DINER/6HN0RMAL/,
1DIMM/6HMEAN /
DATA AT1/6HARCC /,AT2/6HUSSTD /,AT3/6HP0E /,AT4/6HSMALL /,
1ATS/6HSPE0AR/
COMMON/HBLK/XKERTH,XA0,XB0,XAE,XJJ,XHH,XCD,XDAN0M,XF,XPRINT,
1XATM0S,XDIURN,XLAG,XMVA,XMVP,XCDPM(25),XMASS(25),
2XATTK(45),XCN(45),XAREA(45),XINTA(6),XINTP(6),XDAP0(10),
3XCDA(50),XCUT(2),XXCAT(3),XC0R(11C),XIN,XASN,XARG
4,XECLPT,XAMPR,XFTENB(153),XFTEN(153),XAP(153),XSA,XSR
COMMON/CLK/AP0,PER1,TIME,AE,SINI,B0,F,JJ,KERTH,
1C0SI,JCNT,CDPRIM,AREA,ATTACK,CN,
2MASS,AD0T,PD0T,PD0AC,TIMED
3,C0SE,E,DA02,PER,TIME1,HH,DE03
4,CAPDM1,CAPID,SMAM1,ADTM1,AP0M1,SMAN,SMACM1,SMAID,CAPM1,CAPW
5,CAP0,DATE,XM0NTH,FTENB,AP
6,INTERA,INTERP,DD,CAN0M,DAP05E(10),CDA(50)
7,PRINT,CUT0FF(2),AI,RPAI,SAC0TI
8,REV0U,MT,VPI,PDI
9,PN(6),AN(6),REV1
1,C0RREC,S0LAR,ATM0S,FTEN,DIURNL,XLAG,RH0XX,S0,SA
1,EI,RIPP,RIPA,AMPR
D0 10 I=1,365
C0SE(I)=0.
E(I)=0.
STAPA(I)=0.
10 STEPP(I)=0.
REV1=0.
REV0L=0.
TIME1=0.
D0 104 I=1,5
INTERA(I)=C.
104 INTERP(I)=C.
CD=0.
TIME=0.
D0 7000 I=4,110
7000 C0RREC(I)=C.
D0 857 I=1,153
FTENB(I)=XFTENB(I)

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#1
#2
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KILGØ LIFE		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	FTEN(I)=XFTEN(I)	✓21	
857	AP(I)=XAP(I)	✓22	✓23
	ECLIPT=XECLPT	✓24	
	AMPR=XAMPR	✓25	
	SA=XSA	✓26	
	SØ=XSR	✓27	
	KERTH=XKERTH	✓28	
	AØ=XAO	✓29	
	BØ=XBO	✓30	
	AE=XAB	✓31	
	JJ=XJJ	✓32	
	HH=XHH	✓33	
	DD=XDD	✓34	
	OANØM=XOANØM	✓35	
	F=XF	✓36	
	PRINT=XPRINT	✓37	
	ATMØS=XATMØS	✓38	
	DIURNL=XDIURN	✓39	
	XLAC=XXLAG	✓40	
	AØØ=XMVA	✓41	
	PØØ=XMVP	✓42	
	DØ 850 I=1,25	✓43	
	COPRIM(I)=XCOPM(I)	✓44	
850	MASS(I)=XMASS(I)	✓45	✓46
	DØ 851 I=1,45	✓47	
	ATTACK(I)=XATTK(I)	✓48	
	CN(I)=XCN(I)	✓49	
851	AREA(I)=XAREA(I)	✓50	✓51
	DØ 852 I=1,6	✓52	
	INTERA(I)=XINTA(I)	✓53	
852	INTERP(I)=XINTP(I)	✓54	✓55
	DØ 853 I=1,10	✓56	
853	DAPØGB(I)=XDAPØ(I)	✓57	✓58
	DØ 854 I=1,50	✓59	
854	CDA(I)=XCDA(I)	✓60	✓61
	CUTØFF=XCUF	✓62	
	CUTØFF(2)=XCUT(2)	✓63	
	DØ 855 I=1,3	✓64	
855	DATE(I)=XXCAT(I)	✓65	✓66
	DØ 856 I=1,11C	✓67	
856	CØRREC(I)=XCØR(I)	✓68	✓69
	INC=XIN	✓70	
	CAPØ=XASN	✓71	
	WØ=XARG	✓72	
3015	CØNTINUE	✓73	
2700	FØRMAT(IHØ,1A6/)		
	WRITE(6,30)	✓74	✓75
30	FØRMAT(IH1,25X,27H***** EARTH CØNSTANTS *****)		
	WRITE(6,31)JJ,HH,DC,KERTH,AE,F	✓76	✓77 ✓78
31	FØRMAT(IHØ21HEARTH SECØND HARMØNICE15.8,5X,		
	120HEARTH THIRC HARMØNICE15.8,5X,		
	221HEARTH FØURTH HARMØNICE15.8/,		
	31H 40HEARTH GRAVITATØNAL CØNSTANT (KILØMETERS,		
	423H CUBED/SECØNDS SQUARED)B15.8/,		
	51H 30HEQUATØRIAL RADIUS (KILØMETERS)E15.8,5X,		
	611HELLIPTICITYE15.8/)		

KILGØ LIFE		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	WRITE(6,1400)	,79	,80
1400	FORMAT(1H0,25X,32H***** BALLISTIC PARAMETERS *****)		
	IF(CDA-SNBCI)22,33,32	,81	
33	WRITE(6,34)	,82	,83
34	FORMAT(1H011HSPECIAL CDA)		
	WRITE(6,1100)	,84	,85
1100	FORMAT(1H 17HREV(CYCLES/ØRBIT),5X,1ØHTIME(DAYS))		
	KK=2		
1103	IF(CCA(KK)-ENDID)1101,1102,1101	,86	
1101	KK=KK+2	,87	
	GØTØ1103	,88	
1102	KK=KK+2	,89	
	DØ 1104 I=1,KK,2	,90	
1104	WRITE(6,1105)CDA(I+1),CDA(I+2)	,91	
1105	FORMAT(1H E15.8,5X,E15.8)	,92	,93 ,94 ,95
32	WRITE(6,35)		
35	FORMAT(1H024HANGLE ØF ATTACK FUNCTION)	,96	,97
	WRITE(6,36)	,98	,99
36	FORMAT(1H 14HALPHA(DEGREES),6X, 116HANØMALY(DEGREES))		
	KK=2	,100	
702	IF(ATTACK(KK-1)-ENDID)700,701,700	,101	
700	KK=KK+2	,102	
	GØ TØ 702	,103	
701	KK=KK+2	,104	
	DØ 38 I=1,KK,2	,105	
	WRITE(6,37)ATTACK(I),ATTACK(I+1)	,106	,107 ,108
37	FORMAT(1H E15.8,5X,E15.8)		
38	CONTINUE		
	WRITE(6,39)	,109	,110
39	FORMAT(1H028HCØEFFICIENT ØF DRAG FUNCTION)	,111	,112
	KK=2	,113	
705	IF(CN(KK)-ENDID)702,704,703	,114	
703	KK=KK+2	,115	
	GØ TØ 705	,116	
704	CONTINUE	,117	
	IF(CN-BCTIM)40,41,40	,118	
40	WRITE(6,42)	,119	,120
42	FORMAT(1H 2HCN,18X,14HALPHA(DEGREES))		
	GØ TØ 44	,121	
41	WRITE(6,43)	,122	,123
43	FORMAT(1H 2HCN,18X,1ØHTIME(DAYS))		
44	KK=KK+2	,124	
	DØ 46 I=1,KK,2	,125	
	WRITE(6,45)CN(I+1),CN(I+2)	,126	,127 ,128
45	FORMAT(1H E15.8,5X,E15.8)		
46	CONTINUE	,129	,130
	WRITE(6,47)	,131	,132
47	FORMAT(1H07HCCPRIME,13X, 11ØHPERIGBE(KILOMETERS))		
	KK=2	,133	
708	IF(CDPRIMLKK-1)-ENDID)706,707,706	,134	
706	KK=KK+2	,135	
	GØ TØ 708	,136	
707	KK=KK+2	,137	
	DØ 49 I=1,KK,2	,138	

KILGØ LIFE		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	WRITE(6,48)CDPRIM(I),CDPRIM(I+1)	#139	#140 #141
48	FORMAT(1H E15.8,5X,E15.8)		
49	CONTINUE	#142	#143
	WRITE(6,50)	#144	#145
50	FORMAT(1H 20HEFFECTIVE DRAG AREA FUNCTION)		
	KK=2	#146	
711	IF(ARBA(KK)-ENDID)7C9,710,709	#147	
709	KK=KK+2	#148	
	G0 T0 711	#149	
710	CONTINUE	#150	
	IF(AREA-BCITIM)51,52,51	#151	
51	WRITE(6,53)	#152	#153
53	FORMAT(1H 20HAREA(METERS SQUARED),3X,		
	114HALPHA(DEGREES))		
	G0 T0 55	#154	
52	WRITE(6,54)	#155	#156
54	FORMAT(1H 20HAREA(METERS SQUARED),3X,		
	110HTIME(DAYS))		
55	CONTINUE	#157	
	KK=KK+2	#158	
	D0 57 I=1,KK,2	#159	
	WRITE(6,56)AREA(I+1),AREA(I+2)	#160	#161 #162
56	FORMAT(1H E15.8,8X,E15.8)		
57	CONTINUE	#163	#164
	WRITE(6,59)	#165	#166
58	FORMAT(1H 014HMASS CONSTANTS)		
	IF(MASS-BCITIM)59,60,59	#167	
59	WRITE(6,61)MASS(2)	#168	#169 #170
61	FORMAT(1H 23HINITIAL MASS(KILOGRAMS)E15.8/)		
	IF(MASS(3))62,70,62	#171	
62	WRITE(6,63)	#172	#173
63	FORMAT(1H 23HMASS DECAY RATE(KG/DAY),3X,		
	114HFINAL MASS(KG))		
	KK=2	#174	
714	IF(MASS(KK+1)-ENDID)712,713,712	#175	
712	KK=KK+2	#176	
	G0 T0 714	#177	
713	KK=KK+2	#178	
	D0 200 I=1,KK,2	#179	
	WRITE(6,64)MASS(I+2),MASS(I+3)	#180	#181 #182
64	FORMAT(1H E15.8,11X,E15.8)		
200	CONTINUE	#183	#184
	G0 T0 70	#185	
60	WRITE(6,65)	#186	#187
65	FORMAT(1H 15HMASS(KILOGRAMS),3X,		
	110HTIME(DAYS))		
	KK=2	#188	
717	IF(MASS(KK)-ENDID)715,716,715	#189	
715	KK=KK+2	#190	
	G0 T0 717	#191	
716	KK=KK+2	#192	
	D0 202 I=1,KK,2	#193	
	WRITE(6,66)MASS(I+1),MASS(I+2)	#194	#195 #196
66	FORMAT(1H E15.8,5X,E15.8)		
202	CONTINUE	#197	#198
70	CONTINUE	#199	

KILGØ LIFE	EXTERNAL FØRMULA NUMBER	SØRCE STATEMENT	INTERNAL FØRMULA NUMBER(S)
		WRITE(6,14C1)	✓200 ,201
1401		FØRMAT(1H0,25X,30H***** DENSITY PARAMETERS *****)	
		DELYR=DATE(3)-1957.	✓202
		XDAYS=DELYR*365.	✓203
		XLEAP=DELYR/4.	✓204
		I=XLEAP	✓205
		XLEAP=I	✓206
		XDAYS=XDAYS+XLEAP	✓207
		K=DATE(1)	✓208
		YDAYS=0.	✓209
		K=K-1	✓210
		DØ 1700 I=1,K	✓211
1700		YDAYS=XMONTH(1)+YDAYS	✓212 ,213
		XDAYS=XDAYS+YDAYS+CATE(2)	✓214
		IF(CATE(1)-2.)1702,1701,1701	✓215
1701		XLPE=DATE(3)-1956.	✓216
1704		XLPE=XLPE-4.	✓217
		IF(XLPE)1702,1703,1704	✓218
1703		XDAYS=XDAYS+1.	✓219
1702		XDAYS=XDAYS-365.	✓220
		WRITE(6,17C5)CATE,XDAYS	✓221 ,222 ✓223
1705		FØRMAT(1H06HMØNTH=E9.2,5X,4HDEARE11.4,5X, 133HCAYS ELAPSED SINCE DEC. 31 , 1957E15.8)	
1402		IF(ATMØS-AT1)6002,6C00,60C2	✓224
6000		WRITE(6,60C1)	✓225 ,226
6001		FØRMAT(1H 20H1959 ARDC ATMØSPHERE1 GØTØ 6016	✓227
6002		IF(ATMØS-AT2)6005,6C03,60C5	✓228
6003		WRITE(6,60C4)	✓229 ,230
6004		FØRMAT(1H 29H1962 U.S. STANDARD ATMØSPHERE) GØTØ 6016	✓231
6005		IF(ATMØS-AT3)6008,6C06,60C8	✓232
6006		WRITE(6,6007)	✓233 ,234
6007		FØRMAT(1H 21HPØE ATMØSPHERE (LMSC)) GØTØ 6016	✓235
6008		IF(ATMØS-AT4)6011,6C09,6011	✓236
6009		WRITE(6,6010)	✓237 ,238
6010		FØRMAT(1H 28HFUNT SMALL ATMØSPHEREB (LMSC)) GØTØ 6016	✓239
6011		IF(ATMØS-AT5)6014,6C12,6014	✓240
6012		WRITE(6,6013)	✓241 ,242
6013		FØRMAT(1H 29HSPECIAL 1959 ARDC ATMØSPHERE) GØTØ 6016	✓243
6014		WRITE(6,6015)	✓244 ,245
6015		FØRMAT(1H 37HSPECIAL 1962 U.S. STANDARD ATMØSPHERE) 6016 CØNTINUE	✓246
		WRITE(6,1412)	✓247 ,248
1412		FØRMAT(1H018DCENSITY (CØRRECTIØN) WRITE(6,1413)	✓249 ,250
1413		FØRMAT(1H 2HDC,18X,19HPERIGEE(KILØMETERS)) KK=2	✓251
1416		IF(CØRREC(KK-1)-ENCID)1414,1415,1414	✓252
1414		KK=KK+2	✓253
		GØTØ 1416	✓254
1415		KK=KK-2	✓255
		DØ 1417 I=1,KK,2	✓256

KILGØ LIFE		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	WRITE(6,1410)CØRREC(J),CØRREC(J+1)	✓257	✓258 ✓259
1418	FORMAT(1H E15.8,5X,E15.8)		
1417	CONTINUE	✓260	✓261
	WRITE(6,1465)	✓262	✓263
1465	FORMAT(1H02HKP,18X,4HYEAR)		
	KK=3	✓264	
1452	IF(AP(KK-2)-ENDID)145C,1451,1450	✓265	
1450	KK=KK+2	✓266	
	GØTØ1452	✓267	
1451	KK=KK-3	✓268	
	DØ 1453 I=1,KK,2	✓265	
	WRITE(6,1454)AP(I),AP(I+1)	✓270	✓271 ✓272
1454	FORMAT(1H E15.8,5X,E15.8)		
1453	CONTINUE	✓273	✓274
	WRITE(6,1455)	✓275	✓276
1455	FORMAT(1H04HFTEN,16X,4HYEAR)		
	KK=3	✓277	
1458	IF(FTEN(KK-2)-ENDID)1456,1457,1450	✓278	
1456	KK=KK+2	✓279	
	GØTØ1458	✓280	
1457	KK=KK-3	✓281	
	DØ 1459 I=1,KK,2	✓282	
	WRITE(6,1454)FTEN(I),FTEN(I+1)	✓283	✓284 ✓285
1459	CONTINUE	✓286	✓287
	WRITE(6,1460)	✓288	✓289
1460	FORMAT(1H05HFTENB,15X,4HYEAR)		
	KK=3	✓290	
1463	IF(FTENB(KK-2)-ENDID)1461,1462,1461	✓291	
1461	KK=KK+2	✓292	
	GØTØ1463	✓293	
1462	KK=KK-3	✓294	
	DØ 1464 I=1,KK,2	✓295	
	WRITE(6,1454)FTENB(I),FTENB(I+1)	✓296	✓297 ✓298
1464	CONTINUE	✓299	✓300
	IF(CIURNL-CINØR)1422,1420,1422	✓301	
1420	WRITE(6,1421)	✓302	✓303
1421	FORMAT(1H016HC IURNAL NØRMAL)		
	GØTØ1427	✓304	
1422	CONTINUE	✓305	
1423	WRITE(6,1424)	✓306	✓307
1424	FORMAT(1H014HC IURNAL MEAN)		
1427	CONTINUE	✓308	
	WRITE(6,1429)	✓309	✓310
1429	FORMAT(1H0,25X,26H***** SPECIAL EVENTS *****)		
	IF(CUTØFF-AID)71,72,71	✓311	
72	WRITE(6,73)CUTØFF(2)	✓312	✓313 ✓314
73	FORMAT(1H017HAPØGEE CUTØFF(KM)E15.8)		
	GØ TØ 80	✓315	
71	IF(CUTØFF-PID)74,75,74	✓316	
75	WRITE(6,76)CUTØFF(2)	✓317	✓318 ✓319
76	FORMAT(1H018HPERIGEE CUTØFF(KM)E15.8)		
	GØ TØ 80	✓320	
74	WRITE(6,77)	✓321	✓322
77	FORMAT(1H019HEARTH IMPACT CUTØFF)		
80	CONTINUE	✓323	
	IFIINTERA183,83,82	✓324	

KILGØ LIFE		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
82	WRITE(6,84)	✓325	✓326
84	FORMAT(1H034H TIME FOR APØGEE INTERPOLATION(DAY))		
	DØ 86 I=1,5	✓327	
	WRITE(6,85)INTERA(I)	✓328	✓329 ✓330
85	FORMAT(1H E15.8)		
86	CONTINUE		
83	IF(INTERP)87,87,88	✓331	✓332
88	WRITE(6,89)	✓332	
89	FORMAT(1H035H TIME FOR PERIGEE INTERPOLATION(DAY))	✓334	✓335
	DØ 91 I=1,5	✓336	
	WRITE(6,90)INTERP(I)	✓337	✓338 ✓339
90	FORMAT(1H E15.8)		
91	CONTINUE		
87	CONTINUE	✓340	✓341
	WRITE(6,1430)	✓342	
1430	FORMAT(1H0,25X,30H***** INITIAL CONDITIONS *****)	✓343	✓344
	IF(PRINT-DETC)92,53,92		
93	WRITE(6,94)	✓345	
94	FORMAT(1H015HDETAIL PRINTOUT)	✓346	✓347
	GØ TØ 100		
92	IF(PRINT-SPØIC)95,56,95	✓348	
96	WRITE(6,97)	✓349	
97	FORMAT(1H014HSHORT PRINTOUT)	✓350	✓351
	GØ TØ 100		
95	WRITE(6,98)	✓352	
98	FORMAT(1H015HNORMAL PRINTOUT)	✓353	✓354
100	CONTINUE		
	WRITE(6,81)CANØM	✓355	
81	FORMAT(1H021HANØMALY STEP(DEGREES)E15.8)	✓356	✓357 ✓358
	WRITE(6,101)	✓359	✓360
101	FORMAT(1H016HAPØGEE STEPS(MM),13X,		
	118HPERIGEE RADIUS(KM))		
	DØ 103 I=1,10,2	✓361	
	WRITE(6,102)DAPØGE(I),DAPØGE(I+1)	✓362	✓363 ✓364
102	FORMAT(1H E15.8,15X,E15.8)		
103	CONTINUE	✓365	✓366
	TEMP=0.	✓367	
	TEMP=360./CANØM	✓368	
	RADDE=DANØM/DPR	✓369	
	I=TEMP	✓370	
	JCNT=I+1	✓371	
	K=2	✓372	
4	IF(I)2,2,3	✓373	
3	I=I-1	✓374	
	TEMP=RADDE+TEMP	✓375	
	CØSE(K)=CØS(TEMP)	✓376	
	E(K)=TEMP*CPR	✓377	
	K=K+1	✓378	
	GØ TØ 4	✓379	
2	CØSE=1.	✓380	
	E=0.	✓381	
	DEØ3=RADDE/3.	✓382	
	SINI=SIN(INC/CPR)	✓383	
	CØS1=CØS(INC/CPR)	✓384	
	KA =1	✓385	
	KP=1	✓386	

KILCO LIFE		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
I=1		✓387	
302	IF(A00-DAP0GE(I+1))300,301,301	✓388	
300	I=I+2	✓389	
G0 T0 302		✓390	
301	DA=CAP0GE(I)	✓391	
DA02=DA/2.		✓392	
PER=P00		✓392	
PER1=P00		✓394	
AP0=A00		✓395	
CALL PDAD		✓396	
ADTM1=AD0T		✓397	
IF(PRINT-DETC)105,106,105		✓398	
106	WRITE(6,15C)	✓399	✓400
CALL PRINTT		✓401	
150	FORMAT(1H146HAP0GEE,PERIGEE,MAJOR AXIS,AND EARTH RADIUS(KM)/, 11X,48HAP0GEE,PERIGEE,MAJOR AXIS RATES(KM/DAY) MASS(KG)/, 21X,39HASCENDING NZCE,ARGUMENT OF PERIGEE(DEG)/, 31X,38HND00,PERIGEE REGRESSION RATES(DEG/DAY)/, 41X,24HPERIGEE VELOCITY(KM/SEC)/, 51X,19H0RBITAL PERIOD(MIN)/, 61X,29HLIFETIME SPENT(0RBIT AND DAY)/, 71X,47HRH0(KG/M3), E(UNITLESS), R1PERG AND R1PAPG(KM)/)		
G0T0 108		✓402	
105	IF(PRINT-SH0IC)107,106,107	✓403	
107	WRITE(6,109)	✓404	✓405
109	FORMAT(1H129HAP0GEE,PERIGEE,MAJOR AXIS,AND, 117H,EARTH RADIUS(KM)/,1X, 243HAP0GEE,PERIGEE,AND MAJOR AXIS RATES(KM/DAY)/,1X, 329HLIFETIME SPENT(0RBIT AND DAY))		
WRITE(6,11C)AP0,PER1,AI,RPAT,AD0T,PD0T,SAD0TI,REV0L,TIME		✓406	✓407 ✓408
110	FORMAT(1H06HA E15.8,3X,6HP E15.8,3X,6HAXIS E15.8,3X, 16HRADIUSE15.8/,1X,6HAD0T E15.8,3X,6HPD0T E15.8,3X, 26HAXID0TE15.8,3X,6H0RBIT E15.8,3X,6HTIME E15.8/)		
108	CONTINUE	✓409	
3001	CALL RK	✓410	
3021	IF(INTERA(KA))400,4C0,401	✓411	
401	IF(TIME-INTERA(KA))400,402,402	✓412	
402	AN(KA)=(AP0-DA)+((INTERA(KA)-TIME1)*(AP0-(AP2-DA)))/(TIME-TIME1)	✓413	
KA=KA+1		✓414	
G0T03021		✓415	
400	IF(INTERP(KP))403,4C3,4C4	✓416	
404	IF(TIME-INTERP(KP))403,405,405	✓417	
405	PN(KP)=PER+((INTERP(KP)-TIME1)*(PER1-PER))/(TIME-TIME1)	✓418	
KP=KP+1		✓419	
G0T0400		✓420	
403	CONTINUE	✓421	
I=1		✓422	
305	IF(AP0-DAP0GE(I+1))303,304,304	✓423	
303	I=I+2	✓424	
G0 T0 305		✓425	
304	DA=CAP0GE(I)	✓426	
DA02=DA/2.		✓427	
PER=PER1		✓428	
TIME1=TIME		✓429	
IF(PRINT-DETC)111,112,111		✓430	
111	IF(PRINT-SH0IC)113,114,113	✓431	

KILGØ LIFE		06/18/65		
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)		
113	WRITE(6,110)APØ,PER1,A1,RPAL,ADØT,PCØT,SADØTI,REVØL,TIME	,432	,433	,434
	GØ TØ 114	,435		
112	CALL PRINTT	,436		
114	IF(CUTØFF-AID)115,116,115	,437		
116	IF(APØ-CUTØFF(2))130,130,3001	,438		
115	IF(CUTØFF-PID)117,118,117	,439		
118	IF(PER1-CUTØFF(2))130,130,3001	,440		
117	IF(PER1-AB)130,130,3001	,441		
130	IF(PRINT-DEIIC)131,132,131	,442		
131	IF(PRINT-SH2IC)133,132,133	,443		
132	CALL PRINTT	,444		
	GØ TØ 3000	,445		
133	WRITE(6,110)APØ,PER1,A1,RPAL,ADØT,PCØT,SADØTI,REVØL,TIME	,446	,447	,448
	GØ TØ 3000	,449		
3000	IF(INTERA)500,500,501	,450		
501	WRITE(6,502)	,451	,452	
502	FORMAT(1H033HAPØGEE ALTITUDE INTERPØLATION(KM),3X, 112HTIME IN DAYS)			
	KA=KA-1	,453		
	DØ 504 I=1,KA	,454		
	WRITE(6,503)AN(I),INTERA(I)	,455	,456	,457
503	FORMAT(1H0E15.8,5X,E15.8)			
504	CØNTINUE	,458	,459	
500	IF(INTERP)505,505,506	,460		
506	WRITE(6,507)	,461	,462	
507	FORMAT(1H034HPERIGEE ALTITUDE INTERPØLATION(KM),3X, 112HTIME IN DAYS)			
	KP=KP-1	,463		
	DØ 509 I=1,KP	,464		
	WRITE(6,508)PK(I),INTERP(I)	,465	,466	,467
508	FORMAT(1H0E15.8,5X,E15.8)			
509	CØNTINUE	,468	,469	
505	CØNTINUE	,470		
	TIME=0.	,471		
	TIME1=0.	,472		
	REVØL=0.	,473		
	REV1=0.	,474		
	RETURN	,475		
3020	STØP	,476		
	END	,477		

KILGØ PDAD		06/18/65	
EXTERNAL FORMULA NUMBER		SOURCE STATEMENT	
		INTERNAL FORMULA NUMBER(S)	
SUBROUTINE PDAD			
REAL JJ,KERTH,INTA,INTP,MASS,MT,INTERA,INTERP,INC,NI			
DIMENSION DATE(3), XMONTH(12)			
DIMENSION FTENB(152),FTEN(153),AP(153)			
DIMENSION CORREC(110),SOLAR(301)			
DIMENSION PR(16)			
DIMENSION TN(6),INTERA(6),TN1(6),INTERP(6),			
IC0SE(365),E(365),CDPRIM(25),AREA(45),CN(45),			
2ATTACK(45),STEPA(365),STEPR(365),MASS(25)			
COMMON /ARCC/TEMP,TMP,PRBSS,P0MP,			
1PSP0,RH0,RH0SR0,VISC,VISC SL,KVISC,VS,G			
DATA DPR/57.2957795/, PI/3.14159291/,SNBCI/6HSINE /			
1,BCITIM/6HTIME /			
DATA DIN0R/6HARMAL/,DIMN/6HMEAN /,DIN0N/6H0NE /			
DATA AID/6HA /,PID/6HP /,CETID/6HDETAIL/,			
1SH0ID/6HSH0RT /			
DATA BNDID/6HEND /			
DATA AT1/6HARCC /,AT2/6HUSSTD /,AT3/6HP0E /,AT4/6HSMALL /,			
1AT5/6HSPECAR/			
COMMON/CLK/AP0,PER1,TIME,AE,SINI,W0,F,JJ,KERTH,			
1C0SI, JCNT,CDPRIM, AREA,ATTACK, CN,			
2MASS,AD0T,PD0T,PD0AC,TIMED			
3, C0SE,E,DA02,PER,TIME1,HH,DE03			
4,CAPDM1,CAPID,SMAM1,ADTM1,AP0M1,SMAN,SMACM1,SMAID,CAPM1,CAPW			
5,CAP0,DATE,XMONTH,FTENB,AP			
6,INTERA,INTERP,DD,DAN0M,DAR0GE(10),COA(50)			
7,PRINT, CUT0FF(2), AI,RPAI,SAD0TI			
8,REV0U,MT,VPI,PDI			
9,PN(6),AN(6),REVI			
1,C0RREC,SOLAR,ATM0S,FTEN,DIURNL,XUAG,RH0XX,S0,SA			
1,EI,RIPP,RIPA,AMPR			
DELYR=DATE(3)-1957.			
XDAY5=DELYR*365.			
XLEAP=DELYR/4.			
I=XLEAP			
XLEAP=I			
XDAY5=XDAY5+XLEAP			
K=DATE(1)			
YDAY5=0.			
K=K-1			
D0 1706 I=1,K			
1706 YDAY5=XMONTH(I)+YDAY5			
XDAY5=XDAY5+YDAY5+DATE(2)			
IF(CATE(1)-2.)1702,1701,1701			
1701 XLPE=DATE(3)-1956.			
1704 XLPE=XLPE-4.			
IF(XLPE)1702,1703,1704			
1703 XDAY5=XDAY5+1.			
1702 XDAY5=XDAY5-365.			
AI=(AP0+PER1)/2.			
EI=(AP0-PER1)/(AP0+PER1)			
IF(TIME)10,10,11			
10 RPAI=AE*11.-(SINI*SINI*SIN(W0/DPR1**2/F))			
B1=1.-3.*SINI*SINI/2.			
TEMP=1.-EI*EI			

KILGØ PDAD		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
	TEMP1=SQRT(TEMP)	#26
	NI=1.+(JJ*AE/AI*AE/AI*B1/(TEMP*TEMP1))	#27
	NI=SQRT(KERTH/(AI*AI*AI))*NI*24.*36CO.*DPR	#28
	SMAID=JJ*NI*(AE/(AI*TEMP))*2*(2.-5.*SINI*SINI/2.)	#29
	CAPID=JJ*NI*(AE/(AI*TEMP))*2*CØSI	#30
	CAPM1=CAPØ	#31
	SMAW=WØ	#32
	SMAW=WØ	#33
	CAPW=CAPØ	#34
	APØM1=APØ	#35
	CAPCM1=CAPID	#36
	SMACM1=SMAID	#37
	GØ TØ 12	#38
11	DTI=(APØ-APØM1)/ADTM1	#39
	IF(AMPR)458,468,469	#40
468	SINTA=0.	#41
	SINTP=0.	#42
	SINTW=0.	#43
	GØTØ470	#44
469	CALL SØRAP(XDAYZ,AI,EI,CAPW,SMAW,INC,AMPR,KERTH,SCW,SDRA,SDRP)	#45
	SINTA=(2.*SDRA-SDRP)/3./5.729578	#46
	SINTP=SDRP/3./5.729578	#47
	SINTW=SDW*10./3.	#48
470	SMAW=SMAW1+DTI*(SMACM1+SINTW)	#49
2102	IF(SMAW-360.)2100,2101,21C1	#50
2101	SMAW=SMAW-360.	#51
	GØTØ 2102	#52
2100	SMAW=SMAW	#53
	CAPW=CAPM1+CAPDM1*CTI	#54
2105	IF(CAPW-360.)2103,2104,21C4	#55
2104	CAPW=CAPW-360.	#56
	GØTØ2105	#57
2103	CAPW=CAPW	#58
	B1=1.-3.*SINI*SINI/2.	#59
	TEMP=1.-EI*EI	#60
	TEMP1=SQRT(TEMP)	#61
	NI=1.+(JJ*AE/AI*AE/AI*B1/(TEMP*TEMP1))	#62
	NI=SQRT(KERTH/(AI*AI*AI))*NI*24.*36CO.*DPR	#63
	CAPID=JJ*NI*(AE/(AI*TEMP))*2*CØSI	#64
	SMAID=JJ*NI*(AE/(AI*TEMP))*2*(2.-5.*SINI*SINI/2.)	#65
	RPAI=AE*(1.-(SINI*SINI*SIN(SMAW/DPR))*2/F))	#66
12	CONTINUE	#67
	PDI=2.*PI/60.*SQRT(AI*AI*AI/KERTHI	#68
	VPI=SQRT(KERTH)*SQRT(2./PER1*(1.-JJ/3.*AE	
	1/PER1*AE/PER1*(3.*SINI*SINI*SIN(SMAW/DPR)*SIN	
	2(SMAW/DPR)-1.))-1./AI)	#69
	L=JCNT	#70
	J=1	#71
1502	IF(L)1500,150C,1501	#72
1501	L=L-1	#73
	RI=AI*(1.-EI*EI)/(1.+EI*CØSE(J))+	
	1(2./3.*JJ/AI*AE/(1.-EI*EI)*AE)*((SINI*SINI)*(1.-	
	2SIN((SMAW+E(J))/DPR))*2/2.))-3./10.*HH/	
	3JJ*AE*SINI*(SIN((SMAW+E(J))/DPR)-SIN(WØ	
	4+E(J))/DPR))	#74
	RIP=RI-AE*(1.-SINI*SINI*	

KILGØ POAD		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
	1 SIN((SMAW+E(J))/DPR)**2/F)	#75
	IF(E(J))1900,1900,1901	#76
1900	RIPP=RIP	#77
	GØ TØ 1903	#78
1901	IF((ABS(E(J)-180.))-.001)1902,1902,1903	#79
1902	RIPA=RIP	#80
1903	CONTINUE	#81
	IF(RIP)80,81,81	#82
80	RIP=0.	#83
81	CONTINUE	#84
	I=1	#85
28	IF(RIP-CDPRIM(I+1))29,30,31	#86
29	I=I+2	#87
	IF(I-24)28,28,7001	#88
31	IF(I-1)30,20,22	#89
32	CDP=CDPRIM(I-2)+(CDPRIM(I)-CDPRIM(I-2))*(RIP-	
	CDPRIM(I-1))/(CDPRIM(I+1)-CDPRIM(I-1))	#90
	GØ TØ 26	#91
20	CDP=CDPRIM(I)	#92
26	IF(CDA-S4BCI)100,101,100	#93
101	I=2	#94
1103	IF(TIME-CDAT(I+1))1100,1100,1102	#95
1102	I=I+2	#96
	IF(I-44)1103,1103,7001	#97
1100	CDAX=CDAL(I)	#98
	CDAREA=CDP*CN(2)*AREA(2)+(CDP*CN(4)*AREA(4)-	
	CDP*GN(2)*AREA(2))*ABS(SIN((CDAX *E(J)+ATTACK(I)/	
	2DPR)))	#99
	GØ TØ 500	#100
100	I=1	#101
203	IF(E(J)-ATTACK(I+1))200,201,202	#102
202	I=I+2	#103
	IF(I-44)203,203,7001	#104
200	IF(I-1)201,201,204	#105
204	ALPHA=ATTACK(I-2)+(ATTACK(I)-ATTACK(I-2))	
	1*(E(J)-ATTACK(I-1))/(ATTACK(I+1)-	
	2ATTACK(I-1))	#106
	GØ TØ 205	#107
201	ALPHA=ATTACK(I)	#108
205	IF(CN=BCITIM)34,33,34	#109
34	I=2	#110
38	IF(ALPHA-CN(I+1))35,36,37	#111
37	I=I+2	#112
	IF(I-44)38,38,7001	#113
35	IF(I-2)36,36,39	#114
39	CNN=CN(I-2)+(CN(I)-CN(I-2))*(ALPHA-	
	CN(I-1))/(CN(I+1)-CN(I-1))	#115
	GØ TØ 40	#116
36	CNN=CN(I)	#117
	GØ TØ 40	#118
33	I=2	#119
53	IF(TIME-CN(I+1))50,51,52	#120
52	I=I+2	#121
	IF(I-44)53,53,7001	#122
50	IF(I-2)51,51,54	#123
54	CNN=CN(I)	#124

KILGØ ROAD		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
	GØ TØ 40	✓125
51	CNN=CN(I)	✓126
40	CD=CDP*CNN	✓127
	IF(AREA-BCITIP)60,61,60	✓128
60	I=2	✓129
65	IF(ALPHA-AREA(I+1))62,63,64	✓130
64	I=I+2	✓131
	IF(I-44)65,65,7C01	✓132
62	IF(I-2)63,63,66	✓133
66	ARAA=AREA(I-2)+(AREA(I)-AREA(I-2))*ALPHA- 1AREA(I-1))/(AREA(I+1)-AREA(I-1))	✓134
	GØ TØ 70	✓135
63	ARAA=AREA(I)	✓136
	GØ TØ 70	✓137
61	I=2	✓138
74	IF(TIME-AREA(I+1))71,72,73	✓139
73	I=I+2	✓140
	IF(I-44)74,74,7C01	✓141
71	IF(I-2)72,72,75	✓142
75	ARAA=AREA(I)	✓143
	GØ TØ 70	✓144
72	ARAA=AREA(I)	✓145
70	CDAREA=ARAA*CD	✓146
500	IF(RIP-700.)3C0,301,301	✓147
301	RHØ=0.	✓148
	GØTØ 503	✓149
300	IF(ATMØS-AT1)302,3C3,302	✓150
303	CALL ARDC59(RIP*1.E3)	✓151
	GØ TØ 503	✓152
302	IF(ATMØS-AT2)304,3C5,304	✓153
305	PR(1)=RIP*1.E3	✓154
	CALL PRA63(PR,ERRØR)	✓155
	RHØ=PR(6)/9.81	✓156
	GØ TØ 503	✓157
304	IF(ATMØS-AT3)306,3C7,306	✓158
307	X=RI *CØS((SMAW+E(J))/DPR)	✓159
	Y=RI *SIN((SMAW+E(J))/DPR)	✓160
	XP=X	✓161
	YP=Y*SQRT(1.-SINI**2)	✓162
	ZP=Y*SINI	✓163
	TEMP=CØS(CAPW/DPR)	✓164
	TEMQ=SINI(CAPW/DPR)	✓165
	XS=XP*TEMP-YP*TEMQ	✓166
	YS=XP*TEMQ+YP*TEMP	✓167
	ZS=ZP	✓168
	RS=SQRT(XS*XS+YS*YS+ZS*ZS)	✓169
	IF(ATMØS-AT3)350,351,350	✓170
351	D=XDAYS+TIME	✓171
	CALL PØEAT(RIP,RHØ,D,XS,YS,ZS,RS)	✓172
	RHØ=RHØ*515.7/9.81	✓173
	GØTØ 503	✓174
350	D=XDAYS+TIME+36203.	✓175
	CALL SMATMS(XS,YS,ZS,SA,D,RHØ,RIP)	✓176
	RHØ=RHØ/9.81	✓177
	GØ TØ 503	✓178
306	IF(ATMØS-AT4)308,3C7,308	✓179

KILGØ PDAD		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
308	IF(ATMØS-AT5)310,311,31C	✓180	
311	CALL ARDC59(RIP=1.E2)	✓181	
	RHØ=RHØ*9.81	✓182	
	GØTØ 312	✓183	
310	PR(1)=RIP*1.E2	✓184	
	CALL PRA63(PR,ERRØR)	✓185	
	RHØ=PR(6)	✓186	
312	I=1	✓187	
316	IF(CØRREC(1)-ENDID)345,346,345	✓188	
346	DCC=CØRREC(I-2)	✓189	
	GØTØ 318	✓190	
345	IF(RIP-CØRREC(I+1))313,314,315	✓191	
313	I=I+2	✓192	
	IF(I-42)316,316,7001	✓193	
315	IF(I-1)314,314,317	✓194	
317	DCC=CØRREC(I-2)+(CØRREC(1)-CØRREC(I-2))*(RIP- CØRREC(I-1))/(CØRREC(I+1)-CØRREC(I-1))	✓195	
	GØ TØ 318	✓196	
314	DCC=CØRREC(1)	✓197	
318	IF(RIP-120.)319,319,320	✓198	
319	RHØ=RHØ*DCC/9.81	✓199	
	GØ TØ 503	✓200	
320	YERR=1958.+(TIME+XDAYS)/365.24	✓201	
	XDAYZ=XDAYS+TIME+36204.	✓202	
	IF(FTENB)322,321,322	✓203	
321	CØNTINUE	✓204	
	TEMP=(XDAYZ-36030.)/4090.*4.*PI	✓205	
	TEMØ=CØS(TEMP)*15.	✓206	
	TEMP=(XDAYZ-36340.)/4090.*2.*PI	✓207	
	TEMØ=CØS(TEMP)*75.	✓208	
	FTENBX=135.+TEMØ+TEMØ	✓209	
	GØTØ 4206	✓210	
322	I=1	✓211	
4205	IF(FTENB(I)-ENDID)4201,4200,4201	✓212	
4200	FTENBX=FTENB(I-2)	✓213	
	GØTØ 4206	✓214	
4201	IF(FTENB(I+1)-YERR)4204,4203,4202	✓215	
4204	I=I+2	✓216	
	GØTØ 4205	✓217	
4203	FTENBX=FTENB(I)	✓218	
	GØTØ 4206	✓219	
4202	IF(I-1)4203,4203,5200	✓220	
5200	FTENBX=FTENB(I-2)+(YERR-FTENB(I-1))*(FTENB(I)-FTENB(I-2))/ 1(FTENB(I+1)-FTENB(I-1))	✓221	
4206	IF(FTENB)4207,4208,4207	✓222	
4208	FTENX=FTENBX	✓223	
	GØ TØ 4215	✓224	
4207	I=1	✓225	
4214	IF(FTEN(I)-ENDID)4209,4210,4209	✓226	
4210	FTENX=FTEN(I-2)	✓227	
	GØTØ 4215	✓228	
4209	IF(FTEN(I+1)-YERR)4211,4212,4213	✓229	
4211	I=I+2	✓230	
	GØ TØ 4214	✓231	
4212	FTENX=FTEN(I)	✓232	
	GØTØ 4215	✓233	

KILGØ ROAD	EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
4213	IF(I-1)4212,4212,52C1		234
5201	FTENX=FTEN(I-2)*(YERR-FTEN(I-1))*(FTEN(I)-FTEN(I-2))/		235
	1(FTEN(I+1)-FTEN(I-1))		236
4215	IF(AP)4216,4217,4216		237
4217	APX=0		238
	GØTØ343		239
4216	I=1		240
4223	IF(AP(I)-ENDIC)4218,4219,4218		241
4219	APX=AP(I-2)		242
	GØTØ343		243
4218	IF(AP(I+1)-YERR)4220,4221,4222		244
4220	I=I+2		245
	GØTØ4223		246
4221	APX=AP(I)		247
	GØTØ343		248
4222	IF(I-1)4221,4221,52C2		249
5202	APX=AP(I-2)+(YERR-AP(I-1))*(AP(I)-AP(I-2))/		250
	1(AP(I+1)-AP(I-1))		251
343	SBAR=25.+28*FTENBX+.4*(FTENX-FTENBX)+APX*10.		252
	TEMP=LXDAYZ-38047.)/365.25		253
	TEMQ=.06*CØS(4.*PI*TEMP)		254
	TEMR=.025*CØS(2.*PI*TEMP)		255
	GTT=TEMR-TEMQ		256
	SS=SBAR*EXP(GTT)		257
	IF(CIURNL-CINØR)400,403,400		258
400	CØNTINUE		259
402	CØSPP=CØS(75./DPR)		260
	GØTØ 404		261
403	CØNTINUE		262
	TEMP=(SS-160.)/90.		263
	TEMR=-.00567*(RIP-200.)*EXP(-.01455*(RIP-200.))		264
	TEMQ=18.5+21.5*EXP(-.0315*(RIP-200.))		265
	TEMS=(18.5+30.*EXP(TEMR)+TEMQ*TEMR+4.*(1.-TEMP*TEMP))/DPR		266
	IF(TEMS-5.)510,510,511		267
511	TEMS=5.		268
510	XLAG=TEMS*DPR		269
	XLAMS=.017203*XDAYZ+.0335*SIN(.017203*XDAYZ)-1.41		270
	TEMP=CØS(XLAG)		271
	TEMQ=SIN(XLAG)		272
	XLS=TEMP		273
	TEMR=CØS(ECLIPT/DPR)		274
	TEMS=SIN(ECLIPT/DPR)		275
	XMS=TEMR*TEMQ		276
	XNS=TEMS*TEMQ		277
	RAS=ATAN2(XMS,XLS)		278
	RAB=RAS-XLAG/DPR		279
	XLB=SQRT(XNS*XNS+XLS*XLS)*CØS(RAB)		280
	XMB=SQRT(XNS*XNS+XLS*XLS)*SIN(RAB)		281
	XNB=XMS		282
	X=RI *CØS((SMAW+E(J))/DPR)		283
	Y=RI *SIN((SMAW+E(J))/DPR)		284
	XP=X		285
	YP=Y*SQRT(1.-SINI**2)		286
	ZP=Y*SINI		287
	TEMP=CØS(CAPW/DPR)		
	TEMQ=SIN(CAPW/DPR)		

KILGØ PDAC		06/18/65
EXTERNAL FORMULA NUMBER		SOURCE STATEMENT
		INTERNAL FORMULA NUMBER(S)
	XS=XP*TEMP-YP*TEMQ	288
	YS=XP*TEMQ+YP*TEMP	289
	ZS=ZP	290
	XL=XS/RI	291
	XM=YS/RI	292
	XN=ZS/RI	293
	CØSPP=XL*XLB+XM*XMB+XN*XNB	294
404	XK={3.+2.5*((RIP-36C.)/24C.)-.5*((RIP-360.)/240.))**2}* 1((5.6-CØSPP)/6.6)	295
405	TEMP={EXP (.0C55*RIP)-.19)*.19 XMLTP= (1.+(TEMP)*((1.+CØSRP)/2.))**3)/ 1((1.+(TEMP)*((1.+CØS(75./DPR))/2.))**3)	296
406	RHØ=RHØ*DCC=((SS/SØ)**XK) *XMLTP/9.81	297
	GØ TØ 503	298
503	RHØ=RHØ*.9.81	299
	RHØXX=RHØ	300
	TERM=CDAREA*RIØ*(SCRT(1.+2J*EI*CØSE(J) 1+EI*EI)/((1.+EI*CØSE(J))**2))	301
	STAPA(J)=TERM*(1.+CØSE(J))	302
	STEPP(J)=TERM*(1.-CØSE(J))	303
	J=J+1	304
	GØ TØ 1502	305
1500	INTA=0.	306
	INTP=0.	307
	TERM1=-86.4E6*SQRT(KERTH)/6.2831858*SQRT(AI)	308
	L=JCNT-1	309
	M=1	310
1506	IF(L)1504,1504,1505	311
1505	L=L-2	312
	INTA=INTA+STAPA(M)+STAPA(M+2)+STAPA(M+1)*4.	313
	INTP=INTP+STEPP(M)+STEPP(M+2)+STEPP(M+1)*4.	314
	M=M+2	315
	GØ TØ 1506	316
1504	CONTINUE	317
	INTA=INTA*DEØ3	318
	INTP=INTP*DEØ3	319
	ADØTP=TERM1*(INTA*(1.+EI)**2-SINTA)	320
	PDØTP=TERM1*(INTP*(1.-EI)**2-SINTP)	321
	IF(MASS-BCITIM)1601,160C,1601	322
1601	IF(MASS(3))16C3,16C2,16C3	323
1602	MT=MASS(2)	324
	GØ TØ 1700	325
1603	IF(TIME)16C2,1602,1604	326
1604	I=3	327
1607	IF(MT=MASS(I+1))16C5,16C6,1606	328
1606	MT=MASS(2)-MASS(I)*TIME	329
	GØ TØ 1700	330
1605	I=I+2	331
	IF(MASS(I)-ENCID)1,2,1	332
2	MT=MASS(I-1)	333
	GØTØ 1700	334
1	IF(I-24)1607,1607,7C01	335
1600	I=2	336
1803	IF(TIME=MASS(I+1))180C,18C1,1802	337
1802	I=I+2	338
	IF(MASS(I)-ENCID)3,4,3	339
		340

KILGØ PDAD		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
3	IF(I-24)18C3,18C3,7C01	√341
4	MT=MASS(I-2)	√342
	GØTØ 1700	√343
1800	IF(I-2)1801,1801,18C4	√344
1804	MT=MASS(I)	√345
	GØ TØ 1700	√346
1801	MT=MASS(I)	√347
1700	ADØT=ADØTP/MT	√348
	PDØT=PDØTP/MT	√349
	SADØTI=(ADØT+PDØT)/2.	√350
	PDØAD=PDØT/ADØT	√351
	TIMED=MT/ACØTP	√352
	REVØL=REV1+(TIME-TIME1)*1440./PDI	√353
	RETURN	√354
7001	WRITE(6,70C2)	√355 ,356
	CALL DUMP	√357
	STØP	√358
7002	FORMAT(1HØ2ØHTABLE VALUE EXCEEDED)	
	END	√359

KILGØ PRINTT		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
SUBROUTINE PRINTT			
REAL JJ,KERTH,INTA,INTP,MASS,MT,INTERA,INTERP,INC,NI			
DIMENSION DATE(3), XM0NTH(12)			
DIMENSION FTENB(153),FTEN(153),AP(153)			
DIMENSION CORREC(11C),SOLAR(3C1)			
DIMENSION TN(6),INTERA(6),TNI(6),INTERP(6),			
IC0SE(365),E(365),CDPRIM(25),AREA(45),CN(45),			
2ATTACK(45),STPA(365),STEPR(365),MASS(25)			
COMMON /ARCC/TEMPT,TEMK,PRESS,P0MP,			
1PSP0,RH0,RH0SR0,VISC,VISC5L,KVISC,VS,G			
DATA DPR/57.2557795/, PI/3.14159291/,SNBCI/6HSINE /			
1,BCITIM/6HTIME /			
DATA AID/6HA /,PID/6HP /,DETID/6HDETAIL/,			
1SH0ID/6HSH0RT /			
DATA BNDID/6HEND /			
COMMON/CLK/AP0,PER1,TIME,AE,SINI,W0,F,JJ,KERTH,			
IC0SI, JCNT,CDPRIM, AREA,ATTACK, CN,			
2MASS,AD0T,PD0T,PD0AC,TIMED			
3, C0SE,E,DA02,PER,TIME1,HH,DE03			
4,CAP0M1,CAPID,SMAM1,ADTM1,AP0M1,SMAM,SMACM1,SMAID,CAPM1,CAPW			
5,CAP0,DATE,XM0NTH,FTENB,AP			
6,INTERA,INTERP,CD,CAN0M,DAR0GE(10),CDA(5C)			
7,PRINT, CUTOFF(2), AI,RPAI,SAD0TI			
8,REV0L,MT,VPI,POI			
9,PN(6),AN(6),REV1			
1,CORREC,SOLAR,ATM0S,FTEN,DIURNL,XLAG,RH0XX,S0,SA			
1,EI,RIPP,RIPA,AMPR			
WRITE(6,151)AP0,PER1,AI,RPAI,AD0T,PD0T,SAD0TI,			
1MT,CAPW,SMAM,CAPID,SMAID,VPI,POI,REV0L,TIME,RH0XX			
1,EI,RIPP,RIPA			
RETURN			
151	FORMAT(1H06HA	E15.8,3X,6HP	E15.8,3X,6HAXIS E15.8,3X,
	16HRADIUSE15.8/,1X,6HAD0T	E15.8,3X,6HPD0T	E15.8,3X,
	26HAXID0TE15.8,3X,6HMASS	E15.8/,1X,6HN0DE	E15.8,3X,
	36HARGP	E15.8,3X,6HCN0DE	E15.8,3X,6HDARGP E15.8/,1X,
	46HVPERIGE15.8,3X,6HPERI0DE	E15.8,3X,6H0RBIT	E15.8,3X,
	56HTIME	E15.8/,1X,6H0	E15.8,3X,6HEI E15.8,3X,
	16HRIPERGE15.8,3X,6HRIPAPGE15.8/)		
END			

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SUBROUTINE RK
REAL JJ,KERTH,INTA,INTP,MASS,MT,INTERA,INTERP,INC,NI
DIMENSION CATE(3), XM0NTH(12)
DIMENSION FTENB(153),FTEN(153),AP(153)
DIMENSION C0RREC(11C),S0LAR(3C1)
DIMENSION TN(6),INTERA(6),TN1(6),INTERP(6),
1C0SE(365),E(365),CDPRIM(25),AREA(45),CN(45),
2ATTACK(45),STPA(365),STEPP(365),MASS(25)
COMMON /ARCC/TEMPT,TEMK,PRBSS,P0MP,
1PSP0,RH0,RH0SR0,VISC,VISC SL,KVISC,VS,G
DATA DPR/57.2957795/, P1/3.14159291/,SNBCI/6HSINE /
1,BCITIM/6HTIME /
DATA AID/6HA /,PID/6HP /,DETID/6HDETAIL/,
1SH0ID/6HSH0RT /
DATA BNDID/6HEND /
COMMON/CLK/AP0,PER1,TIME,AE,SINI,X0,F,JJ,KERTH,
1C0SI, JCNT,CDPRIM, AREA,ATTACK, CN,
2MASS,AD0T,PD0T,PD0AC,TIMED
3, G0SE,E,DA02,PER,TIME1,HH,DE03
4,CAPDM1,CAPID,SMAM1,ADTM1,AP0M1,SMAM,SMACM1,SMAID,CAPM1,CAPW
5,CAP0,DATE,XM0NTH,FTENB,AP
6,INTERA,INTERP,DD,CAN0M,DAR0GE(10I,CDA(5C)
7,PRINT, CUT0FF(2), AI,RPAI,SAD0TI
8,REV0L,MT,VPI,PCI
9,PN(6),AN(6),REV1
1,C0RREC,S0LAR,ATM0S,FTEN,DIURNL,XLAG,RH0XX,S0,SA
1,EI,RIPP,RIPA,AMPR
IF(AD0T)1,1,2
1 DA02=-ABS(CA02) #1
G0T03 #2
2 DA02=ABS(DA02) #3
3 C0NTINUE #4
CK1=DA02*PC0AC #5
PER1=PER+CK1 #6
AP0=AP0+DA02 #7
CK1X=DA02*TIMED #8
TIME=TIME1+CK1X #9
CALL PDAD #10
IF(AD0T)4,4,5 #11
4 DA02=-ABS(CA02) #12
G0T06 #13
5 DA02=ABS(DA02) #14
6 C0NTINUE #15
CK2=DA02*PC0AC #16
PER1=PER+CK2 #17
CK2X=DA02*TIMED #18
TIME=TIME1+CK2X #19
CALL PDAD #20
IF(AD0T)7,7,8 #21
7 DA02=-ABS(CA02) #22
G0T09 #23
8 DA02=ABS(DA02) #24
9 C0NTINUE #25
CK3=DA02*PC0AC #26
PER1=CK3+CK3+PER #27

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KILGØ RK		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	APØ=APØ+DAØ2	✓29	
	CK3X=DAØ2*TIMED	✓30	
	TIME=CK3X+CK3X+TIME1	✓31	
	CALL PØAD	✓32	
	IF(ADØT)10,10,11	✓33	
10	DAØ2=-ABS(DAØ2)	✓34	
	GØTØ12	✓35	
11	DAØ2=ABS(DAØ2)	✓36	
12	CØNTINUE	✓37	
	DELT=((DAØ2*PCØAD)+CK3+CK2+CK1+CK2+CK3)/3.	✓38	
	PER1=DELT+PER	✓39	
	TIME=((DAØ2*TIMED)+CK3X+CK2X+CK1X+CK2X 1+CK3X)/3.)+TIME1	✓40	
	CALL PØAD	✓41	
	IF(ADØT)13,13,14	✓42	
13	DAØ2=-ABS(DAØ2)	✓43	
	GØTØ15	✓44	
14	DAØ2=ABS(DAØ2)	✓45	
15	CØNTINUE	✓46	
	ACTM1=ADØT	✓47	
	SMAØM1=SMA1D	✓48	
	CAPØM1=CAP1D	✓49	
	SMAØM1=SMAØW	✓50	
	CAPØM1=CAPØW	✓51	
	APØØM1=APØ	✓52	
	REV1=REVØU	✓53	
	RETURN	✓54	
	END	✓55	

KILGØ PØEAT		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
C	HG=GEOMETRIC ALTITUDE	0406
C	N=LENGTH OF TABLE	0407
C	HB=ALTITUDE BASE	0408
C	ATMOSPHERE DATA LØZKUP-GSK	0409
C	RHØB=BASE DENSITY	0412
C	GIVEN HG,N,HB(1) TØ HB(N),TMB(1) TØ TMB(N),GLMB(1) TØ	0417
C	GLMB(N),RHØB(1) TØ RHØB(N)	0418
C	COMPUTE T,RHØ,P,V	0419
C	R=GEOCENTRIC DISTANCE OF THE FIELD POINT	0420
C	CLS,CMS,CNS=DIRECTION COSINES OF SUN	0421
C	CL,CM,CN=DIRECTION COSINES OF FIELD POINT	0422
C	AVERAGE LONGITUDINAL LAG OF DIURNAL BULGE=.55 RADIAN	0423
C	SEPS,CEPS=SINE AND COSINE OF THE INCLINATION OF THE ECLIPTIC	0424
C	PSIP=GEOCENTRIC ANGLE BETWEEN DIURNAL BULGE AND FIELD POINT	0425
C		0426
	SUBROUTINE PØEAT(HG,RHØ,D,X,Y,Z,R)	
	DIMENSION HB(18),TMB(18),GLMB(18),RHØB(18)	0428
	IF(N-12)500,1C,500	
500	CONTINUE	0430
	N=12	0431
	HB(1)=0.	0432
	HB(2)=36089.239	0433
	HB(3)=82020.997	0434
	HB(4)=154199.475	0435
	HB(5)=173884.514	0436
	HB(6)=259186.352	0437
	HB(7)=295275.591	0438
	HB(8)=344488.189	0439
	HB(9)=524934.383	0440
	HB(10)=557742.782	0441
	HB(11)=656167.979	0442
	HB(12)=2296587.93	0443
	TMB(1)=518.69	0444
	TMB(2)=389.988	0445
	TMB(3)=389.988	0446
	TMB(4)=508.788	0447
	TMB(5)=508.788	0448
	TMB(6)=298.188	0449
	TMB(7)=298.188	0450
	TMB(8)=406.188	0451
	TMB(9)=2386.188	0452
	TMB(10)=2566.188	0453
	TMB(11)=2836.188	0454
	TMB(12)=5986.188	0455
	GLMB(1)=-3.56616E-3	0456
	GLMB(2)=0.	0457
	GLMB(3)=1.646592E-3	0458
	GLMB(4)=0.	0459
	GLMB(5)=-2.46888E-3	0460
	GLMB(6)=0.	0461
	GLMB(7)=2.19456E-3	0462
	GLMB(8)=1.09728E-2	0463
	GLMB(9)=5.4864E-3	0464
	GLMB(10)=2.7432E-3	0465
	GLMB(11)=1.92024E-3	0466

KILGØ PRÆT		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	GLMB(12)=1.92024E-3	0467	✓39
	RHØB(1)=2.3765E-3	0468	✓40
	RHØB(2)=7.0547E-4	0469	✓41
	RHØB(3)=7.7615E-5	0470	✓42
	RHØB(4)=2.8829E-6	0471	✓43
	RHØB(5)=1.3964E-6	0472	✓44
	RHØB(6)=4.1123E-8	0473	✓45
	RHØB(7)=4.2560E-9	0474	✓46
	RHØB(8)=2.2243E-10	0475	✓47
	RHØB(9)=1.8477E-12	0476	✓48
	RHØB(10)=1.3357E-12	0477	✓49
	RHØB(11)=6.1161E-13	0478	✓50
	RHØB(12)=4.468E-16	0479	✓51
10	PI=3.14159265	0480	✓52
	HG=FG*3280.833		✓53
	T1=C.017203*D	0481	✓54
	TENBE=2.30258509	0482	✓55
	SLAMB=T1+0.0335*SIN (T1)-1.41C		✓56
	SEPS=SIN (.4052)		✓57
	CEPS=CØS (.4052)		✓58
	CLS=CØS (SLAMB)		✓59
	SSLAMB=SIN (SLAMB)		✓60
	CMS=SSLAMB*CEPS	0488	✓61
	CNS=SSLAMB*SEPS	0489	✓62
1	HNM=HG/6076.1C03	0490	✓63
	H=(20855531.*FG)/(20855531.+HG)	0491	✓64
100	DØ 111 I=1,N	0492	✓65
	IF(H-HB(I))121,111,111	0493	✓66
111	CONTINUE	0494	✓67
200	T=TPB(N)+GLMB(N)*(H-HB(N))	0495	✓69
	GØ TØ 50	0496	✓70
121	IF(I-1)123,122,123	0497	✓71
122	I=2	0498	✓72
123	IF(GLMB(I-1))131,141,131	0499	✓73
141	I=TPB(I-1)	0500	✓74
	RHØ=RHØB(I-1)*EXP (-(H-HB(I-1))*32.1740485/(1716.4827* 1TMB(I-1)))	0502	✓75
	GØ TØ 60	0503	✓76
131	T=TPB(I-1)+GLMB(I-1)*(H-HB(I-1))	0504	✓77
	RHØ=RHØB(I-1)*EXP (-(1.+32.1740485/(1716.4827*GLMB 1(I-1)))*ALØG (T/TPB(I-1)))		✓78
	GØ TØ 60	0507	✓79
50	RHØ=RHØB(N)*EXP (-(1.+32.1740485/(1716.4827*GLMB(N)) 1*ALØG (T/TPB(N)))		✓80
60	V=SCRT (1.4*(1716.4827*T))		✓81
	P=PFØ*(1716.4827*T)	0511	✓82
	IF(C)1000,100C,260	0512	✓83
1000	RETURN	0513	✓84
260	CN=Z/R	0514	✓85
202	IF(HNM-76.)10C0,10CC,25C	0517	✓86
250	CL=X/R	0518	✓87
	CM=Y/R	0519	✓88
	CLCLS=CL*CLS	0520	✓89
	CMCMS=CM*CMS	0521	✓90
	CNCNS=CN*CNS	0522	✓91
	CØPSIP=(CLCLS+CMCMS)*CØS (.255)+(CN*CLS-CL*CMS)		

KILGØ PØEAT		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
	1*SIN (.55)+CN*CNS		#92
	F10=1.5+28*CØS (PI*C/2C10.)		#93
	FB=.85*F10	0526	#94
	IF (HNM-108.) 3C0,35C,3C1	0527	#95
301	IF (HNM-378.) 350,4CC,4CC	0528	#96
138	RHØ=RHØ*(1.-0.3*CN**3*(1.-CØS (2.*PI*(HNM-16.)/34.))		
	1*CØS (2.*PI*(C+9.)/365.))		#97
	P=RFØ*(1716.4827*T)	0521	#98
	V=SCRT (1.4*(1716.4827*T))		#99
	RETURN	0523	#100
300	RHØ=5.606E-12*(76./HNM)**7.18*((1C8.-HNM)/32.+FB*	0524	
	1*(HNM-76.)/32.))*(4.0/3.0))*(1.+(HNM-76.)/153.*((1.+CØPSIP)/2.))	0525	
	2**3)	0536	#101
	P=RFØ*(1716.4827*T)	0527	#102
	V=SCRT (1.4*(1716.4827*T))		#103
	RETURN	0529	#104
350	RHØ=FB*EXP (TENBE*(-15.738-.0C368*HNM+6.363*EXP (-.0048		
	1*HNM)))*(1.+.19*(EXP (0.0102*HNM)-1.9)*((1.+CØPSIP)/2.))**3)		#105
	P=RFØ*(1716.4827*T)	0542	#106
	V=SCRT (1.4*(1716.4827*T))		#107
	RETURN	0544	#108
400	RHØ=0.00504*F10/(HNM)**5*((1.+CØPSIP)/2.))**3*(1.-6.E+6	0545	
	1/HNM**3)+6.E+6/HNM**3)	0546	#109
	P=RFØ*(1716.4827*T)	0547	#110
	V=SCRT (1.4*(1716.4827*T))		#111
	RETURN	0549	#112
	END	055C	#113

KILGØ SMATMS		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
	SUBROUTINE SMATMS(X,Y,Z,SS,T,RHØ,HKM)	
	DIMENSION RHØS (53)	
	S=SS	✓1
	IF (IFLAG-1) 600,300,600	✓2
600	CONTINUE	✓3
	PI=2.1415927	✓4
	PI2=2.*PI	✓5
	PI4=4.*PI	✓6
	CØNV=920.	✓7
	RHØS=0.	✓8
	RHØS(2)=0.	✓9
	RHØS(3)=0.C	✓10
	RHØS(4)=1.225E-3	✓11
	RHØS(5)=0.	✓12
	RHØS(6)=1.225E-3	✓13
	DØ9C I=7.49,2	✓14
90	RHØS(I)=RHØS(I-2)+5.	✓15, 16
	RHØS(8)=7.3643E-4	✓17
	RHØS(10)=4.1351E-4	✓18
	RHØS(12)=1.9475E-4	✓19
	RHØS(14)=8.8910E-5	✓20
	RHØS(16)=4.0084E-5	✓21
	RHØS(18)=1.8410E-5	✓22
	RHØS(20)=8.4624E-6	✓23
	RHØS(22)=3.9957E-6	✓24
	RHØS(24)=1.9663E-6	✓25
	RHØS(26)=1.0269E-6	✓26
	RHØS(28)=5.6C75E-7	✓27
	RHØS(30)=3.0592E-7	✓28
	RHØS(32)=1.6665E-7	✓29
	RHØS(34)=8.7535E-8	✓30
	RHØS(36)=4.325E-8	✓31
	RHØS(38)=1.959E-8	✓32
	RHØS(40)=7.955E-9	✓33
	RHØS(42)=3.170E-9	✓34
	RHØS(44)=1.265E-9	✓35
	RHØS(46)=5.070E-10	✓36
	RHØS(48)=2.07CE-10	✓37
	RHØS(50)=8.75CE-11	✓38
	RHØS(51)=116.C	✓39
	RHØS(52)=3.253E-11	✓40
	RHØS(53)=1.E22	✓41
	IFLAG=1	✓42
300	R=SCRT (X**2+Y**2+Z**2)	✓43
	CL=X/R	✓44
	CM=Y/R	✓45
	CN=Z/R	✓46
	IF (HKM) 200,200,2C1	✓47
200	RHØ =2.3765E-3	✓48
	GØ TØ 1000	✓49
201	IF (HKM-116.) 311,312,312	✓50
311	CALL TBL (HKM,RHØS)	✓51
	IF (HKM-30.) 110,11C,111	✓52
111	IF (HKM-90.) 112,112,11C	✓53
112	C=1.-0.3*CN**3*(1.-CØS (PI2*((HKM-3C.)/60.)))*CØS (PI2*((T-36194.))	

KILGØ SMATMS		06/18/65
EXTERNAL FØRMULA NUMBER	SOURCE STATEMENT	INTERNAL FØRMULA NUMBER(S)
	1/365.25))	✓54
	RHØ=RHØS*G	✓55
	GØ TØ 1000	✓56
110	RHØ=RHØS	✓57
	GØ TØ 1000	✓58
312	CØNTINUE	✓59
	HKM=HKM+4.*C	✓60
	IF (S) 100,10C,101	✓61
100	FBAR=135.+75.*CØS (PI2*(T-36340.)/4C90.)+15.*CØS (PI4*(T-3603C.))	
	1/4090.)	✓62
	TCØN=(T-38C47.)/365.25	✓63
	GT=.025*CØS (PI2*TCØN)-.06*CØS (PI4*TCØN)	✓64
	S=(50.+.*FBAR)*EXP (GT)	✓65
101	CALL HPC(CL,CM,CN,FKM,S,T,RHØHC)	✓66
	RHØ=RHØHC*CØNV	✓67
1000	RETURN	✓68
	END	✓69

KILGØ TBL		06/18/65
EXTERNAL FØRMULA NUMBER	SOURCE STATEMENT	INTERNAL FØRMULA NUMBER(S)
	SUBRØUTINE TBL (HKM,RHØS)	
	DIMENSION RHØS(1)	
	DØ 10 I=5,51,2	✓1
	IF(FKM-RHØS(I))20,3C,10	✓2
10	CØNTINUE	✓3 ,4
20	RHØS=RHØS(I-1)+(RHØS(I+1)-RHØS(I-1))*(HKM	
	1-RHØS(I-2))/(RHØS(I)-RHØS(I-2))	✓5
25	RETURN	✓6
30	RHØS=RHØS(I+1)	✓7
	GØ TØ 25	✓8
	END	✓9

```

SUBROUTINE HPC(CL,CM,CN,HKM,S,T,RH0A)
  DIMENSION S1(35),S2(35),S3(35),S4(35),S5(35),SS1(35),SS2(35),
  1SS3(35),SS4(35),SS5(35),Q(3,3),P(3),H(35),R(3,3),PP(3),C(5)
  DATA (S1(I),I=1,35)/
  1-24.065,-25.887,-27.310,-28.493,-29.530,-31.299,-32.772,
  1-34.068,-35.267,-36.395,-37.447,-38.396,-39.194,-39.817,
  1-40.289,-40.660,-40.973,-41.257,-41.524,-41.782,-42.033,
  1-42.280,-42.523,-42.762,-42.996,-43.566,-44.109,-44.622,
  1-45.101,-45.541,-45.938,-46.293,-46.604,-46.875,-47.109/
  DATA (S2(I),I=1,35)/
  1-24.065,-25.904,-27.228,-28.284,-29.197,-30.758,-32.072,
  1-33.218,-34.260,-35.235,-36.161,-37.044,-37.871,-38.620,
  1-39.268,-39.804,-40.232,-40.577,-40.864,-41.114,-41.344,
  1-41.560,-41.768,-41.970,-42.167,-42.648,-43.111,-43.557,
  1-43.985,-44.355,-44.784,-45.152,-45.496,-45.816,-46.111/
  DATA (S3(I),I=1,35)/
  1-24.065,-25.930,-27.137,-28.046,-28.814,-30.120,-31.232,
  1-32.213,-33.094,-33.903,-34.670,-35.400,-36.102,-36.777,
  1-37.424,-38.036,-38.607,-39.125,-39.584,-39.981,-40.317,
  1-40.601,-40.844,-41.056,-41.246,-41.664,-42.041,-42.397,
  1-42.738,-43.069,-43.389,-43.698,-43.997,-44.286,-44.564/
  DATA (S4(I),I=1,35)/
  1-24.065,-25.954,-27.077,-27.889,-28.558,-29.681,-30.643,
  1-31.496,-32.270,-32.983,-33.646,-34.272,-34.869,-35.443,
  1-35.998,-36.536,-37.056,-37.558,-38.039,-38.496,-38.924,
  1-39.320,-39.680,-40.002,-40.287,-40.856,-41.282,-41.625,
  1-41.927,-42.207,-42.473,-42.729,-42.977,-43.217,-43.451/
  DATA (S5(I),I=1,35)/
  1-24.065,-25.976,-27.036,-27.783,-28.385,-29.377,-30.221,
  1-30.990,-31.669,-32.304,-32.896,-33.454,-33.984,-34.490,
  1-34.976,-35.446,-35.903,-36.347,-36.778,-37.197,-37.604,
  1-37.997,-38.375,-38.736,-39.077,-39.837,-40.443,-40.912,
  1-41.278,-41.577,-41.835,-42.069,-42.287,-42.495,-42.696/
  DATA (SS1(I),I=1,35)/
  1-24.065,-25.852,-27.238,-28.339,-29.227,-30.677,-31.866,
  1-32.888,-33.805,-34.657,-35.464,-36.233,-36.963,-37.658,
  1-38.307,-38.859,-39.421,-39.869,-40.242,-40.553,-40.816,
  1-41.043,-41.247,-41.435,-41.612,-42.027,-42.420,-42.797,
  1-43.162,-43.514,-43.854,-44.182,-44.497,-44.799,-45.087/
  DATA (SS2(I),I=1,35)/
  1-24.065,-25.867,-27.155,-28.153,-28.950,-30.214,-31.250,
  1-32.149,-32.953,-33.685,-34.370,-35.022,-35.648,-36.252,
  1-36.836,-37.398,-37.935,-38.443,-38.915,-39.348,-39.735,
  1-40.075,-40.371,-40.626,-40.848,-41.300,-41.668,-41.996,
  1-42.301,-42.564,-42.877,-43.150,-43.416,-43.673,-43.922/
  DATA (SS3(I),I=1,35)/
  1-24.065,-25.893,-27.067,-27.948,-28.653,-29.731,-30.599,
  1-31.352,-32.027,-32.646,-33.222,-33.765,-34.279,-34.773,
  1-35.248,-35.708,-36.153,-36.586,-37.007,-37.415,-37.811,
  1-38.193,-38.558,-38.907,-39.235,-39.959,-40.536,-40.983,
  1-41.334,-41.623,-41.874,-42.103,-42.317,-42.522,-42.719/
  DATA (SS4(I),I=1,35)/
  1-24.065,-25.921,-27.012,-27.813,-28.451,-29.424,-30.184,
  1-30.841,-31.421,-31.971,-32.474,-32.945,-33.392,-33.817,
  1-34.223,-34.614,-34.992,-35.358,-35.715,-36.062,-36.402,

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KILGØ HPC

06/18/85

EXTERNAL FORMULA NUMBER

SOURCE STATEMENT

INTERNAL FORMULA NUMBER(S)

```

1-36.733,-37.057,-37.373,-37.681,-38.414,-39.088,-39.689,
1-40.208,-40.645,-41.004,-41.300,-41.548,-41.762,-41.952/
DATA (SS(I),I=1,35)/
1-24.065,-25.947,-26.978,-27.721,-28.309,-29.211,-29.898,
1-30.488,-31.016,-31.500,-31.950,-32.372,-32.772,-33.151,
1-33.513,-33.859,-34.192,-34.514,-34.826,-35.128,-35.423,
1-35.710,-35.950,-36.265,-36.534,-37.182,-37.798,-38.379,
1-38.923,-39.425,-39.880,-40.285,-40.639,-40.945,-41.206/
PARF(X,Y,Z)=X+DT*(Y*(DT2-DT)/DT1+Z*(DT1+CT)/(CT2)/(DT1+DT2)
IF(IFLAG-1)601,600,601
601 CONTINUE
H(1)=120.
DO 1400 I=1,34
IF(I-4)1030,1030,1031
1030 H(I+1)=H(I)+2C.
GO TO 1400
1031 IF(I-24)1032,1032,1033
1032 H(I+1)=H(I)+4C.
GO TO 1400
1033 H(I+1)=H(I)+1C0.
1400 CONTINUE
PI=3.1415927
IFLAG=1
600 CONTINUE
CAPM=.2017203*(T-36203.)
SL=CAPM+.0335*SIN (CAPM)-1.41
CLS=COS (SL)
SINSL=SIN (SL)
CMS=.9175*SINSL
CNS=.3977*SINSL
400 DO 20 I=1,35
DT=F(I)-HKM
IF(CT)20,21,21
20 CONTINUE
GO TO 9001
21 LPT=I
IF(I-35)1002,5001,5001
9001 RH0A=0.0
GO TO 3000
1002 CONTINUE
DT1=H(LPT)-H(LPT-1)
DT2=H(LPT+1)-H(LPT)
DT=-DT
IF(S-150.)30,31,31
30 DO 40 I=1,3
LP=LPT-2+I
Q(1,I)=S1(LP)
Q(2,I)=S2(LP)
40 Q(3,I)=S3(LP)
IG0=1
42 DO 41 I=1,3
Q1=Q(I,2)
Q2=Q(I,2)-Q(I,1)
Q3=Q(I,3)-Q(I,2)
41 P(I)=PARF(Q1,Q2,Q3)
GO TO (5000,5001),IG0

```

KILGØ HPC		06/18/65	
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)	
5000	DØ 240 I=1,3	✓52	
	LP=LPT-2+I	✓53	
	R(1,I)=SS1(LP)	✓54	
	R(2,I)=SS2(LP)	✓55	
240	R(3,I)=SS3(LP)	✓56	✓57
5001	DØ 241 I=1,3	✓58	
	R1=R(I,2)	✓59	
	R2=R(I,2)-R(I,1)	✓60	
	R3=R(I,3)-R(I,2)	✓61	
241	PP(I)=PARF(R1,R2,R3)	✓62	✓63
	GØ TØ (43,44),IGØ	✓64	
43	DT=S-100.	✓65	
	DT1=30.	✓66	
	DT2=50.	✓67	
45	RHØN=EXP (PARF(P(2),P(2)-P(1),P(3)-P(2)))	✓68	
	RHØX= EXP (PARF(PP(2),PP(2)-PP(1),PP(3)-PP(2)))	✓69	
	GØ TØ 410	✓70	
31	DØ 140 I=1,3	✓71	
	LP=LPT-2+I	✓72	
	Q(1,I)=S3(LP)	✓73	
	Q(2,I)=S4(LP)	✓74	
140	Q(3,I)=S5(LP)	✓75	✓76
	IGØ=2	✓77	
	DØ 340 I=1,3	✓78	
	LP=LPT-2+I	✓79	
	R(1,I)=SS3(LP)	✓80	
	R(2,I)=SS4(LP)	✓81	
340	R(3,I)=SS5(LP)	✓82	✓83
	GØ TØ 42	✓84	
44	DT=S-200.	✓85	
	DT1=50.	✓86	
	DT2=50.	✓87	
	GØ TØ 45	✓88	
410	SIG=(S-160.)/50.	✓89	
	SIG2=SIG**2	✓90	
	PHIN=591.+32.5*SIG-8.5*SIG2	✓91	
	PHIM=96.+20.*SIG+10.*SIG2	✓92	
	HN=1115.+507.5*SIG+52.5*SIG2	✓93	
	DELH=590.+355.*SIG+25.*SIG2	✓94	
	HS=325.+27.*SIG-5.*SIG2	✓95	
	ZETA=([HKM-HN]/DELH)**2	✓96	
	FZ=-.06+.03*ZETA+1.C6*EXP (-3.7*ZETA)	✓97	
	PHI=PI*(PHIN-PHIM*FZ-4.47+.01174*HKM+EXP (-.04*(HKM-HS)))/1200.	✓98	
	IF(PHI-2.)420,421,421	✓99	
421	PHI=2.	✓100	
	GØ TØ 430	✓101	
420	IF(PHI-1.)425,430,430	✓102	
425	PHI=1.	✓103	
430	EPSI=ALØG (1.+SQRT (RHØX/RHØN))/ALØG (2./((1.+CØS (PHI)))	✓104	
	GAMMA=PI*(118.5+30.*EXP (-.00567*(HKM-200.))+EXP (-.01455*(HKM-200.		
	1)))+(118.5+21.5*EXP (-.0315*(HKM-200.))*SIG+4.*(1.-SIG2))/180.	✓105	
	IF(GAMMA-5.)320,320,2003	✓106	
2003	GAMMA=5.	✓107	
320	CPSIPU=(CL*CLS+CM*CMS)*CØS (GAMMA)+(CM*CLS-CL*CMS)*SIN (GAMMA)+CN*		
	ICNS	✓108	
1000	RHØA=RHØN+ (R-ØX-RHØN)*((1.+CPSIPL)/2.)*EPSI	✓109	

KILG8 HPC		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
1001	BETA=TAN2PI((CLJ,CM)-TAN2PI((CLS,CM91-190.*GAMMA/PI	#110
2002	IF(BETA) 2000,2001,2001	#111
2000	BETA=BETA+360.	#112
	G0 T0 2002	#113
2001	CONTINUE	#114
700	AMP=HKM/4000.+(.91+.44*SIG+.38*SIG2)*EXP (-(2.-HKM/(405.+143.*SIG)	#115
	1)*.2)	#116
710	AMPS=.245+.0425*SIG-.0625*SIG2	#117
	U=AMP*(-.08*EXP (-(BETA-250.)/55.))*2)+AMPS*EXP (-(BETA-135.)/	#118
	134.)*.2))*AMP*.4.E-6*BETA	#119
	FACT=1.+(1.-CN*.2)*L	#120
	RH0A=RH0A*FACT	#121
3000	RETURN	
	END	

KILG8 TAN2PI		06/18/65
EXTERNAL FORMULA NUMBER	SOURCE STATEMENT	INTERNAL FORMULA NUMBER(S)
	FUNCTION TAN2PI(X,Y)	
C	TAN2PI=ARCTAN(Y/X)	C985
C	TAN2PI EQUAL OR LESS THAN 2PI	C986
C	TAN2PI EQUAL OR GREATER THAN ZERO	C987
	RADCEG=57.2957795	C988 #1
	IF(Y)1;2;3	C989 #2
2	IF(X)5;4;6	C990 #3
4	TAN2PI=1.0E+30	C991 #4
	G0 T0 20	C992 #5
5	TAN2PI=180.0	C993 #6
	G0 T0 20	C994 #7
6	TAN2PI=0.0	C995 #8
	G0 T0 20	C996 #9
1	IF(X)7;8;9	C997 #10
7	TAN2PI=180.+RADCEG*ATAN(Y/X)	C998 #11
	G0 T0 20	C999 #12
8	TAN2PI=270.0	C9991 #13
	G0 T0 20	C9992 #14
9	TAN2PI=360.+RADCEG*ATAN(Y/X)	C9993 #15
	G0 T0 20	C9994 #16
3	IF(X)7;10;11	C9995 #17
10	TAN2PI=90.0	C9996 #18
	G0 T0 20	C9997 #19
11	TAN2PI=RADCEG*ATAN(Y/X)	C9998 #20
20	RETURN	C9999 #21
	END	C999J #22

REFERENCES

1. Kilgo, H. F.: MSFC/LMSC Satellite Orbit Decay and Orbital Lifetime Program. Lockheed Missiles and Space Company Technical Report HREC/0082-1, LMSC/HREC A710725, June 18, 1965.
2. Small, H. W.: Atmospheric Density Between 70 and 200 Nautical Miles from Satellite Observations. Lockheed Missiles and Space Company, Tracking Note No. 23, LMSC/A376332, Sunnyvale, California, July 1964.
3. Solar Geophysical Data, Part B. U. S. Department of Commerce, National Bureau of Standards, Central Radio Propagation Laboratory, Boulder, Colorado.
4. Jacchia, Luigi G.: A Variable Atmospheric - Density Model from Satellite Accelerations. Smithsonian Institution Astrophysical Observatory Special Report No. 39. Cambridge, Massachusetts, March 30, 1960.
5. Kurtz, H. F., Jr.; Naumcheff, M.; and McNair, Ann R.: Orbital Tracking and Decay Analysis of the Saturn I Flights. AIAA/NASA Flight Testing Conference Paper Number 65-215, February 1965.
6. Nicolet, M.: Solar Radio Flux and Temperature of the Upper Atmosphere. J. Geophys. Rev. Vol. 68, No. 22, November 15, 1963.
7. Poe, R. F.: A Review of the Geophysical Model. Lockheed Missiles and Space Company, Tracking Note No. 2, LMSC/4082333, Sunnyvale, California, September 25, 1961.
8. Ladner, James E.; and Ragsdale, George C.: Earth Orbital Satellite Lifetime. George C. Marshall Space Flight Center Report MTP-AERO-62-77, Huntsville, Alabama, October 14, 1962.

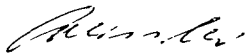
EARTH ORBITAL LIFETIME PREDICTION MODEL AND PROGRAM

By

Ann R. McNair and Edward P. Boykin

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